

Part 2:

Computational Models of Single Cell Astrocytes and Neuron-Astrocyte Interactions

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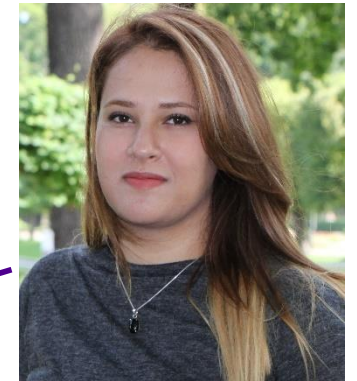
Astrocyte centered modeling (current members)



Kerstin Lenk
Academy of Finland
Postdoctoral Researcher



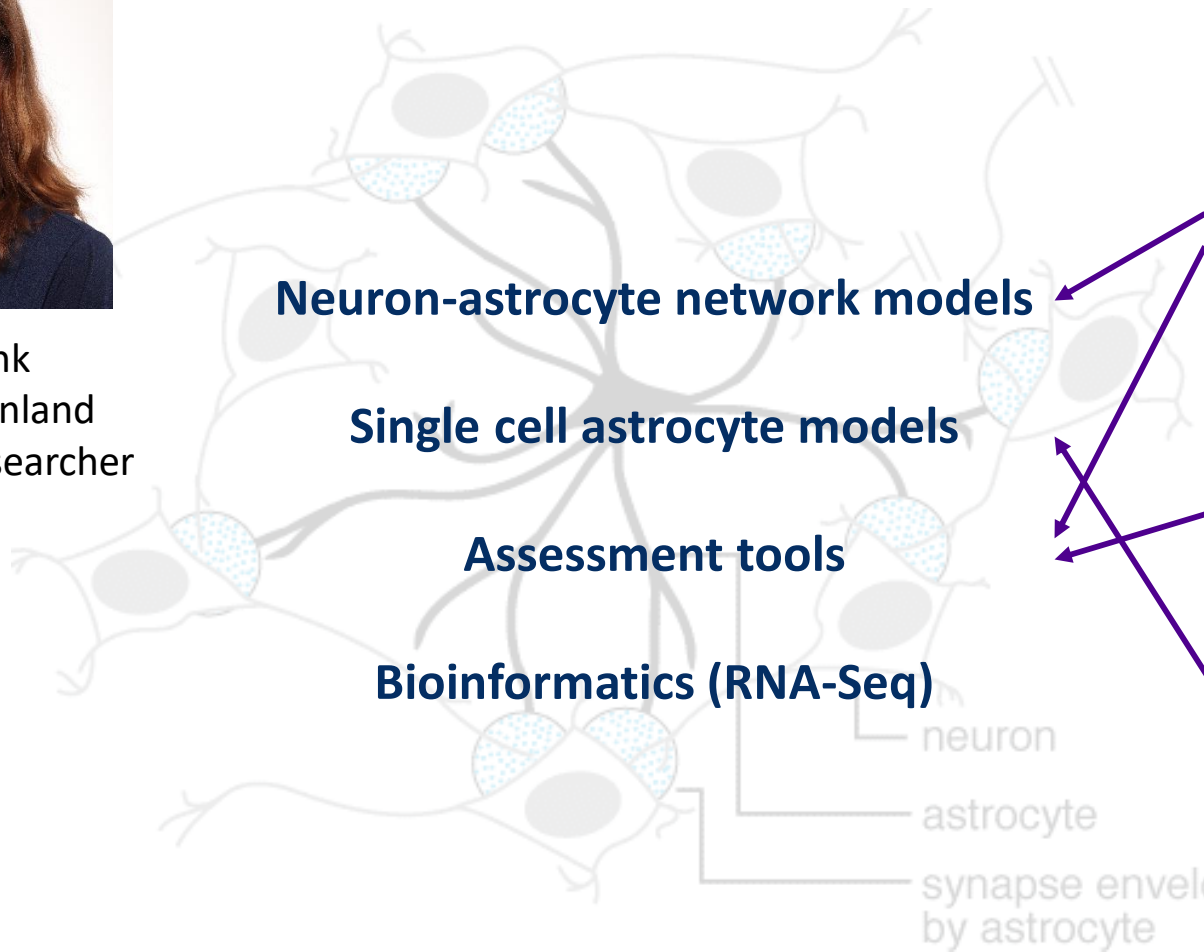
Barbara Genocchi
PhD student



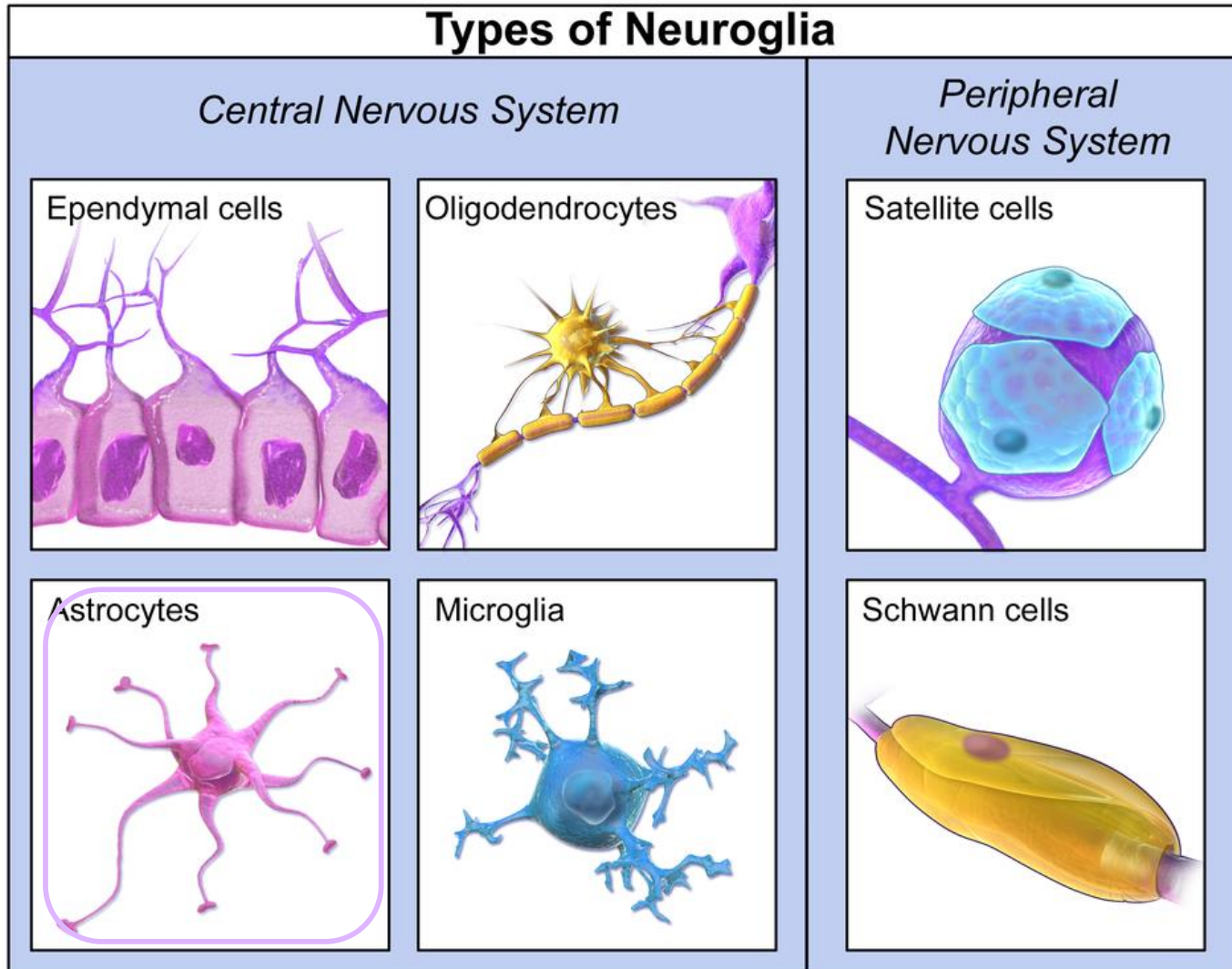
Sama Saeid
Master's student



Aapo Tervonen
PhD student



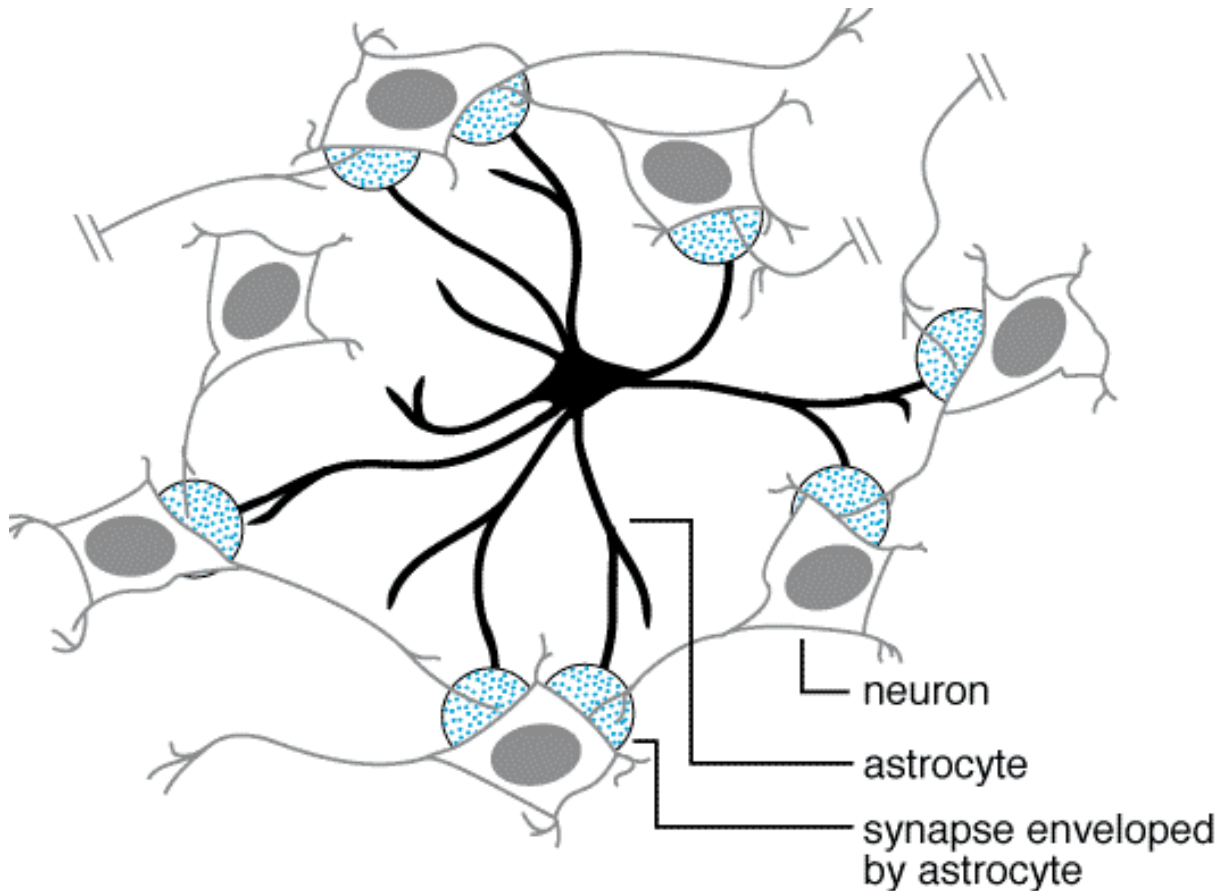
Glia cell types



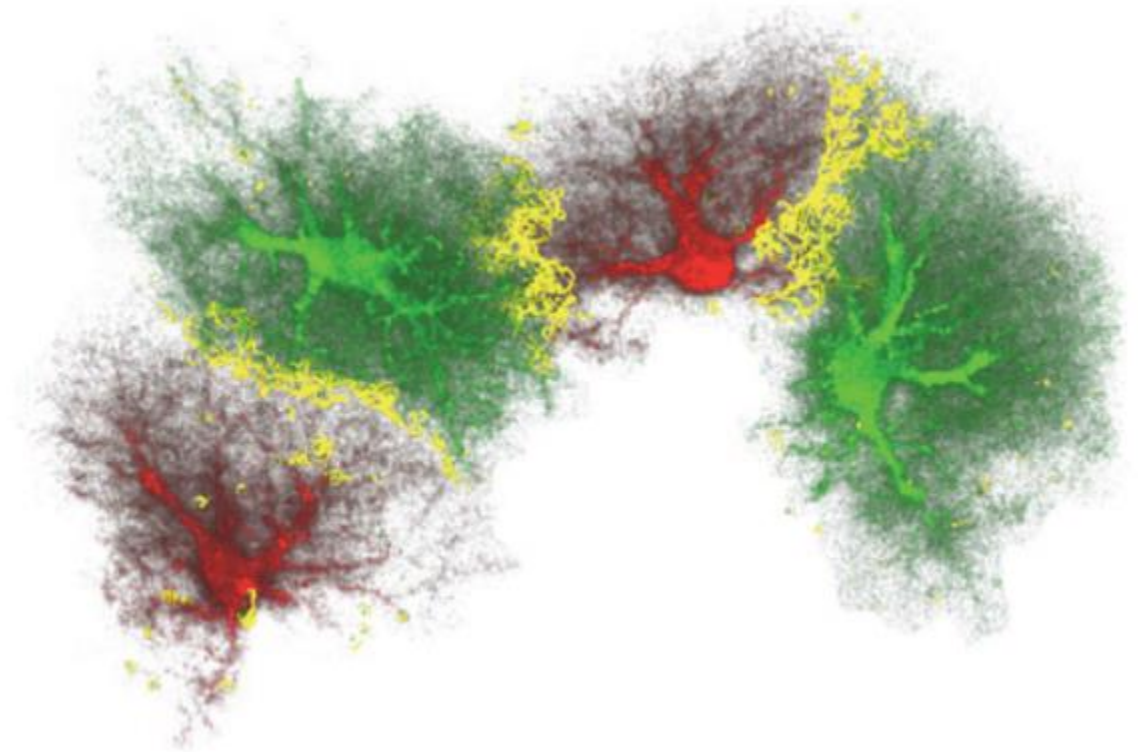
- Ependymal cells – spinal cord, blood-cerebrospinal fluid barrier
- Oligodendrocyte – insulation
- Microglia – immune response, synapse formation/pruning
- Astrocyte – tight junctions, nutrients, modulation of neuronal activity
- Satellite cells – regulate the external chemical environment
- Schwann cell – insulation of axons in peripheral nervous system

Astrocytes are more than support cells

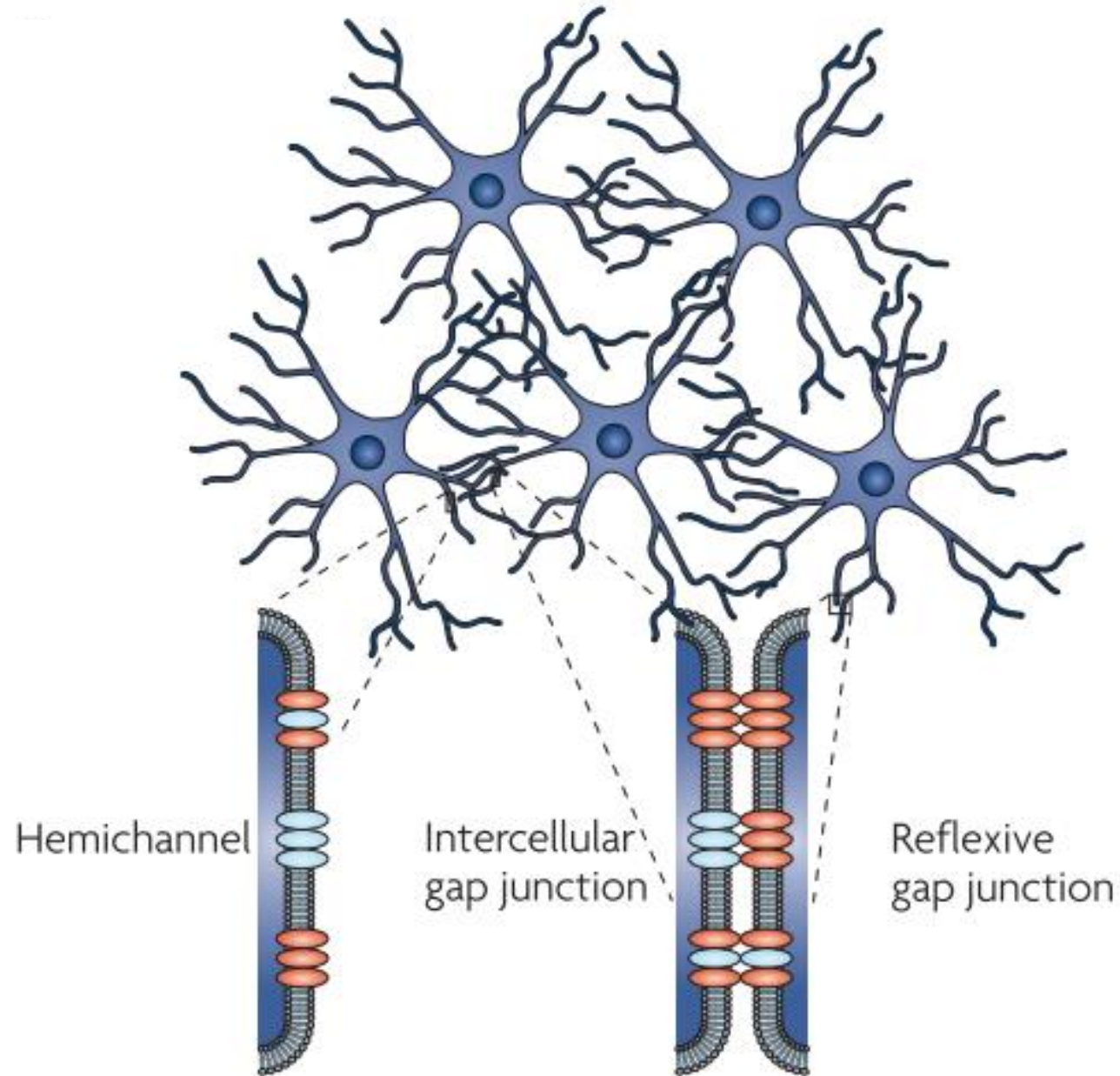
Neuron-astrocyte connections



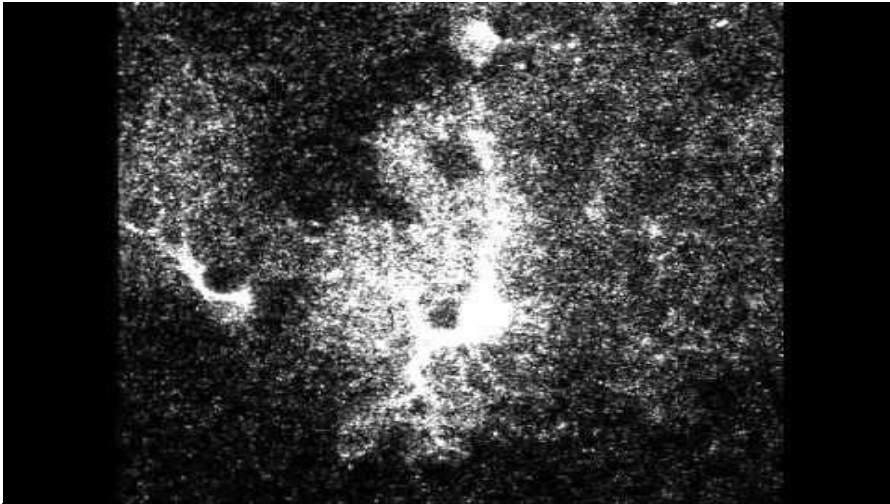
Astrocyte-astrocyte connections



Gap junction coupling between astrocytes



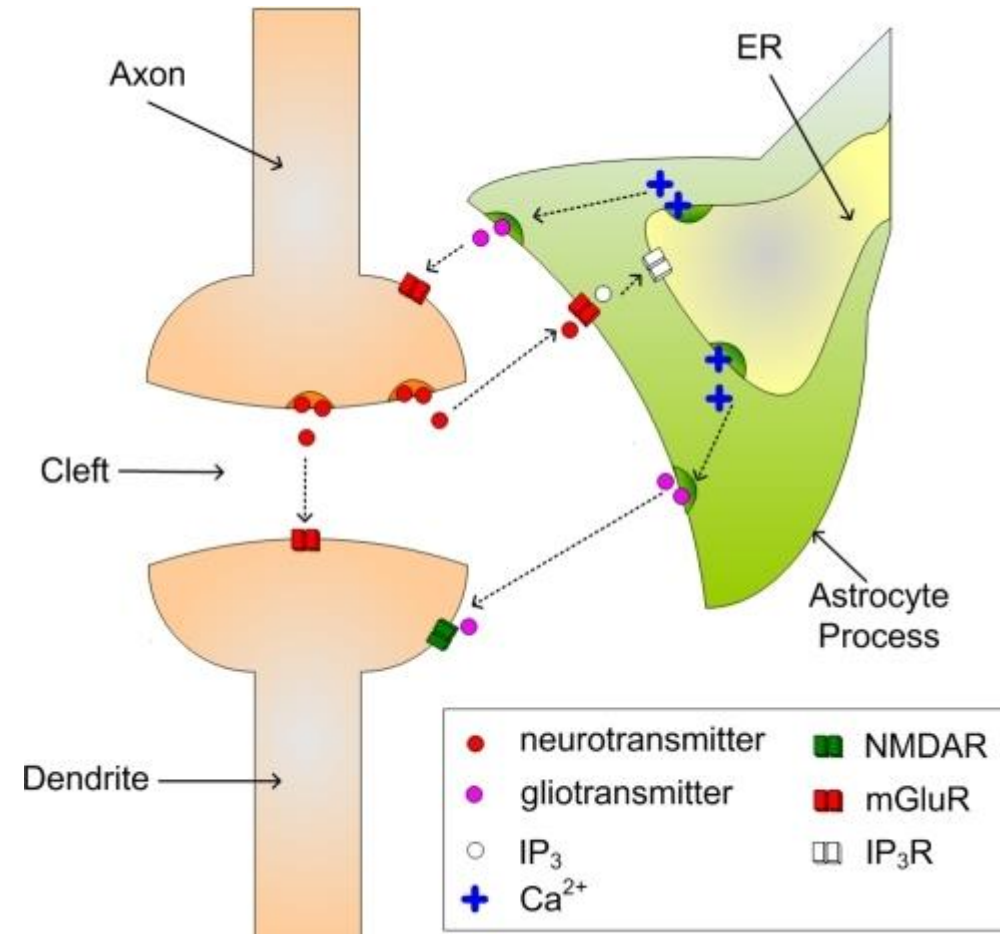
Calcium signalling in the tripartite synapse



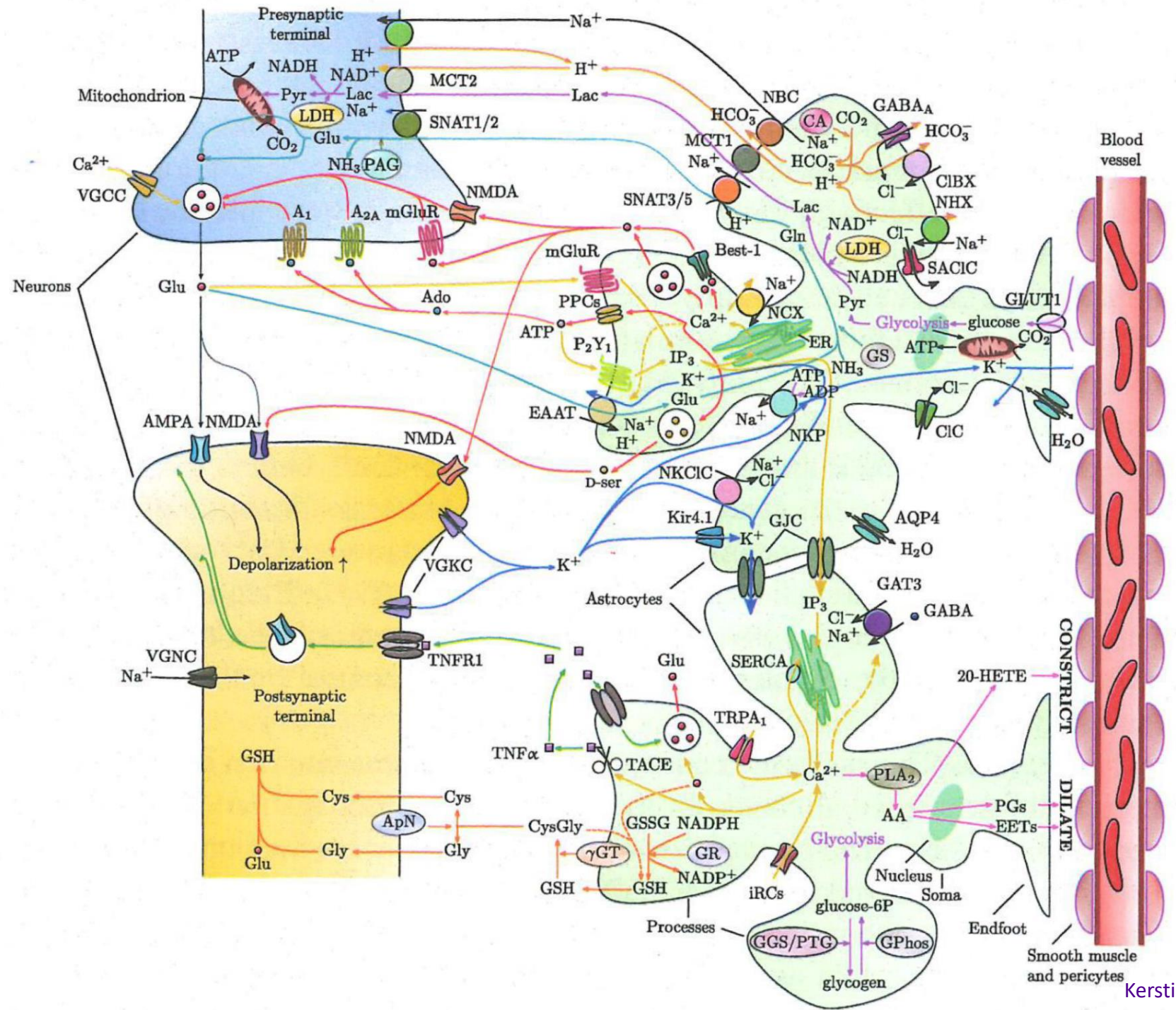
Video:

<https://www.youtube.com/watch?v=y7Yg1mlvLlc>

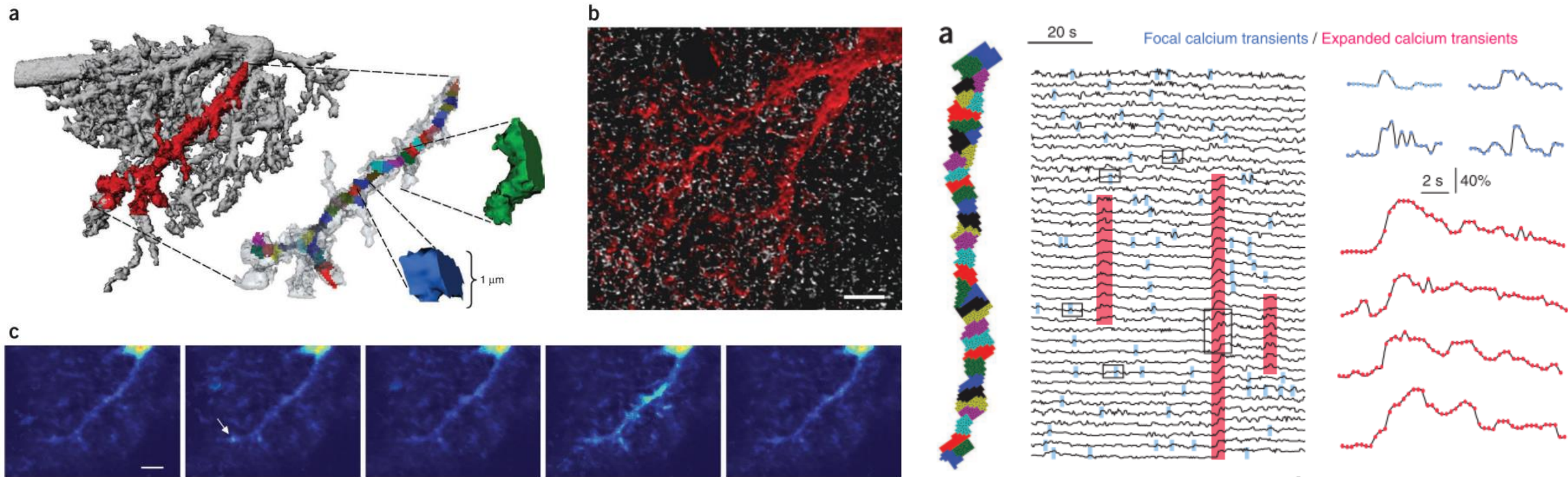
- Neurotransmitters trigger IP₃ release in astrocytes
- IP₃ triggers calcium release from the endoplasmic reticulum
- IP₃ can diffuse through gap junctions; calcium only locally in the astrocytes



Astrocyte communication with neurons and vasculature



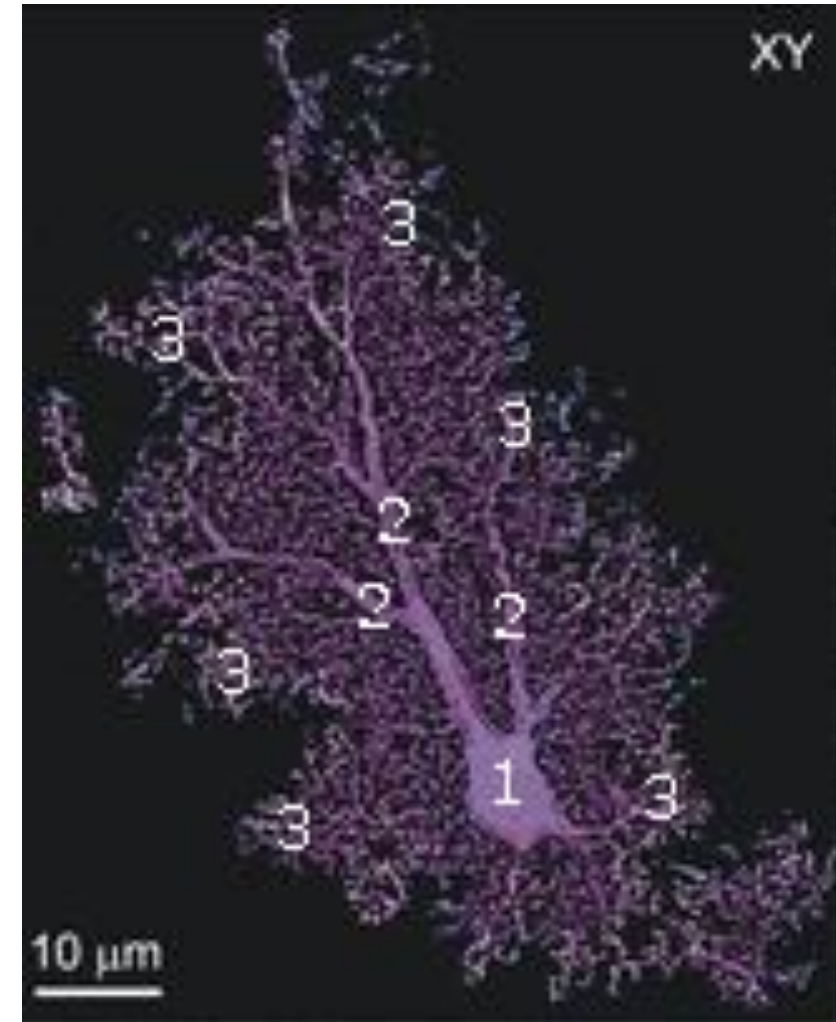
Different calcium signals within one astrocyte?



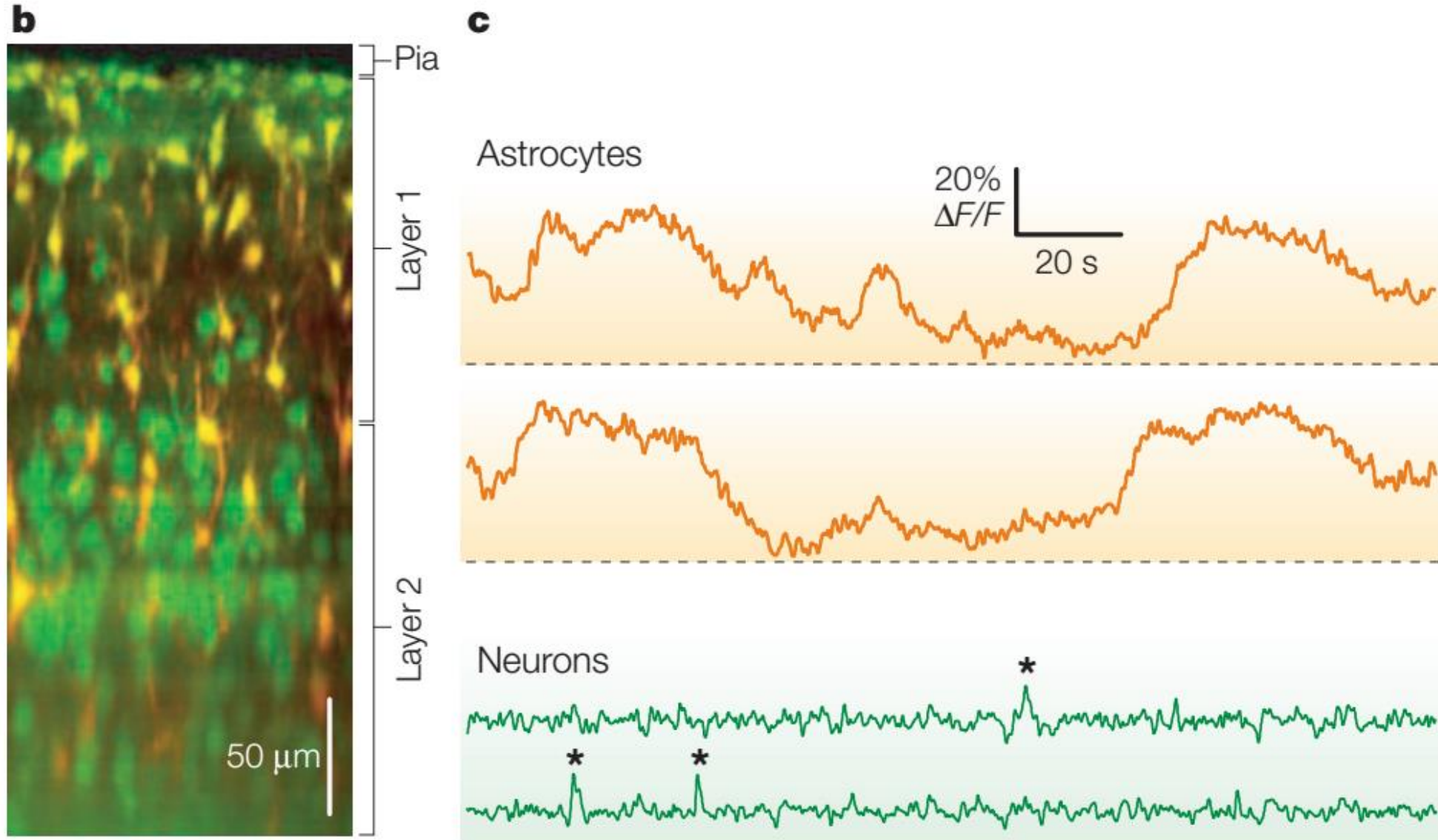
- ✓ Focal Ca^{2+} events depend on spontaneous synaptic release
- ✓ Expanded Ca^{2+} events are mostly the result of an individual action potential fired by an axon

Potentially four levels of calcium dynamics

- 1) the **thinnest processes/branchlets** form an almost nano-scale dense sponge-like network that can be imaged only with electron microscopy or specific Ca^{2+} indicators *in situ*,
- 2) the **main largest (10-20) processes** that are seen in classical microscopy with dyes or immunostaining,
- 3) the **cell body/ soma**, and
- 4) in **cellular networks**



Different time course of astrocytic Ca^{2+} and neuronal potentials



Gliotransmission?

The Journal of Neuroscience, January 3, 2018 • 38(1):3–13 • 3

Dual Perspectives

Dual Perspectives Companion Paper: Gliotransmission: Beyond Black-and-White, by Iaroslav Savtchouk and Andrea Volterra

Multiple Lines of Evidence Indicate That Gliotransmission Does Not Occur under Physiological Conditions

 Todd A. Fiacco¹ and Ken D. McCarthy²

14 • The Journal of Neuroscience, January 3, 2018 • 38(1):14–25

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Gliotransmission: Beyond Black-and-White

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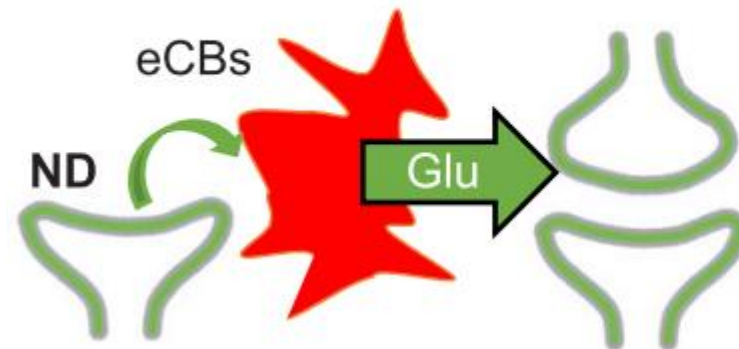
Co-release of gliotransmitters?



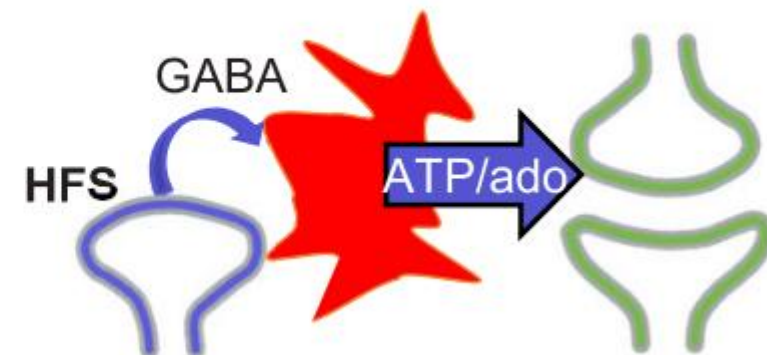
Neuronal activity determines distinct gliotransmitter release from a single astrocyte

Ana Covelo, Alfonso Araque*

eCB synaptic potentiation

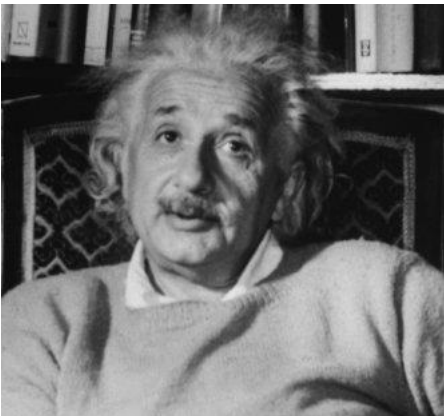
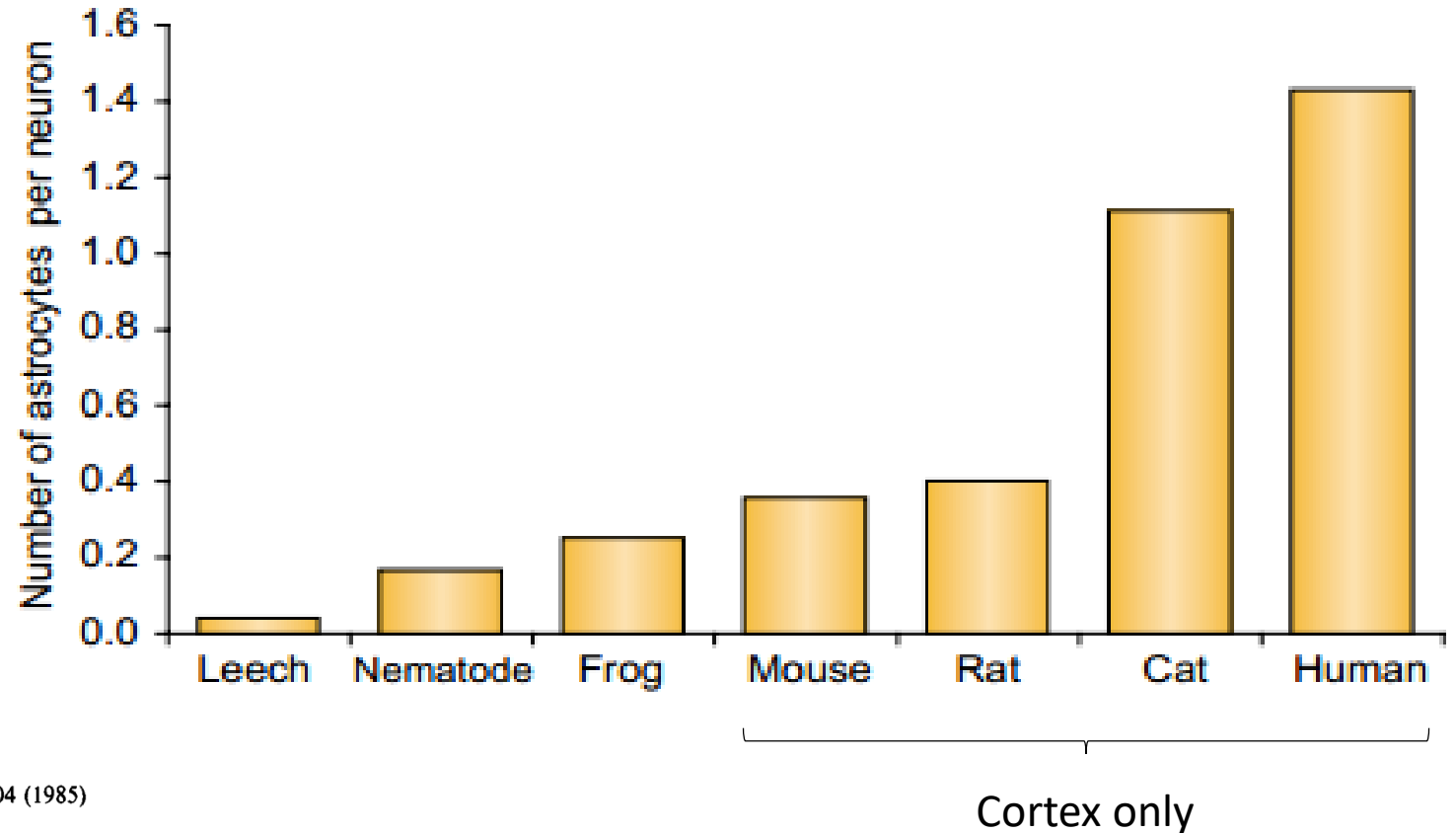


Heterosynaptic depression



Astrocyte numbers across species

- *C. elegans* possesses 302 neurons, but only 56 glial cells (Oikonomou and Shaham 2011), astrocyte/neuron ratio is ~**0.2**.
- **Rat cerebral cortex** contains a mean astrocyte/neuron ratio of **0.4** (Bass et al. 1971).
- The **whole human adult brain** has a **one-to-one ratio** (Azevedo et al. 2009).
- **Human cerebral cortex** has a **ratio of 1.4** (Friede 1954; Pelvig et al. 2008).



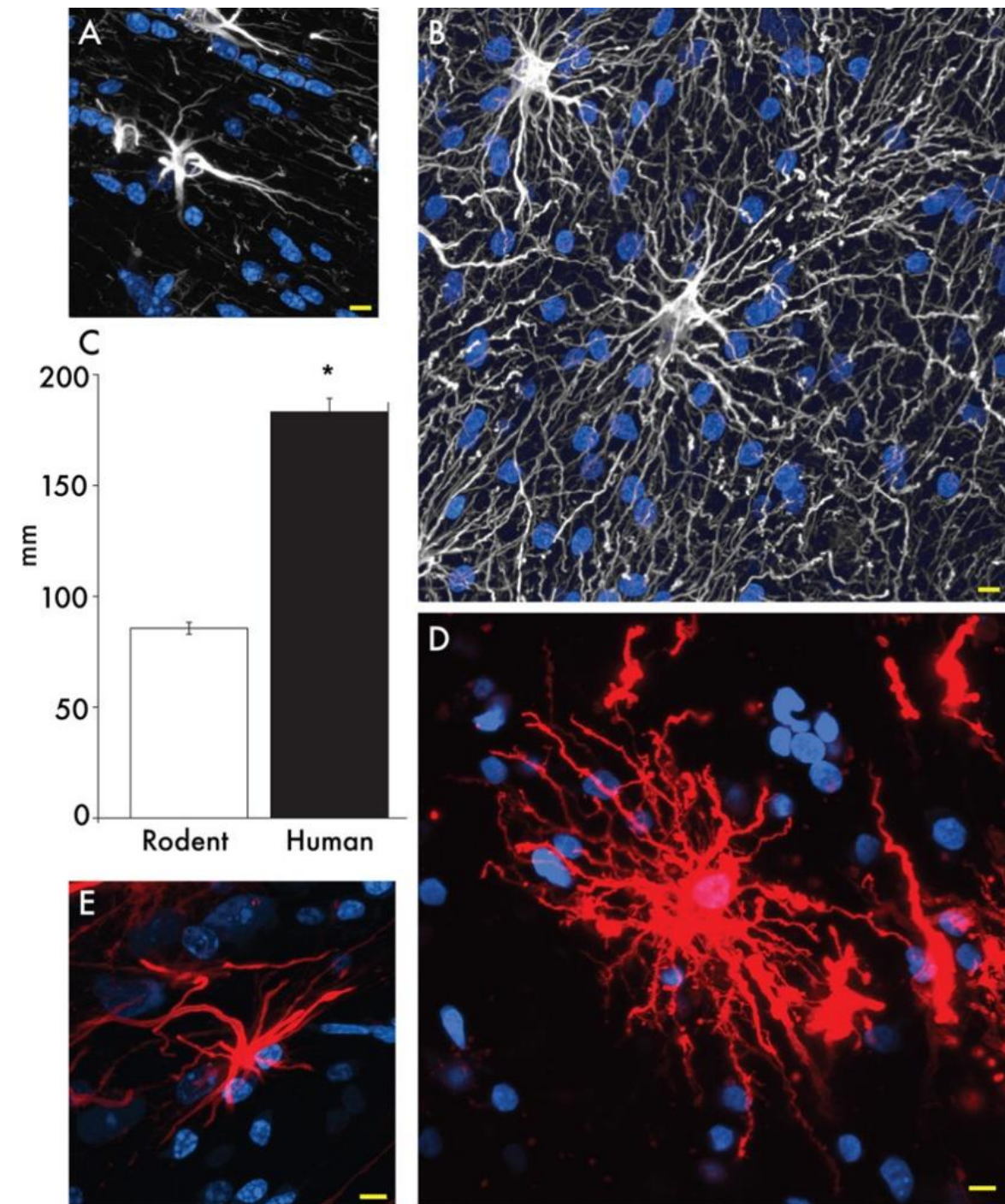
EXPERIMENTAL NEUROLOGY **88**, 198–204 (1985)

On the Brain of a Scientist: Albert Einstein

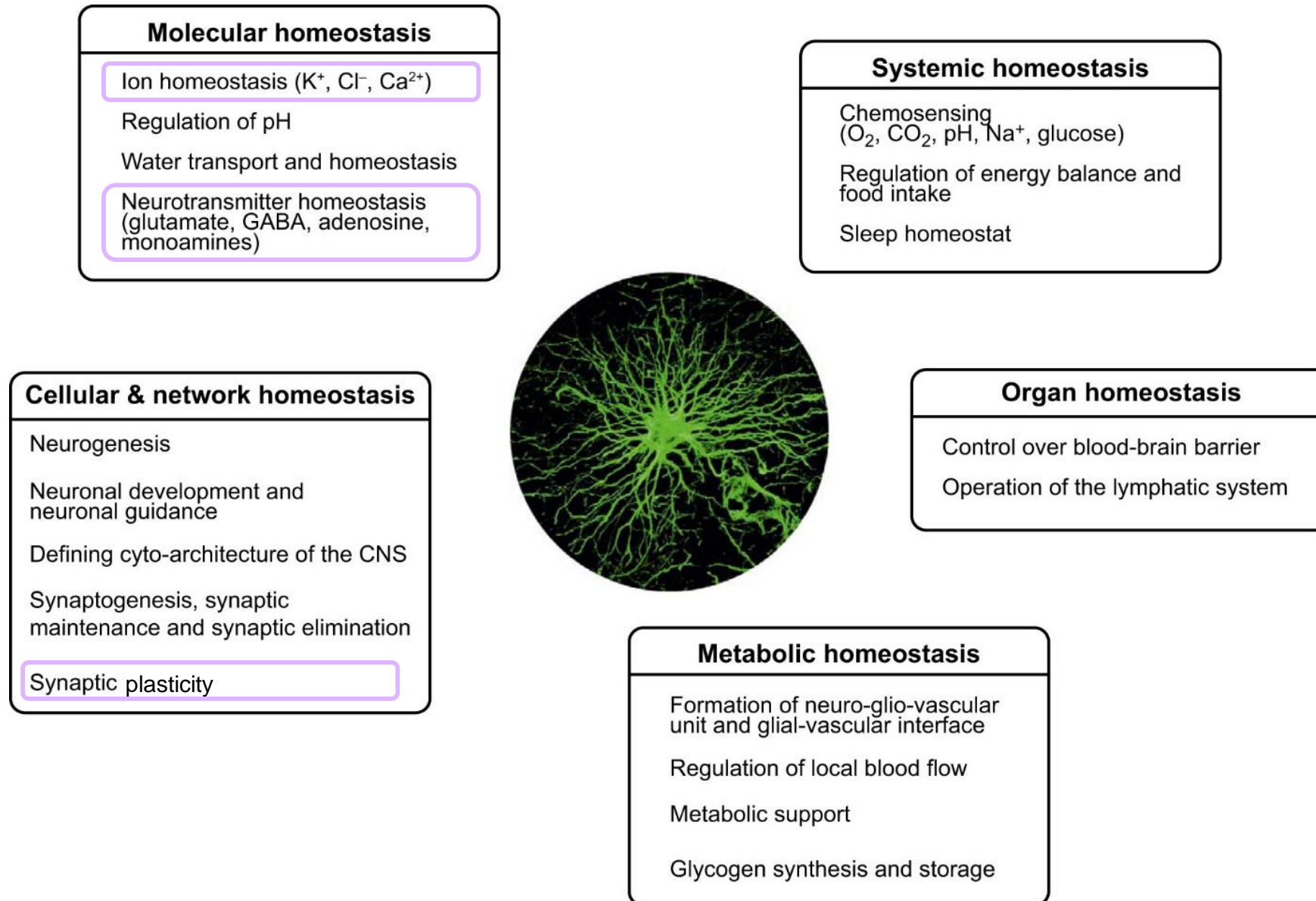
MARIAN C. DIAMOND,* ARNOLD B. SCHEIBEL,†
GREER M. MURPHY, JR.,‡ AND THOMAS HARVEY¹

Human vs. mouse astrocytes

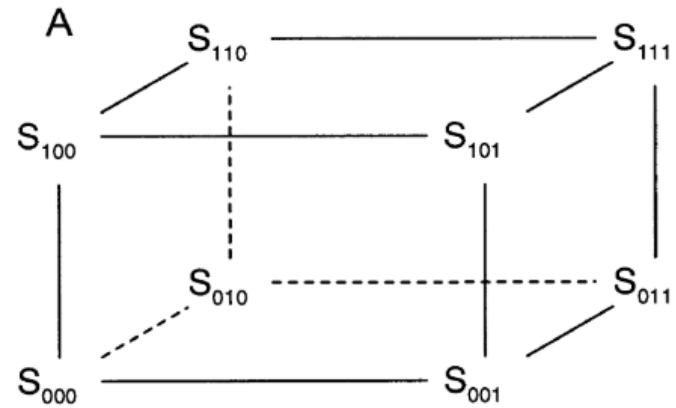
- A) Mouse fibrous astrocyte in white matter. GFAP; white, sytox; blue. SB=10 μ m.
- B) Human fibrous astrocytes in white matter. SB=10 μ m.
- C) Human fibrous astrocytes are approximately 2.14 fold larger in diameter than the rodent counterpart. * $p < 0.0001$; t-test.
- D) Human fibrous astrocyte labeled with Dil revealing the full structure of the cell. Dil; red, Sytox; blue. SB=10 μ m.
- E) Mouse fibrous astrocyte labeled with Dil. SB=10 μ m.



Homeostatic functions of astrocytes



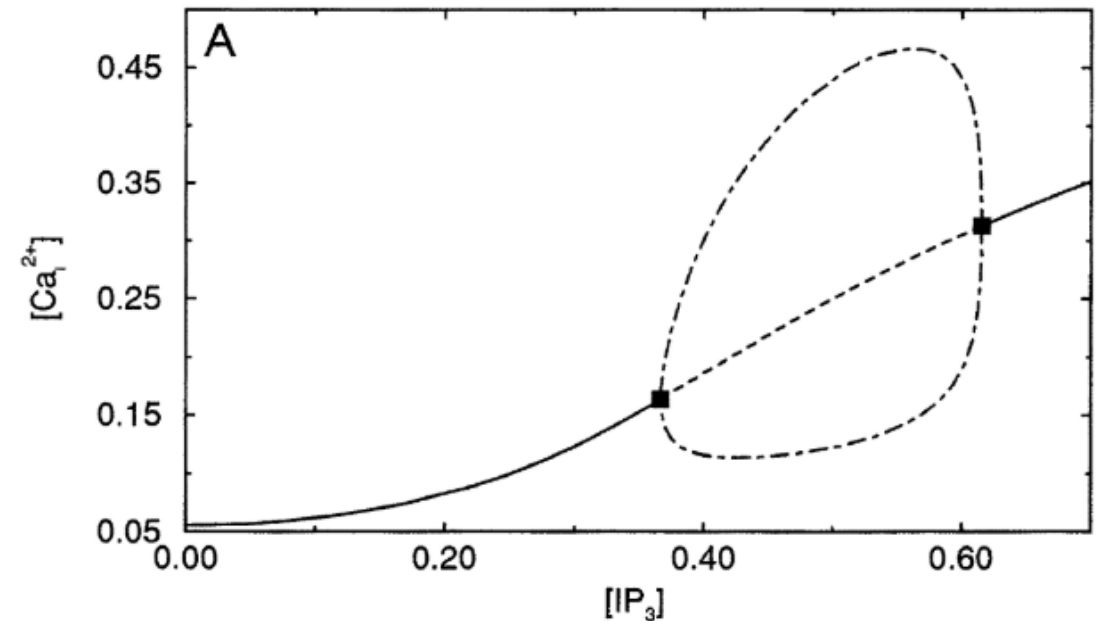
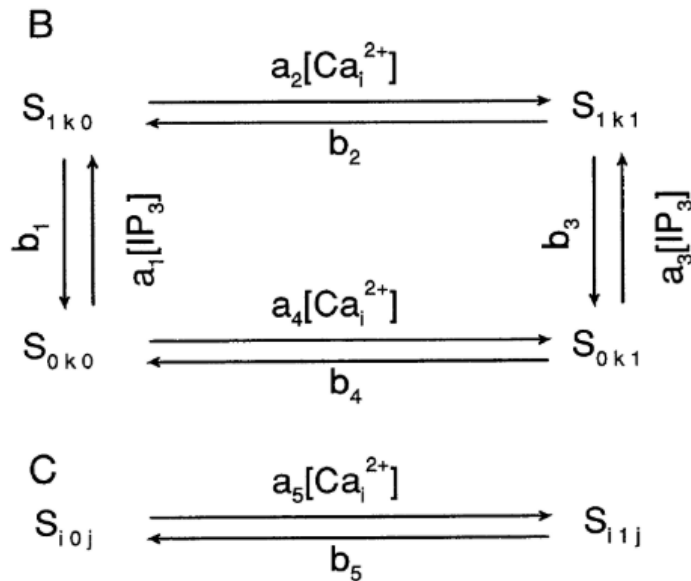
De Young and Keizer model (1992)



State_{xyz} = S_{xyz}
 x = activating IP₃ binding site
 y = activating Ca²⁺ binding site
 z = inactivating Ca²⁺ binding site
 0 = unoccupied binding site
 1 = occupied binding site

**Channel is open
when 3 subunits are open:**

$$\rho = \frac{N_{\text{Open}}}{N_{\text{Total}}} = (x_{110})^3$$



Li and Rinzel model (1994)

$$\frac{dC}{dT} = -V_1 m_\infty^3 h^3 (C - C_0)$$

Hodkin-Huxley like equations to describe IP_3 induced Ca^{2+} release

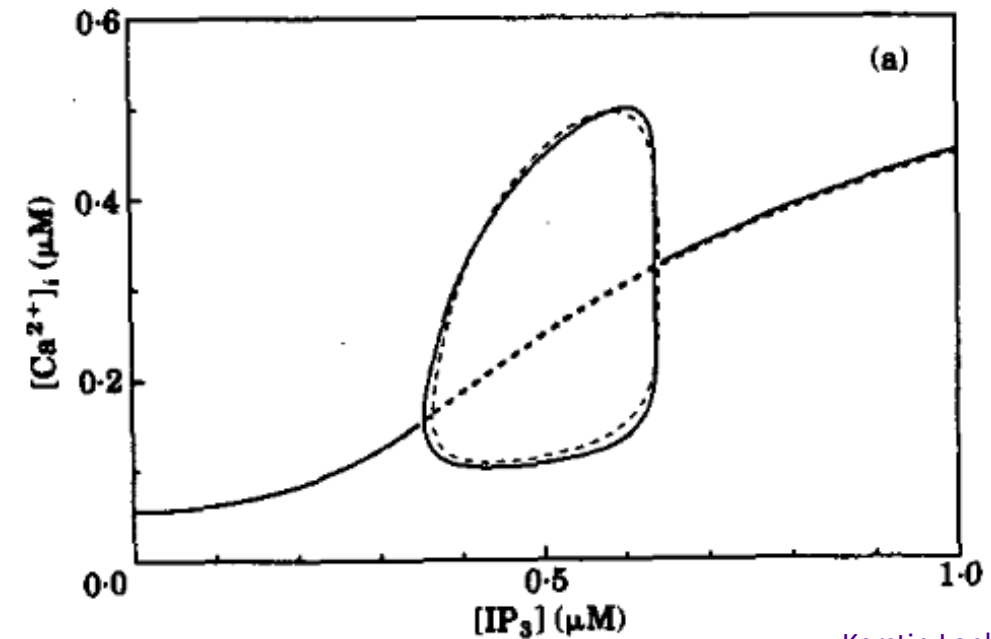
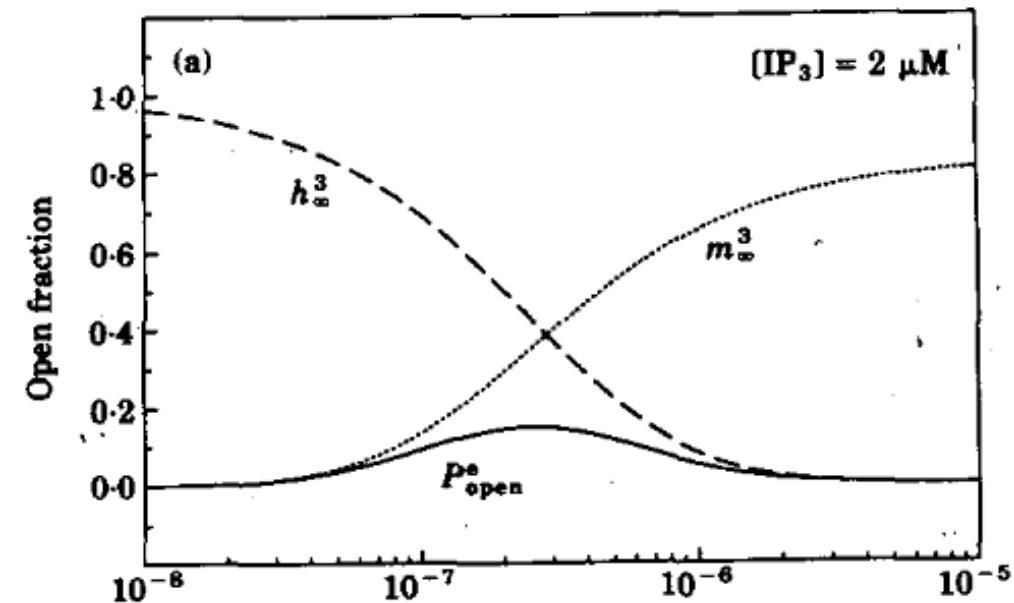
$$-V_2(C - C_0) - \frac{V_3 C^2}{1 + C^2}$$

$$\frac{dh}{dT} = \frac{h_\infty - h}{\tau_h}$$

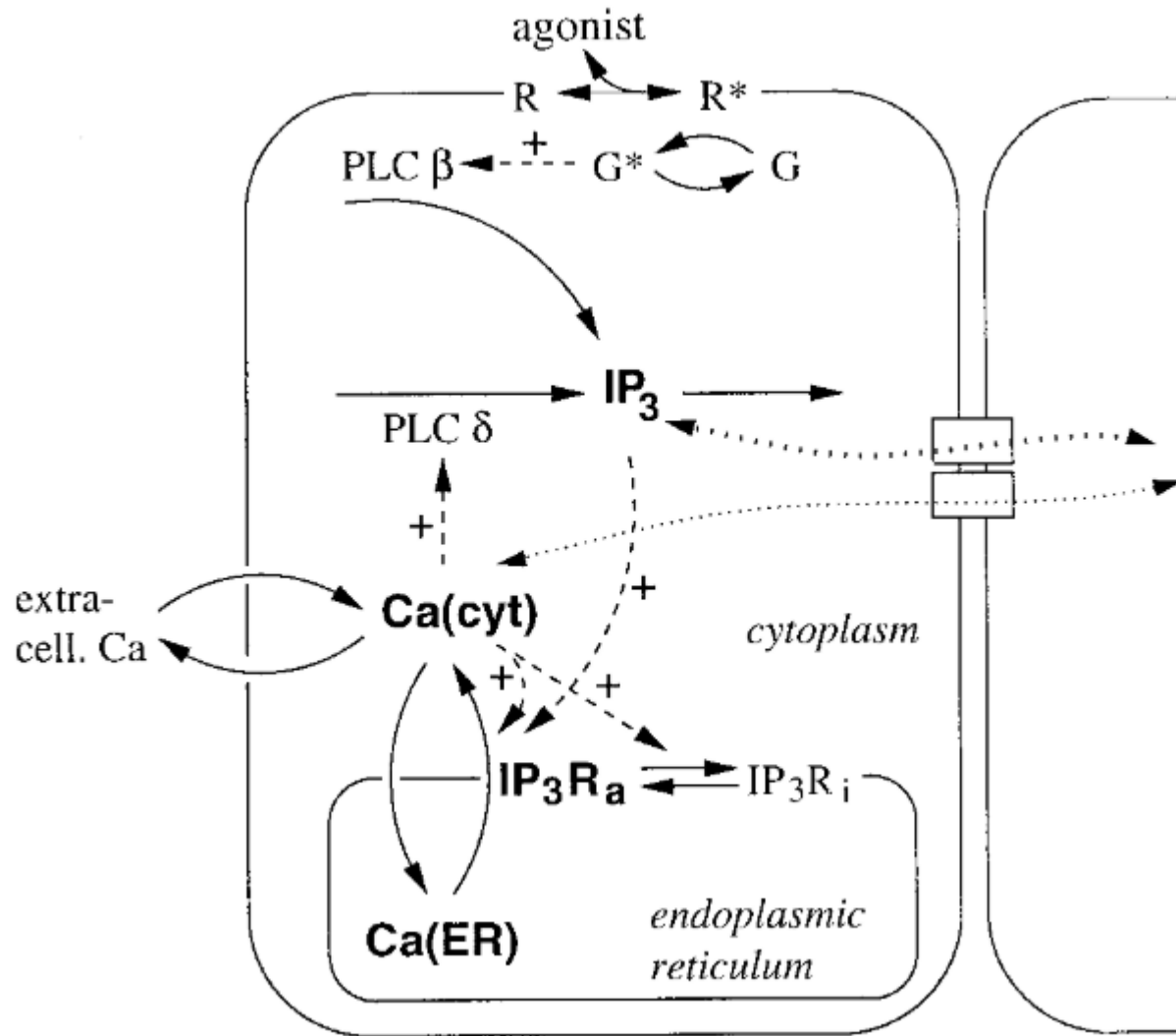
Slow, time dependent inactivation

$$m_\infty = \left(\frac{[\text{IP}_3]}{[\text{IP}_3] + d_1} \right) \left(\frac{[\text{Ca}]}{[\text{Ca}] + d_5} \right)$$

Fast, time independent activation by Ca^{2+} and IP_3

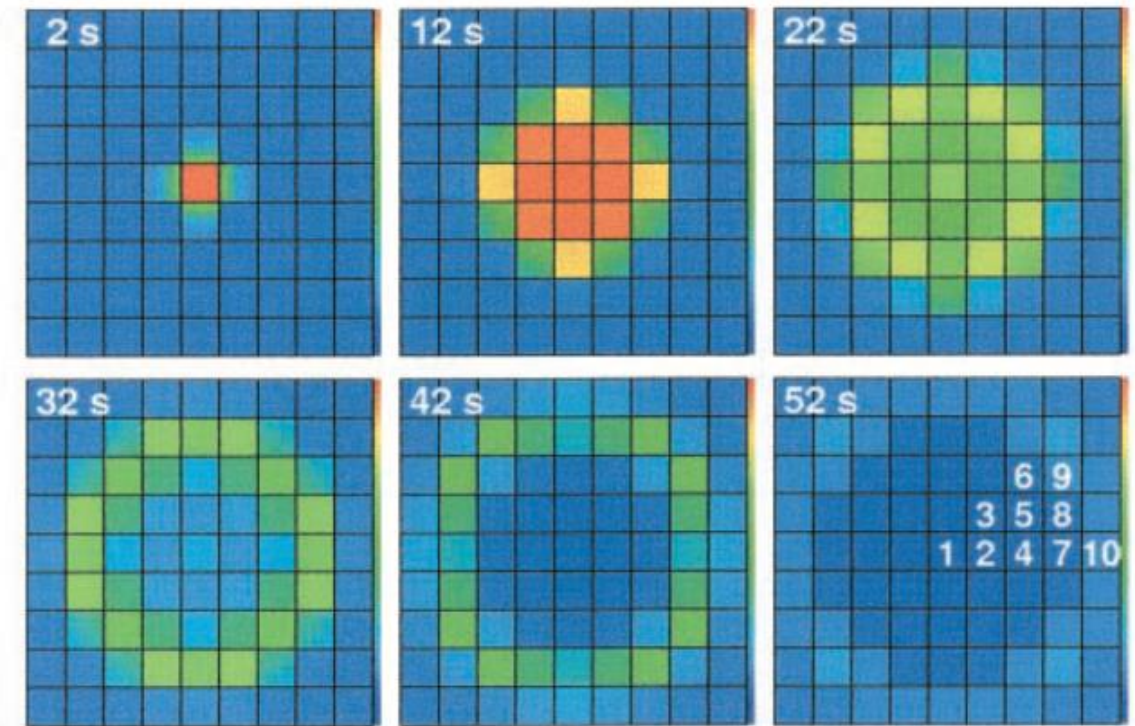


Höfer et al. model (2002)

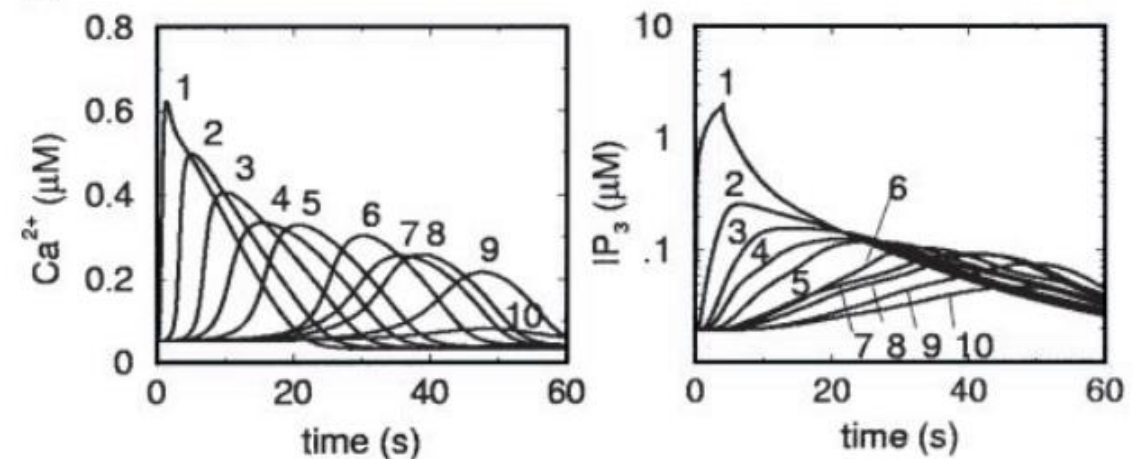


System of balance equations for the four variables: cytoplasmic Ca^{2+} concentration (C), ER store Ca^{2+} concentration (S), IP_3 concentration (I), and active fraction of IP_3R (R).

A



B





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Review

From in silico astrocyte cell models to neuron-astrocyte network models: A review



Franziska Oschmann^{a,b}, Hugues Berry^{c,d}, Klaus Obermayer^{a,b}, Kerstin Lenk^{e,*}

35 models investigated:

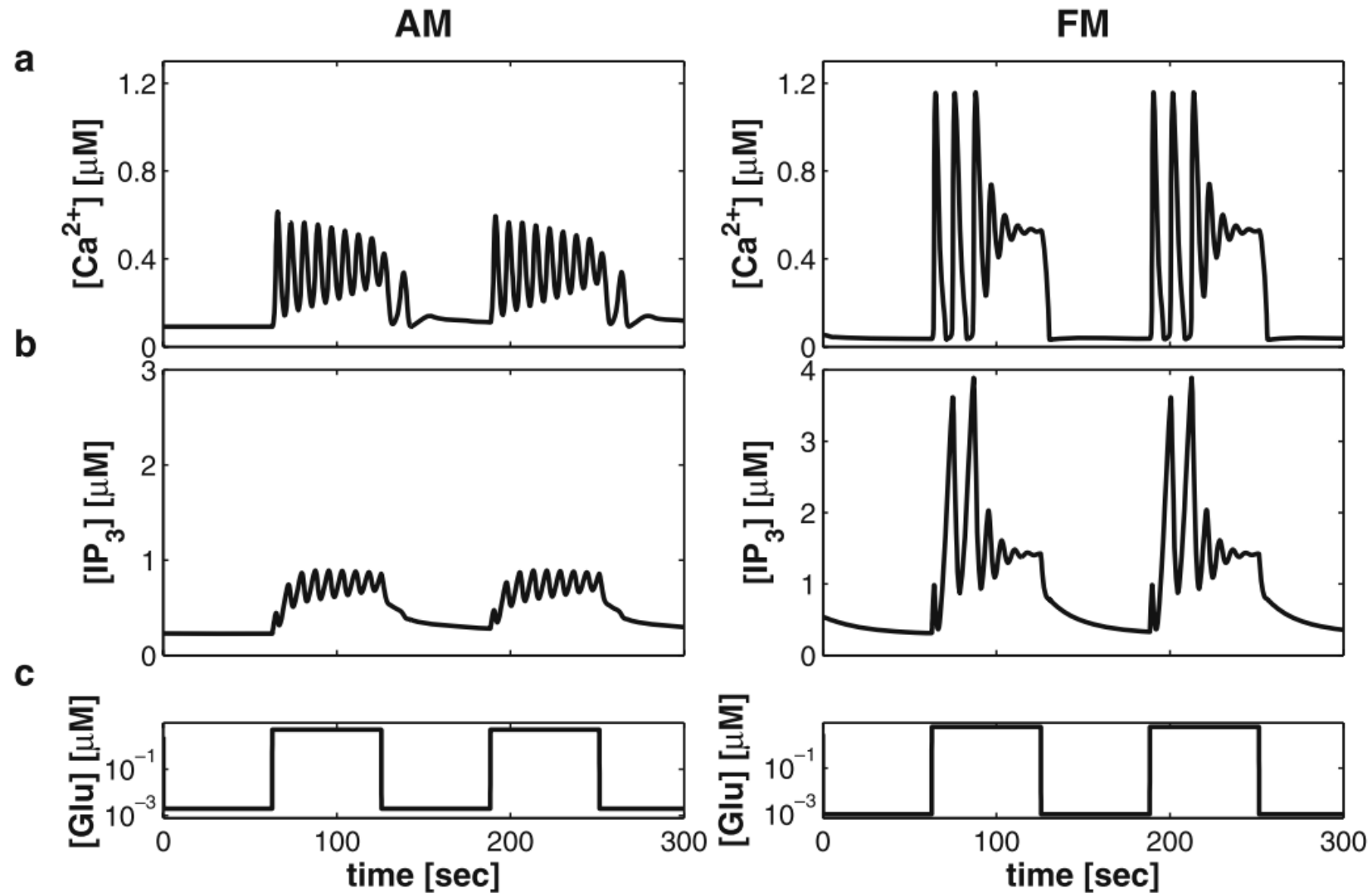
1. Single astrocytic cell models
2. Tripartite synapse models
3. Astrocyte network models
4. Neuron-astrocyte network models

a

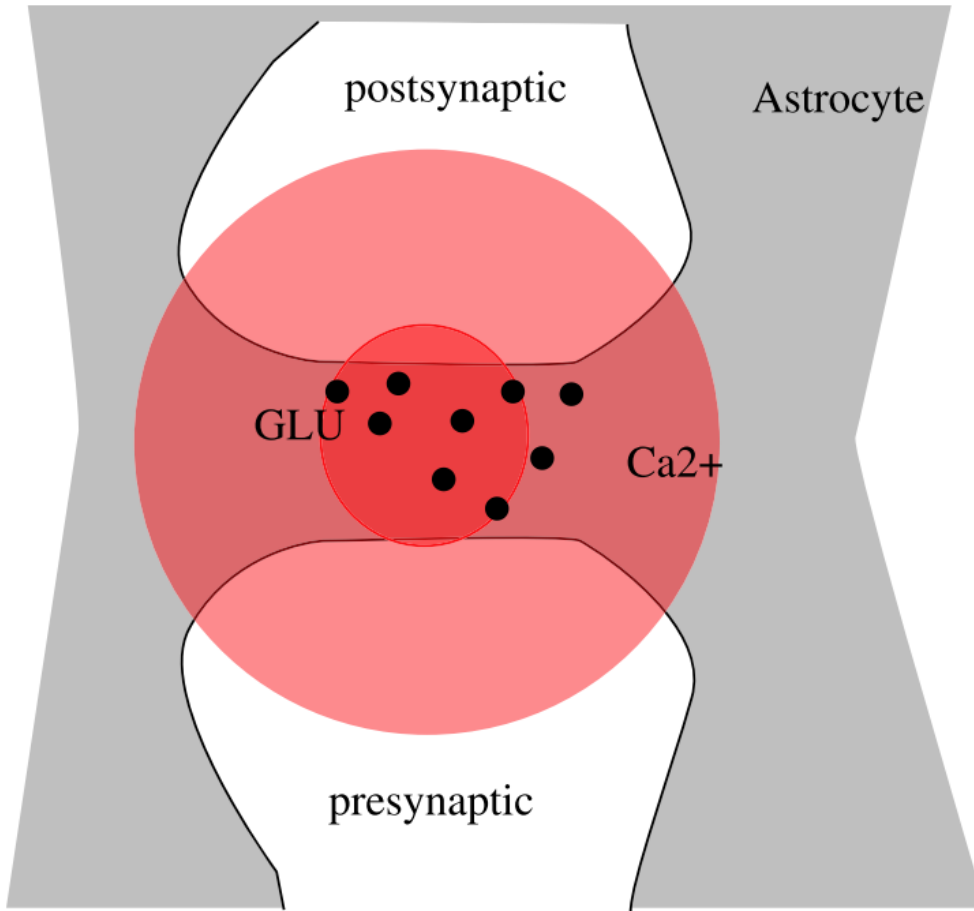


- Kerstin Lenk

Single astrocytic cell model by De Pittà et al., 2009

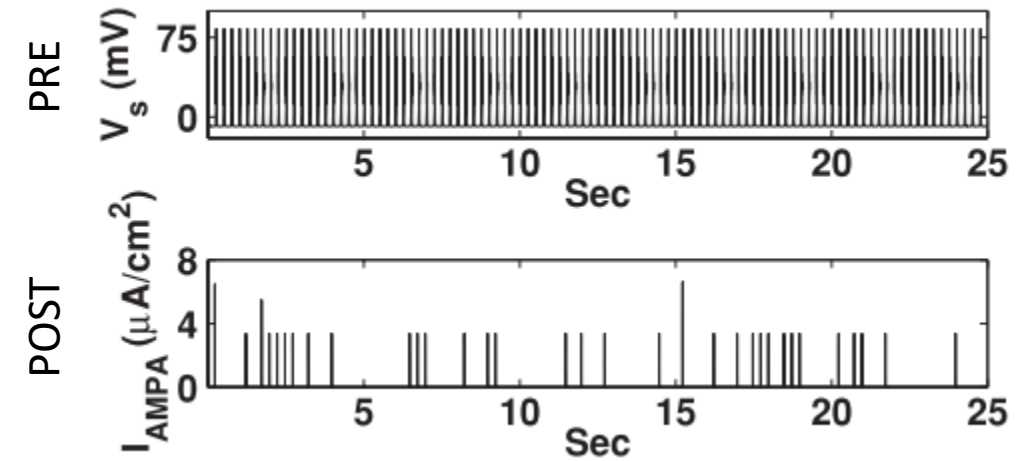


Tripartite synapse model by Nadkarni and Jung, 2007

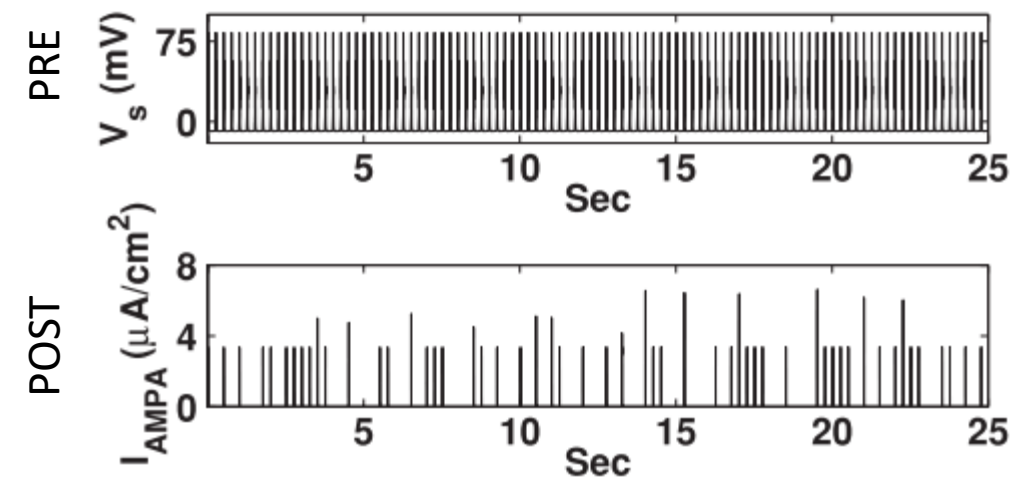


De Young & Keizer and Li and Rinzel -type model
Neuron-astrocyte interaction

Without astrocyte:

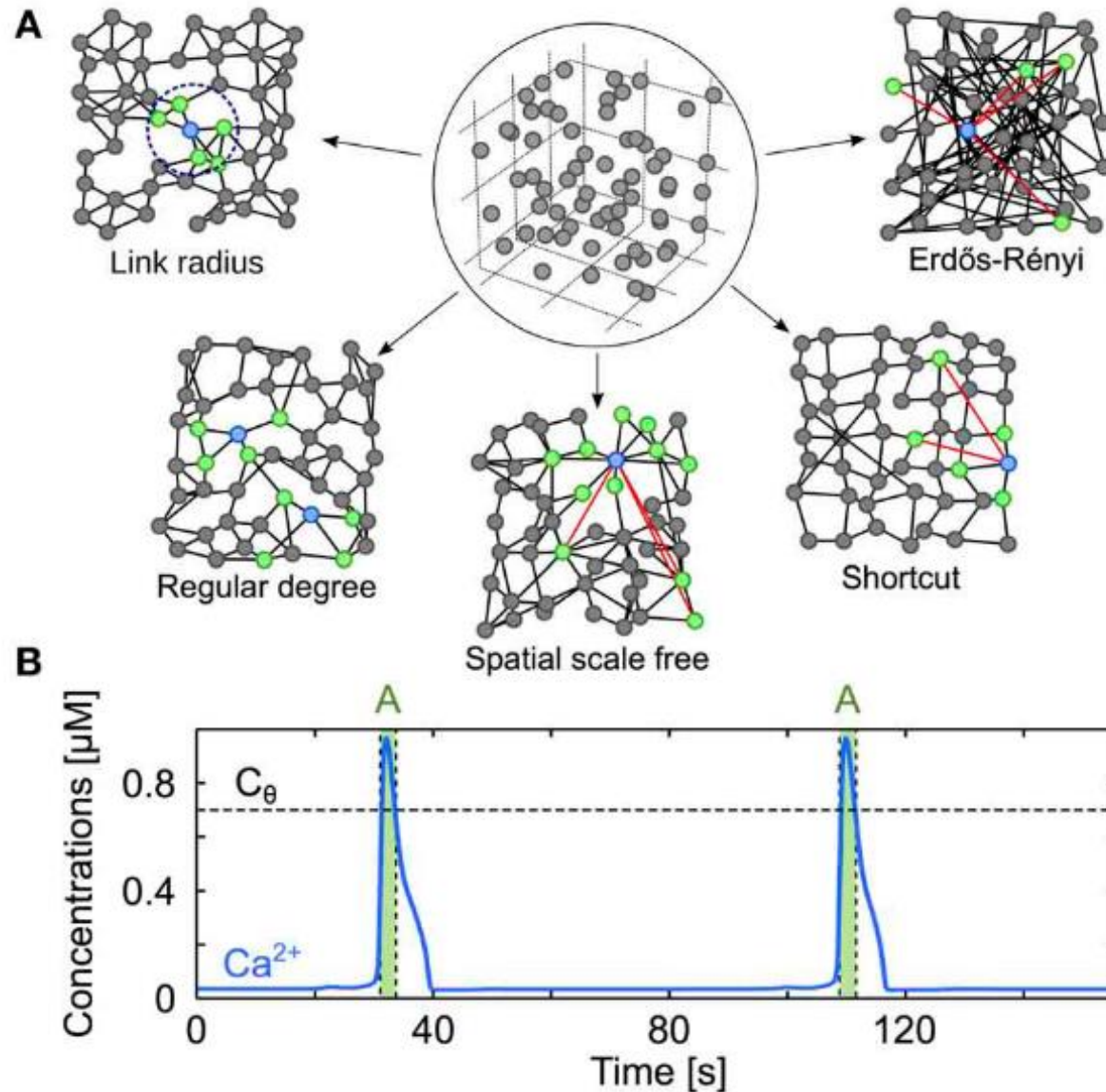


With astrocyte:

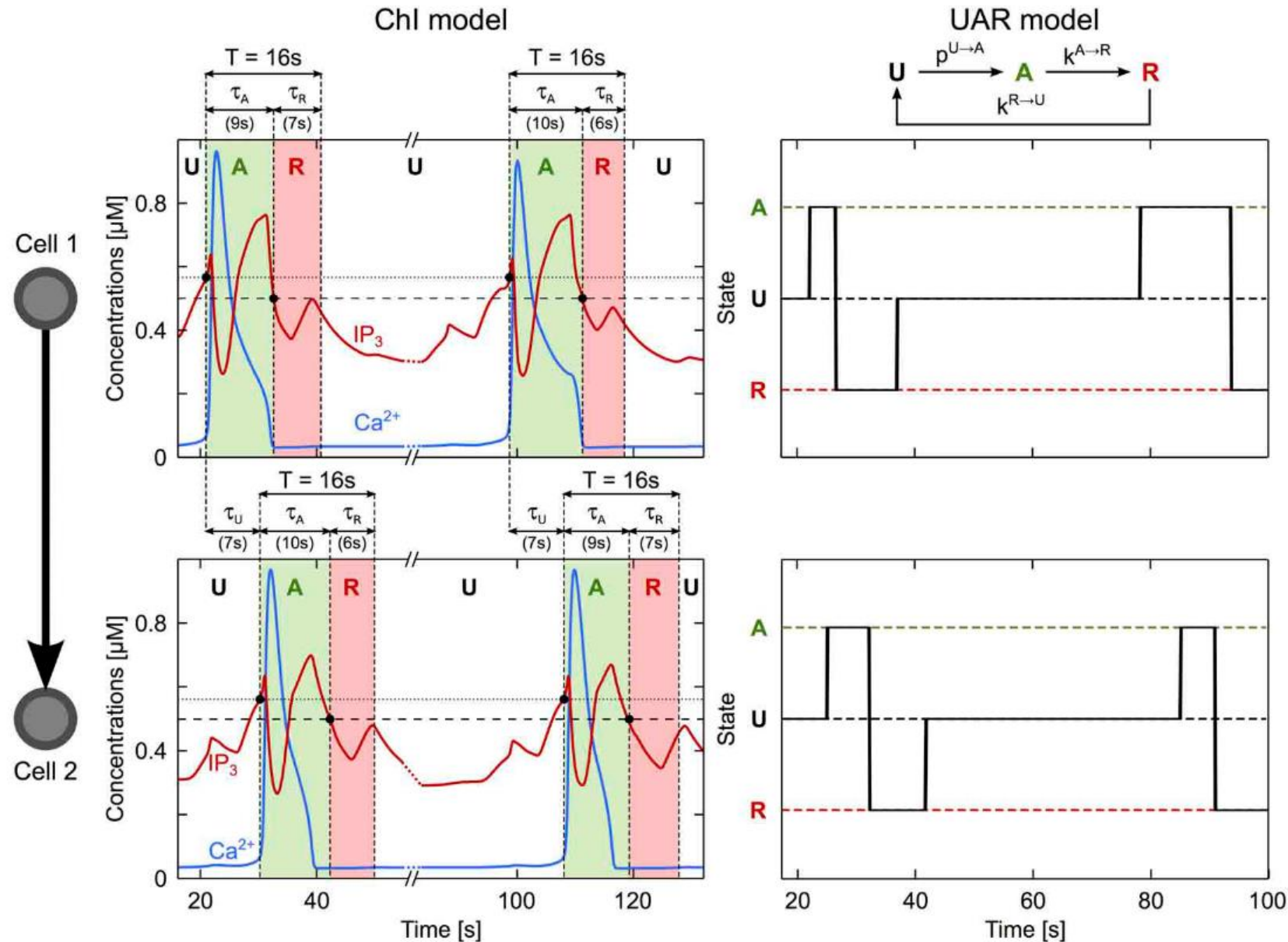


Astrocyte network model by Lallouette et al., 2014

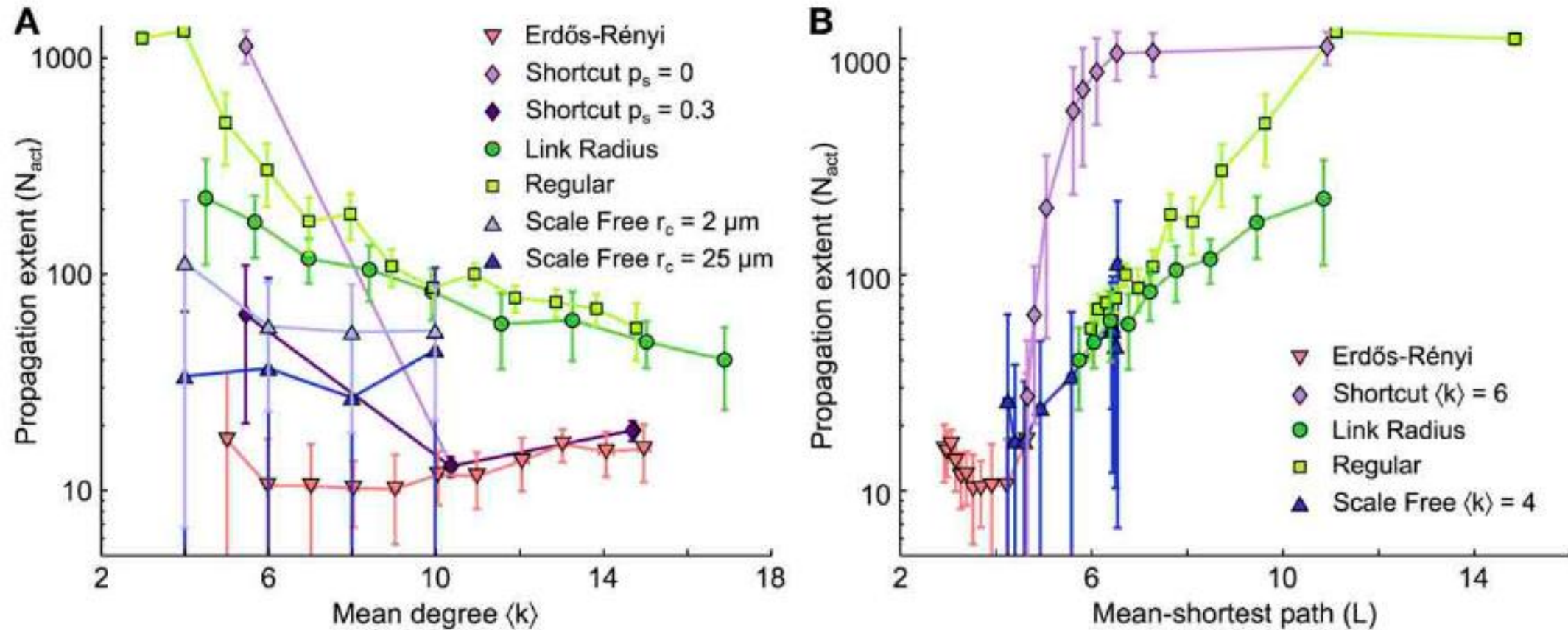
Based on De Pittà et al., 2009 and 2012



Astrocyte network model by Lallouette et al., 2014



Astrocyte network model by Lallouette et al., 2014



Neuron-astrocyte network model



A computational model of interactions between neuron and astrocyte networks: role of astrocytes on stability of the neuronal firing rate

**Kerstin Lenk^{1,†,*}, Eero Satuvuori^{1,2,3,4,†}, Jules Lallouette^{5,6}, Antonio Ladrón-de-Guevara¹,
Hugues Berry^{5,6}, Jari AK Hyttinen¹**

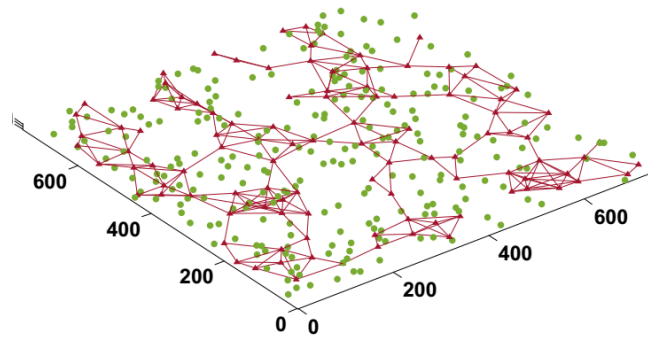
(submitted)

Motivation

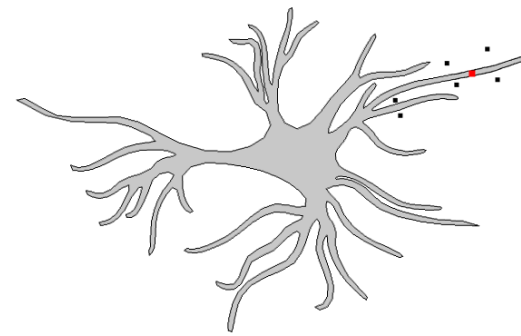
- Astrocytes may influence neuronal network function → What are the mechanism/ pathways? How do astrocytes change the neuronal activity and vice versa?
- How are the astrocytic calcium dynamics influenced by morphology and topology?
- Role and functions of astrocytes in epilepsy and Alzheimer's?



Neuron-astrocyte network model



Single cell astrocyte model



Our modeling approach

Experiments

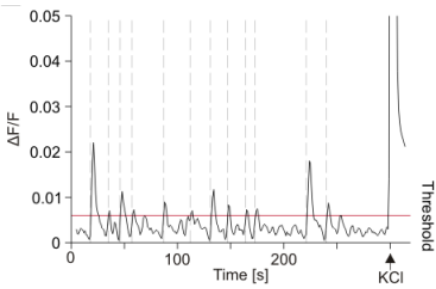
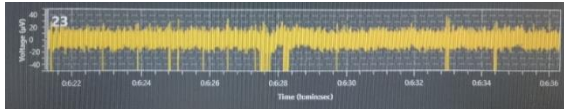
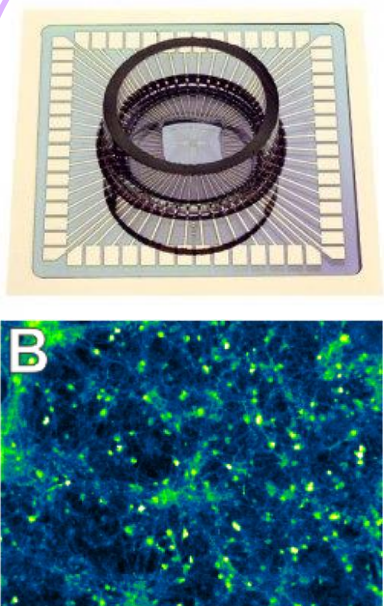


Table 1. Initial values of the ion concentrations, the membrane voltage, IP₃ and the fraction of the activated IP₃ receptor channels. For the calculation of [Ca²⁺]_{ER}, [IP₃]_i and h see Model section Model parameter values.

Parameter	Value	Source
[Ca ²⁺] _i	0.073 μM	[23]
[Ca ²⁺] _{ER}	25 μM	see text
[Ca ²⁺] _o	1800 μM	[18]
[Na ⁺] _i	15 mM	[19]
[Na ⁺] _o	145 mM	[19]
[K ⁺] _i	100 mM	[19]
[K ⁺] _o	3 mM	[19]
V	-85 mV	[24]
[IP ₃] _i	0.15659 μM	see text
h	0.7892	see text

Computational models

$$\frac{d[Ca^{2+}]_i}{dt} = \frac{A}{F \cdot Vol} \cdot I_{NCX} + \frac{A \cdot \sqrt{ratio_{ER}}}{F \cdot Vol} \cdot (I_{IP_3R} - I_{SERCA} + I_{CaLeak}),$$

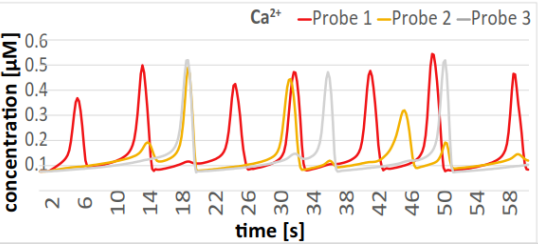
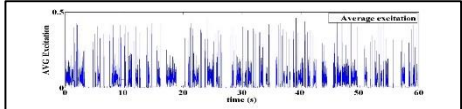
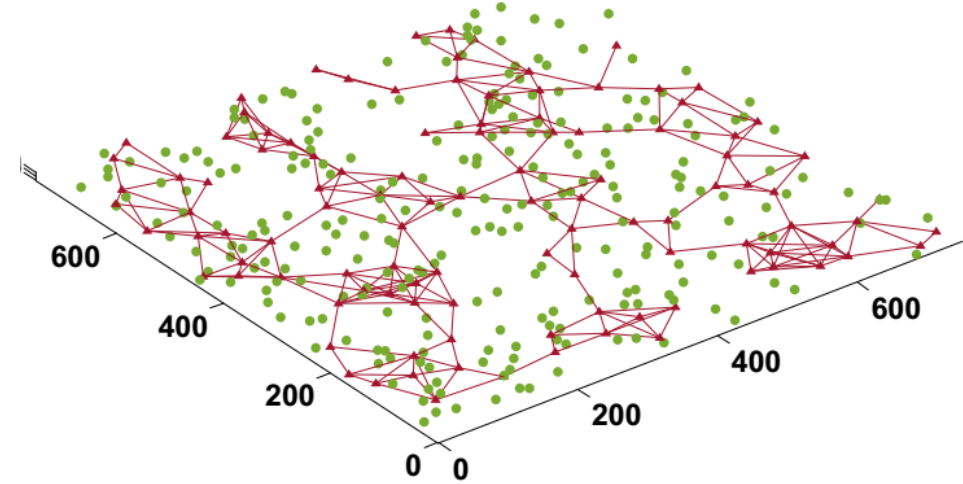
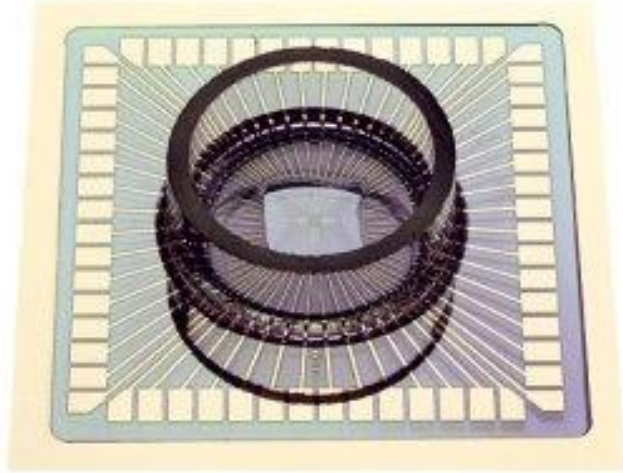


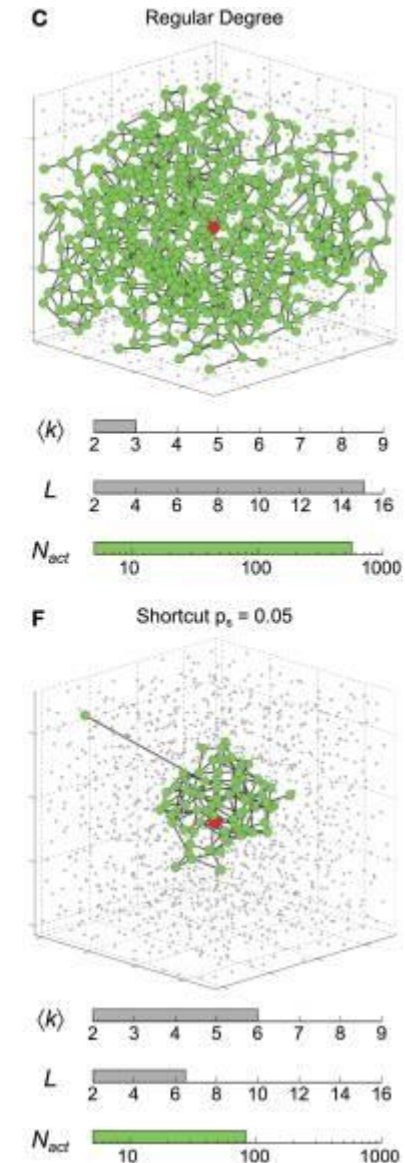
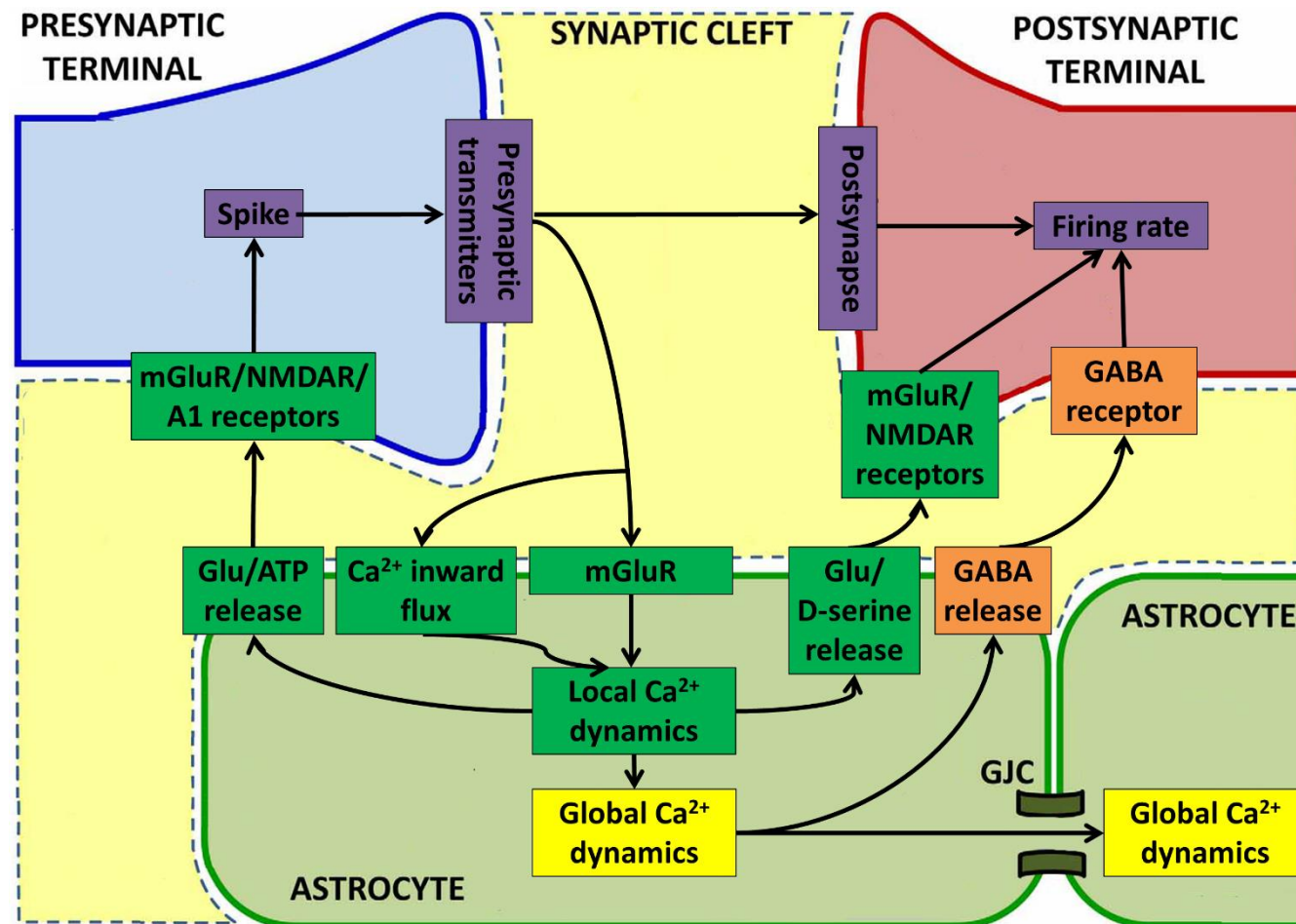
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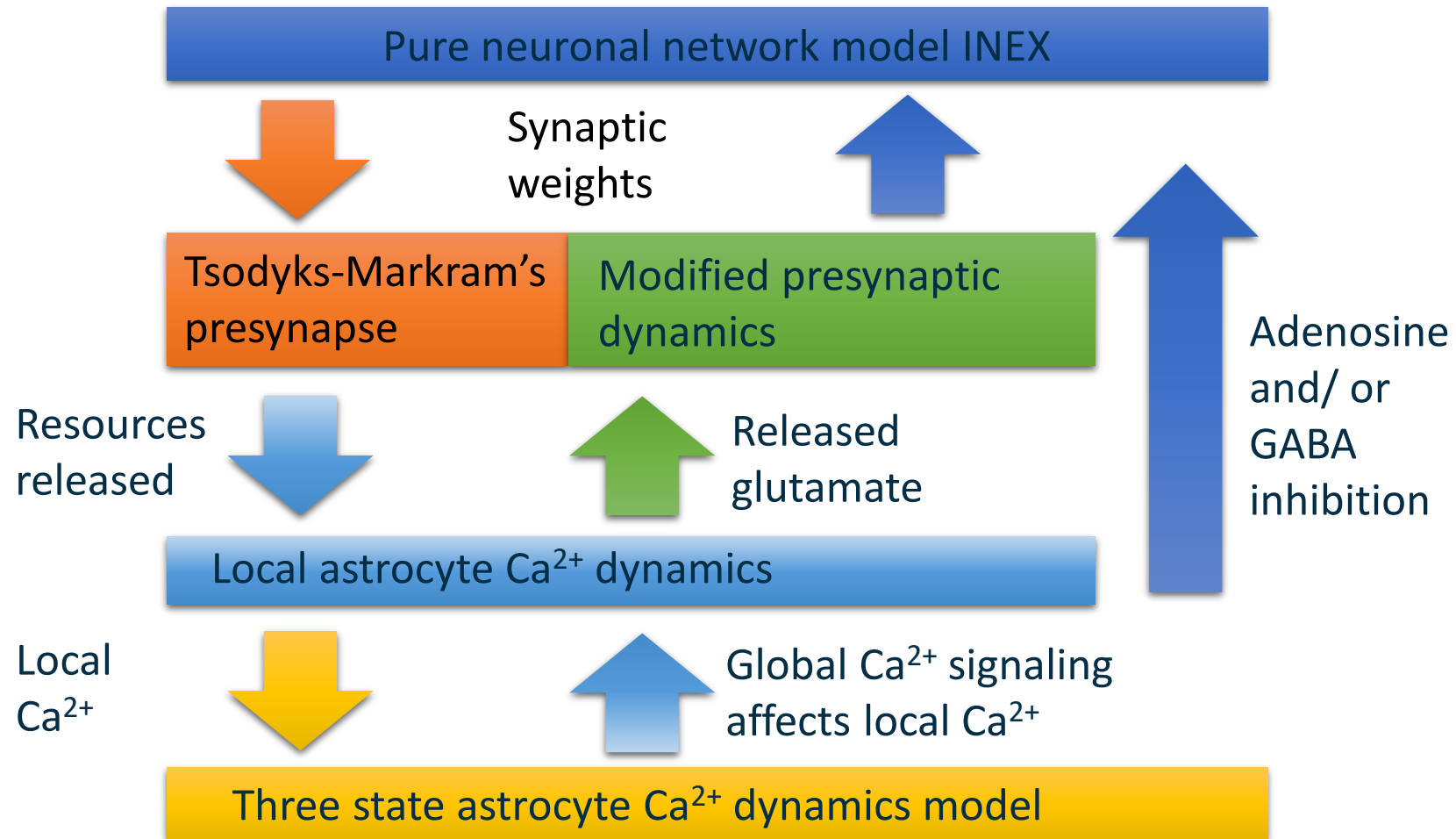
Neuron-astrocyte network model



Model with presynaptic and astrocytic calcium dynamics



Neuron-astrocyte network model INEXA



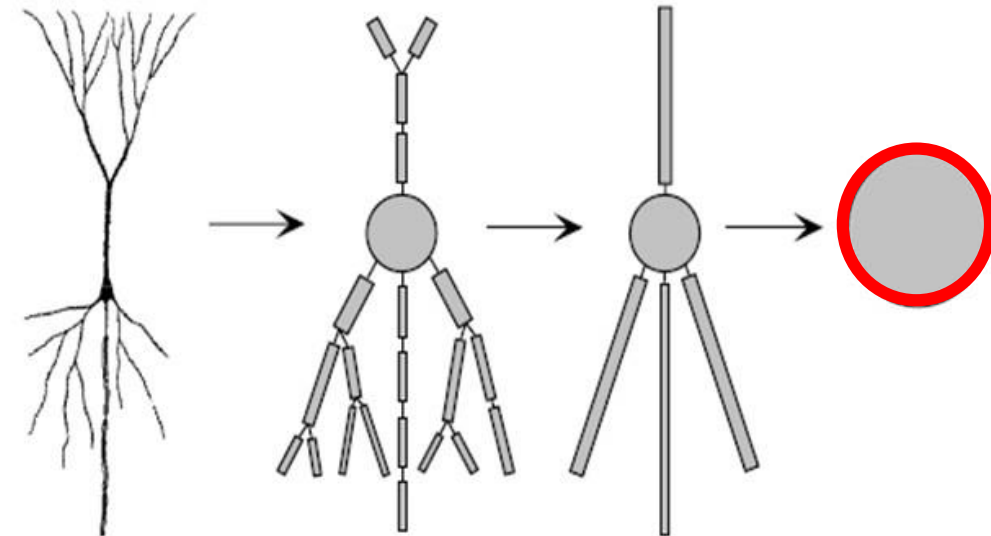
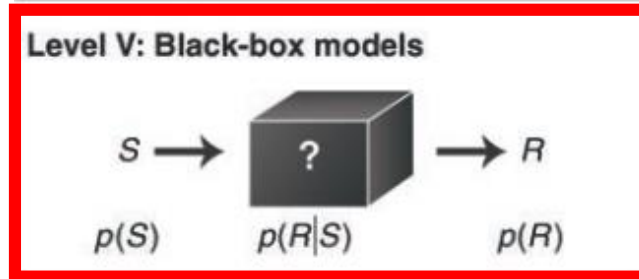
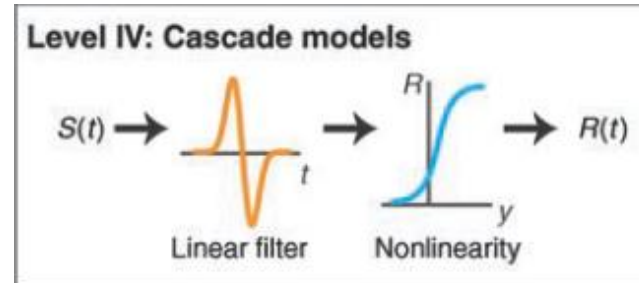
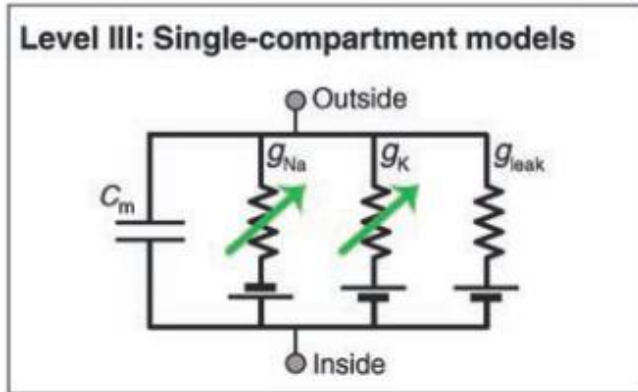
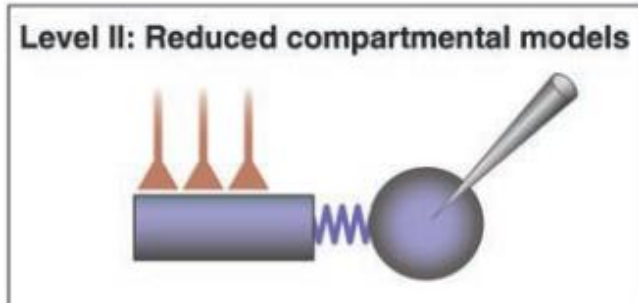
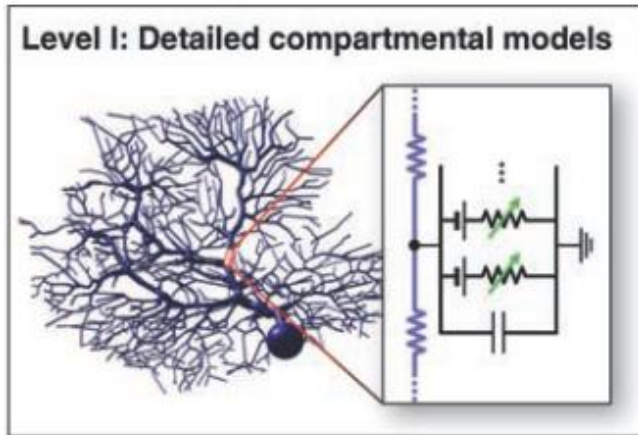
Lenk, 2011

De Pittà et al., PLoS Comput. Biol. 2011

De Pittà et al., Frontiers in Comput. Neurosci. 2012

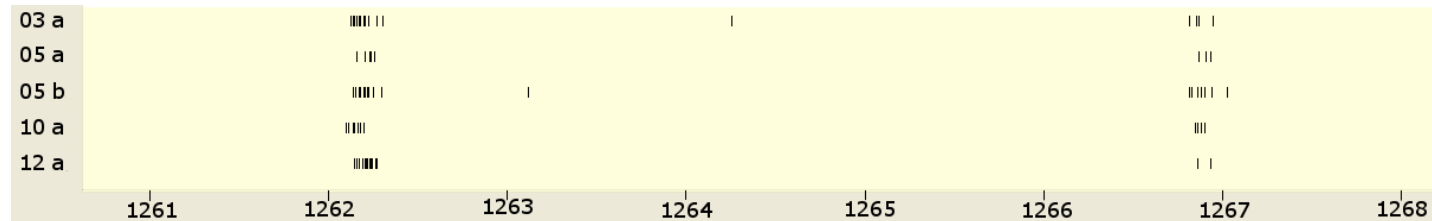
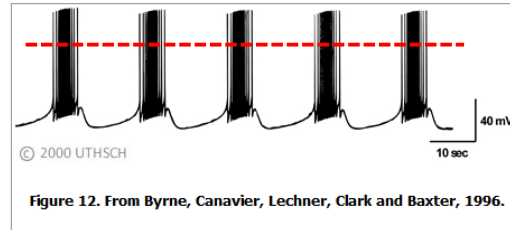
Lallouette et al., Front. Comput. Neurosci. 2014

We start from the neuronal network



Relevant model characteristics

Target: Neuronal model for simulating neuronal activity as observed in *in vitro* experiments with MEAs



Following characteristics:

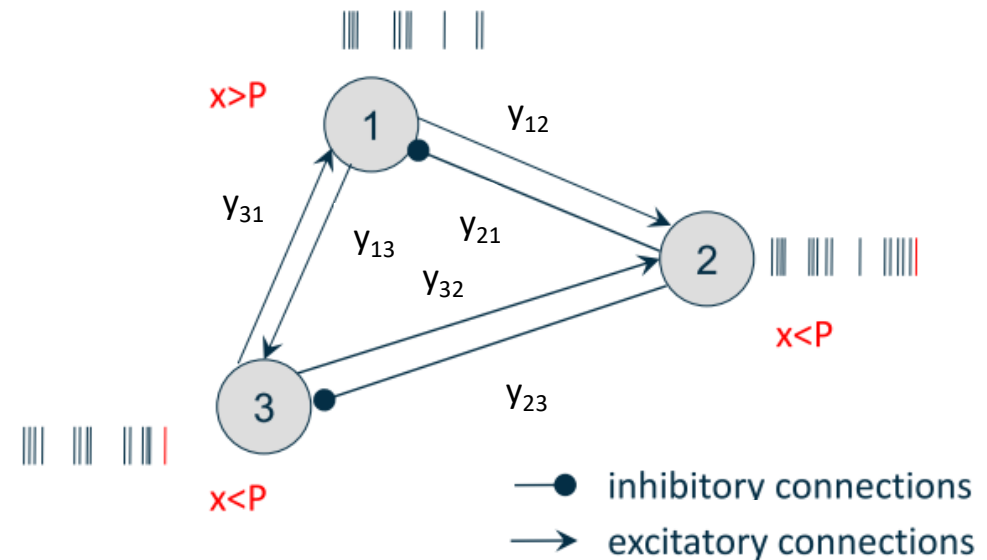
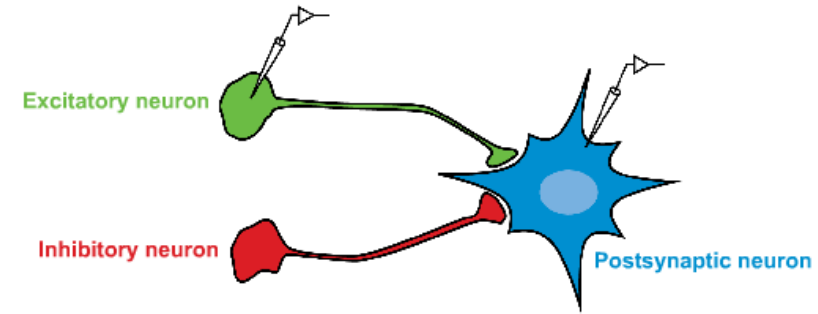
- Simulation of a whole neuronal network
- Bursts
- Spontaneous activity
- Noise
- Simple model with a few parameters

INEX model consists of Poisson neurons

- Phenomenological model
- Cellular automaton
- Firing rate:

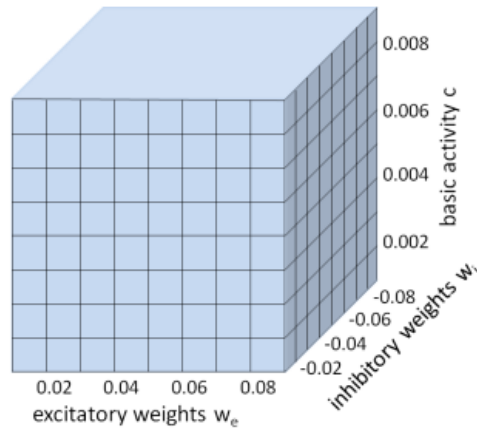
$$\lambda_i(t_k) = c_i + \sum_j y_{ji} s_j(t_{k-1})$$
- Inhomogeneous Poisson processes:

$$P_i\{1 \text{ spike within } \Delta t\} = e^{-\lambda_i \Delta t} \cdot \lambda_i \Delta t$$
- Spike Time History
- Parameters obtained by brute force approach with the goal functions spike and burst rate
- Each neuron makes connection to e.g. 10-30% of the population



INEX model consists of Poisson neurons

Brute Force Approach for Parameter Search:



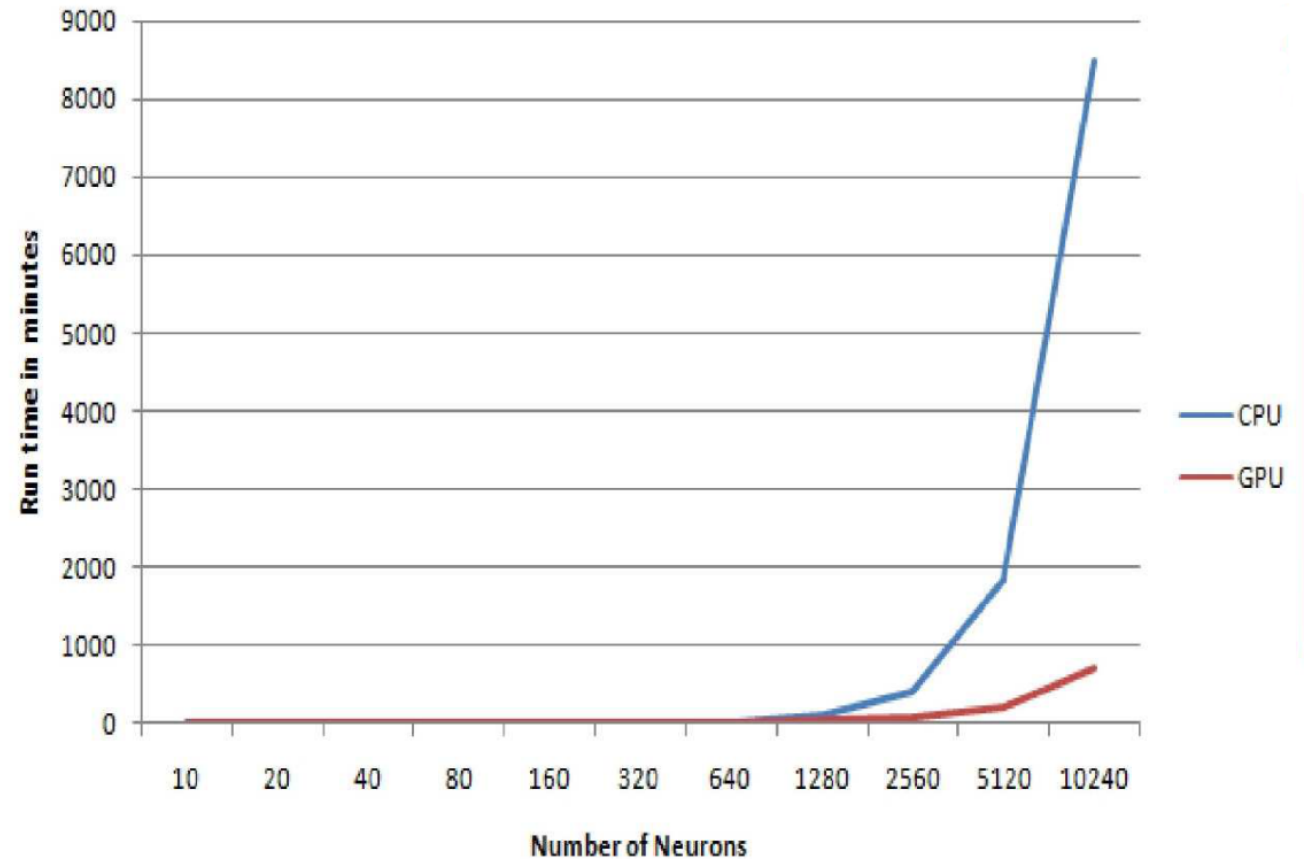
Goal functions:

spike rate + burst rate

Validation:

4-12 calculated features from experimental data

Performance CPU vs. GPU



RESEARCH

Open Access



Simulation of developing human neuronal cell networks

Kerstin Lenk^{1*}, Barbara Priwitzer², Laura Ylä-Outinen³, Lukas H. B. Tietz¹, Susanna Narkilahti³ and Jari A. K. Hyttinen¹

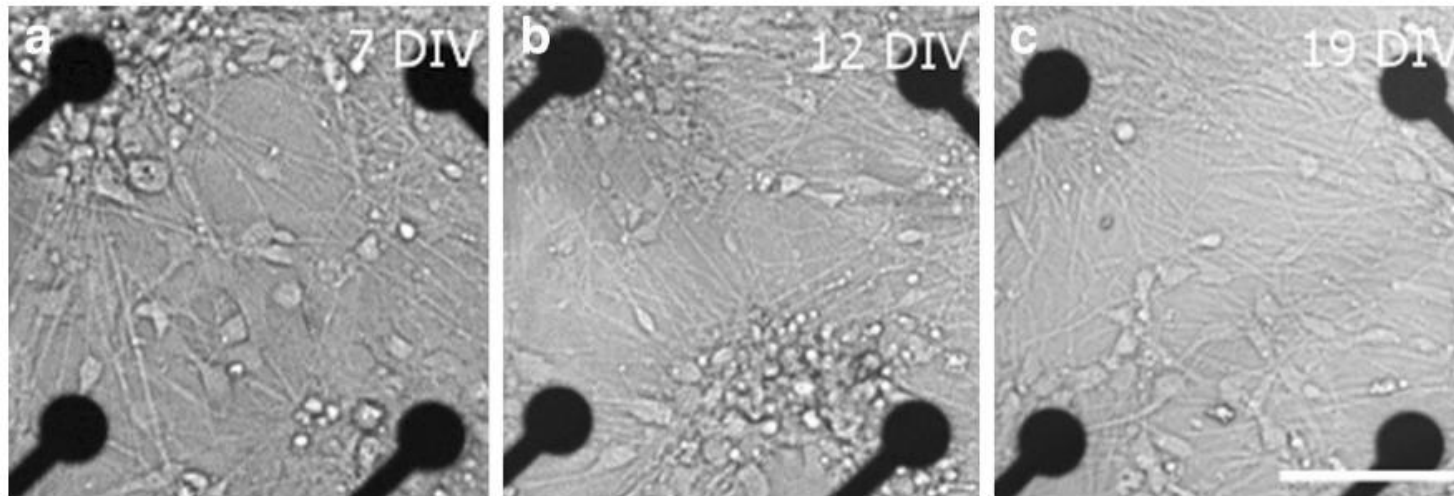
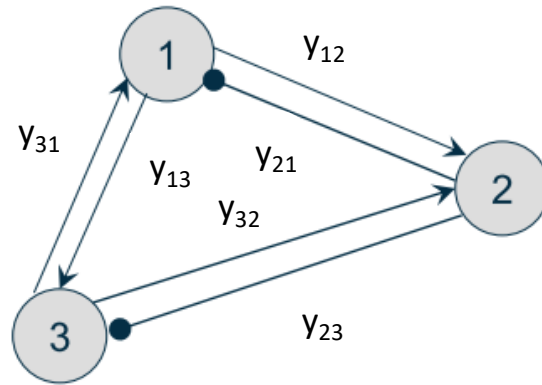


Fig. 1 Neuron distribution of dataset #3 (see Table 1) on the MEA for three points in time (**a** 7 days in vitro (DIV), **b** 12 DIV, and **c** 19 DIV). It is clearly visible that the number of neuronal connections increases and the neurons move over time. The *black dots* indicate the MEA electrodes. The *scale* is 100 μm

Simulation parameters

- 1000 neurons (80% excitatory/ 20% inhibitory)
- Connectivity is increased linearly between measurement time points (1, 2, 4, 6, 8 and 10 %)
- Brute force approach for synaptic strength and noise term



Maturation process reflected by connectivity and synaptic strength

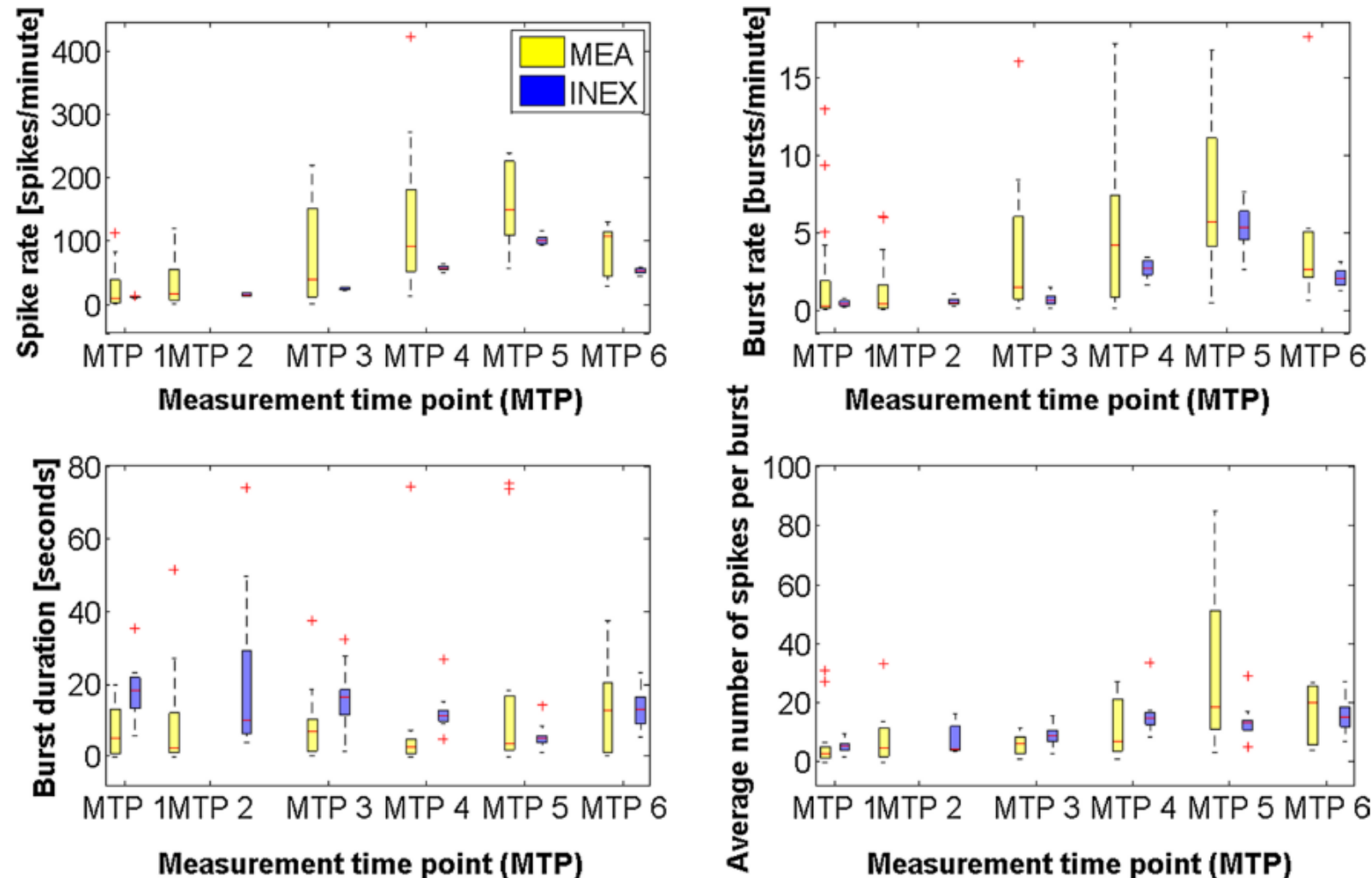
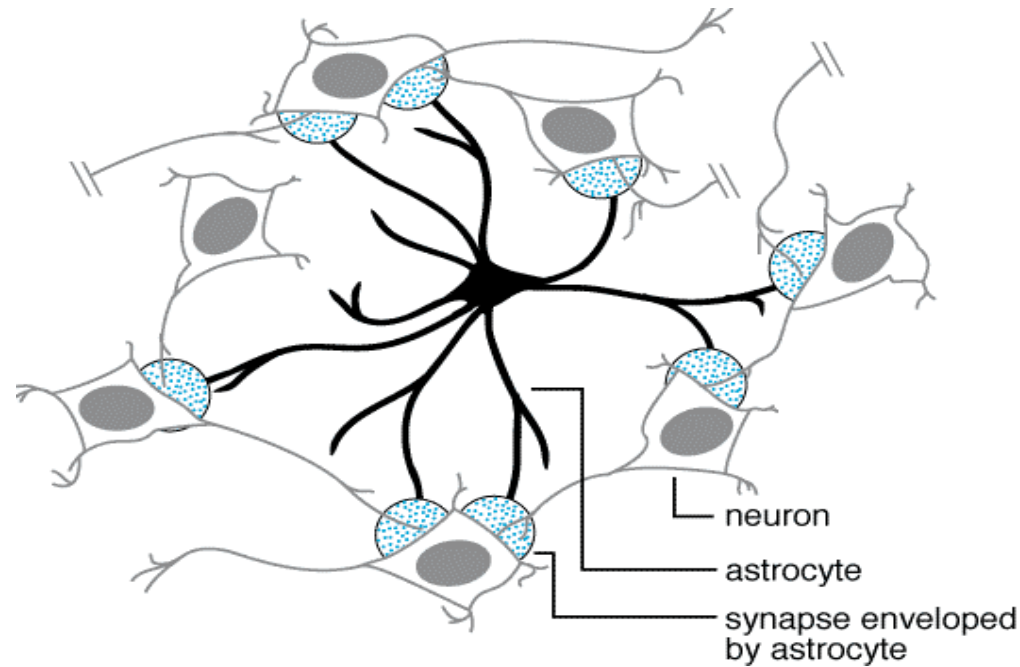


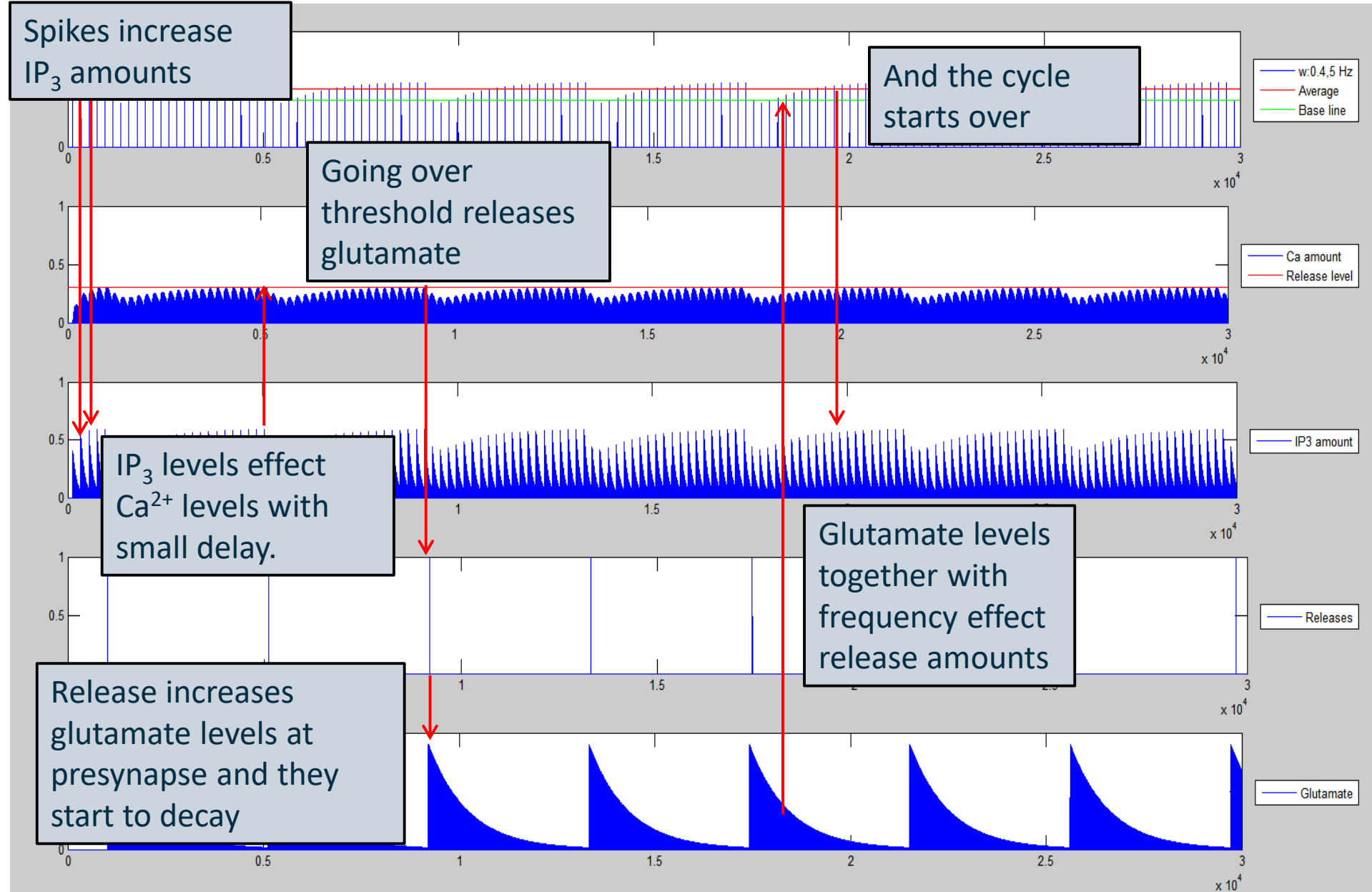
Fig. 3 Development of the neuronal activity over time (measurement time point 1–6). Clockwise: medians and quartiles of the spike rate, the burst rate, the average number of spikes per burst and the burst duration of all wells in the medium activity class, respectively. Note that some outliers are not shown in the last two graphs for visibility reasons. The values of each box plot are represented in Table 3

INEXA model: Astrocytes contribution to the neuronal signaling

$$\lambda_i(t_k) = \max\left(c_i + \sum_j y_{ij} \cdot s_j(t_{k-1}) - \sum_j y_{Astro} \cdot A_{ija}(t_{k-1}), 0\right),$$

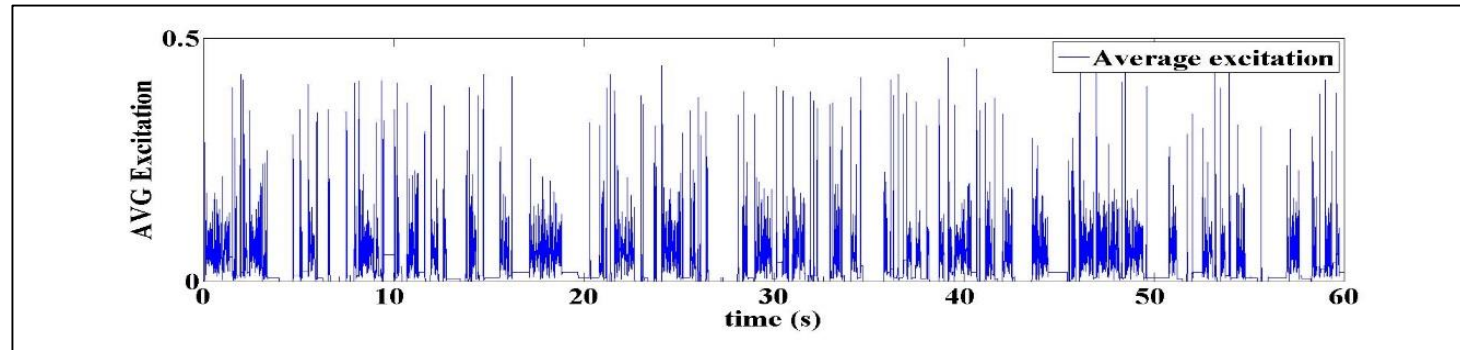


Spike-triggered calcium release

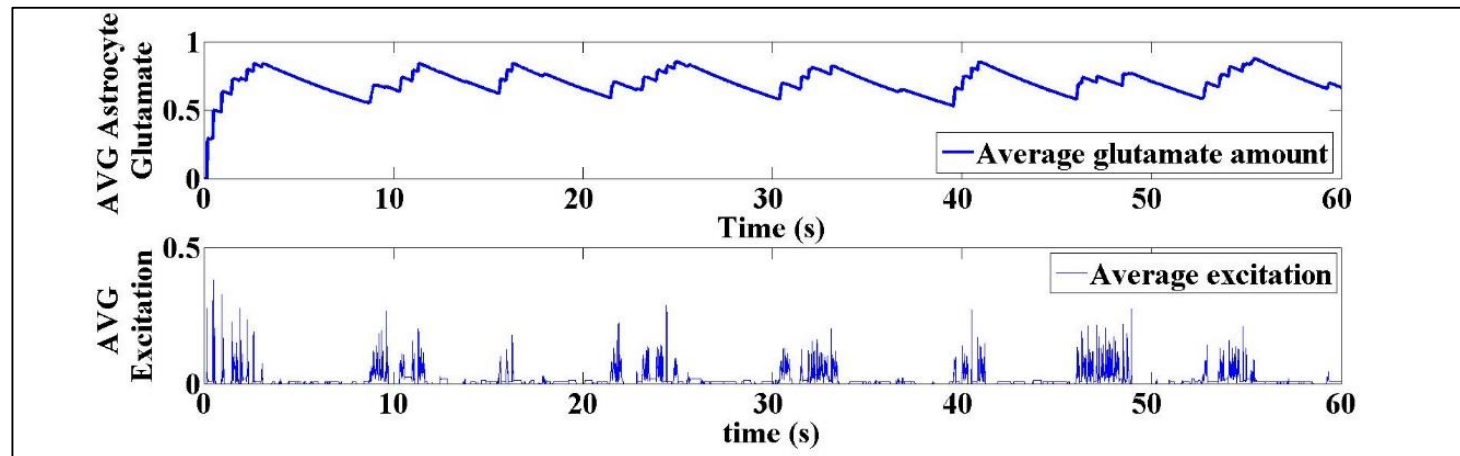


Activity of a single synapse alters from non-bursting behavior to bursting when astrocytes are present

Without astrocyte control (100 neurons)



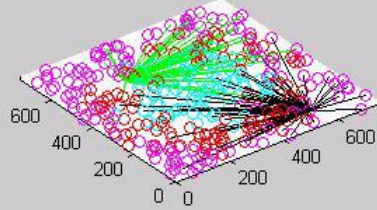
With astrocyte control (100 neurons, 80 astrocytes)



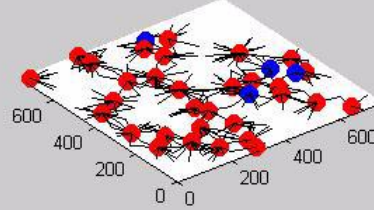
Neuronal firing follows astrocytic calcium dynamics

Mathematical model:

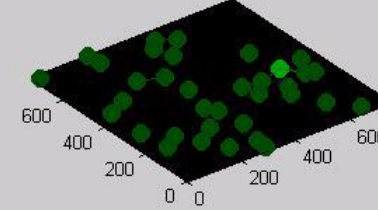
315 neurons (252 ex, 63 in)



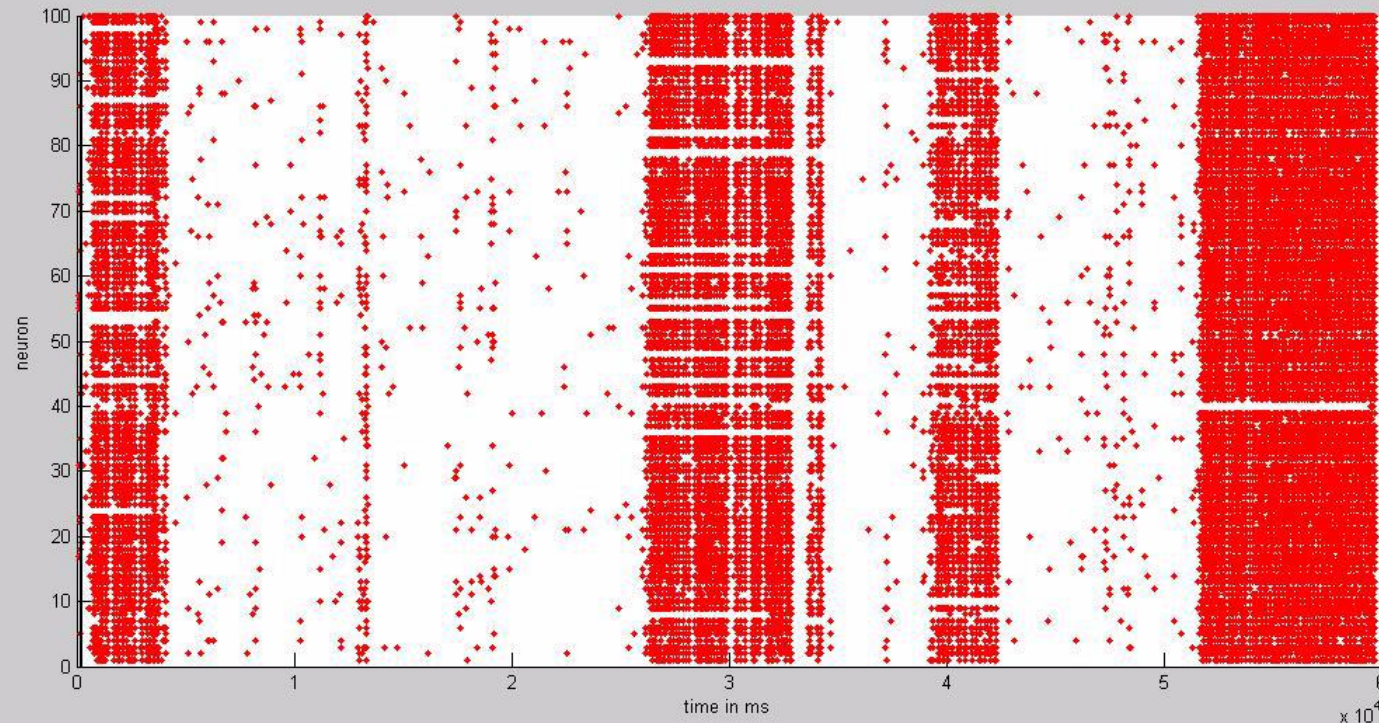
35 astrocytes



"Ca-imaging view":



Example spiketrains of 100 neurons:



Number of astrocytes influences the neuronal network activity

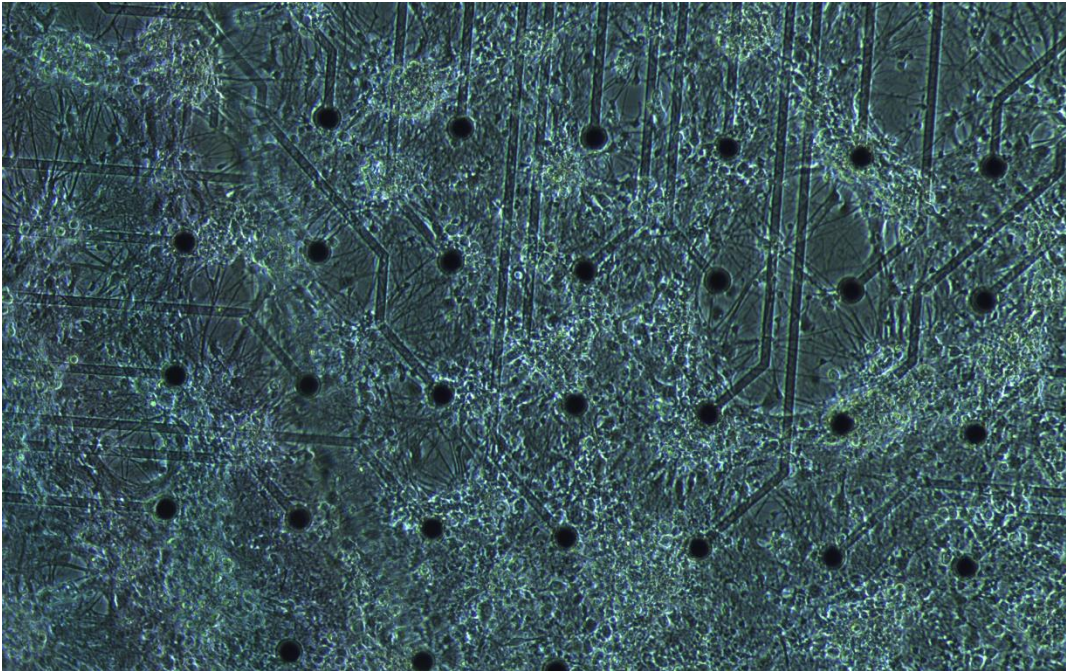
Connectivity

Signaling at the tripartite synapse

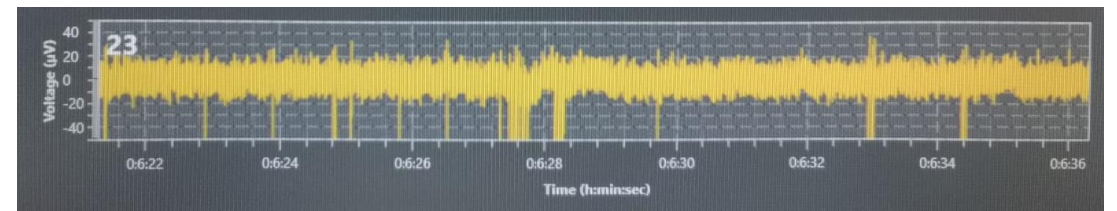
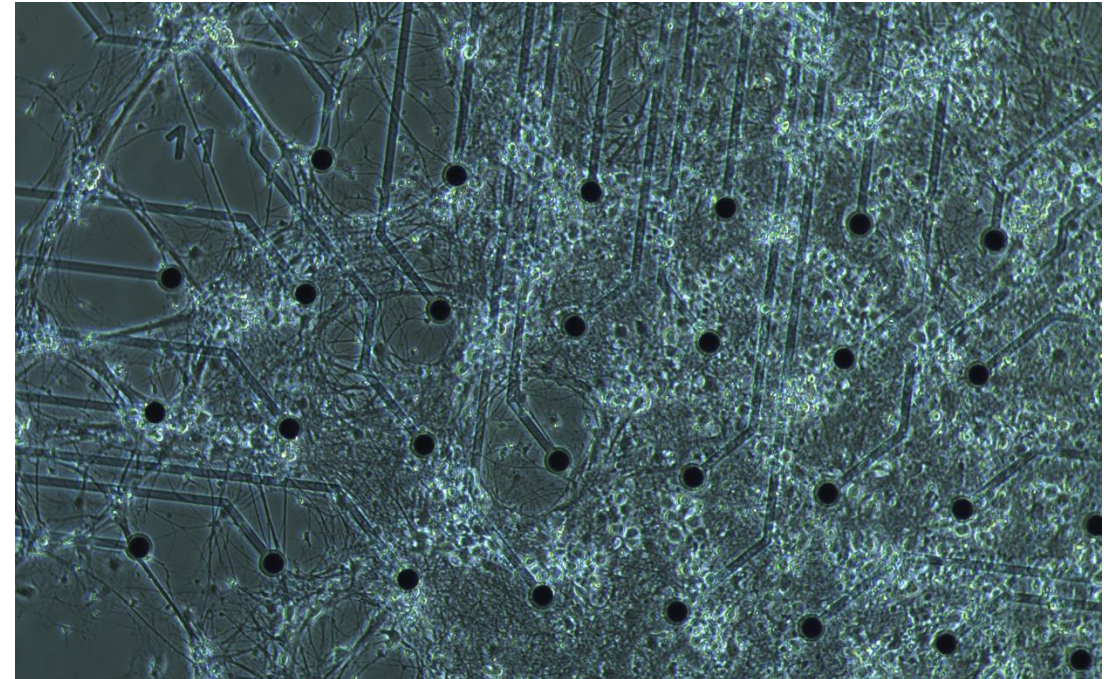
Astrocytes reduce the spike and burst rate but increase the burst duration

Experimental (rat) data on the way

90% neurons, 10% astrocytes

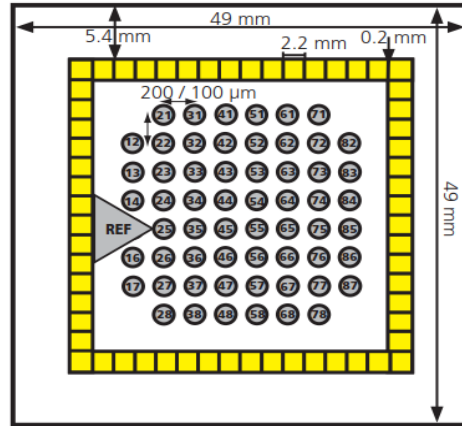
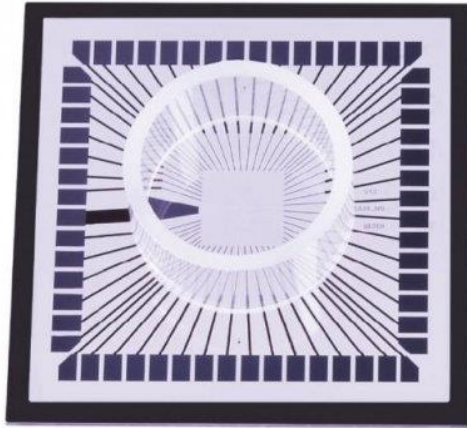


70% neurons, 30% astrocytes



First example of our current work: epilepsy model

Second example of our current work: responses to stimuli

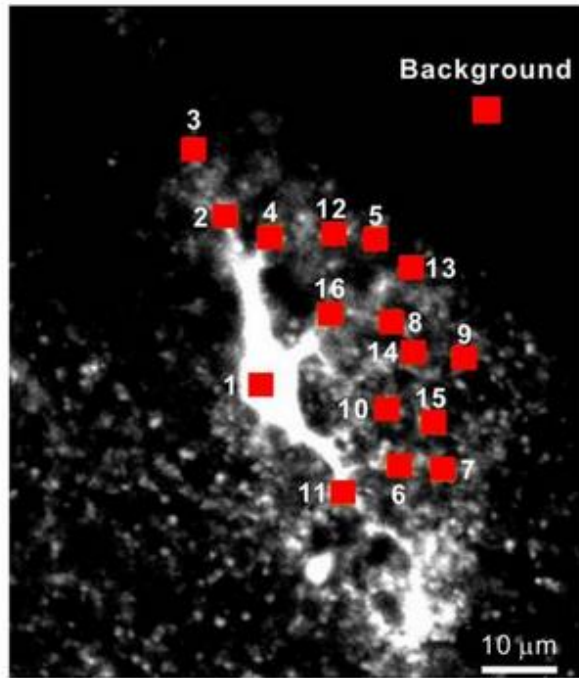


Astrocyte Ca activation; neuronal system driven by noise vs. stimulus

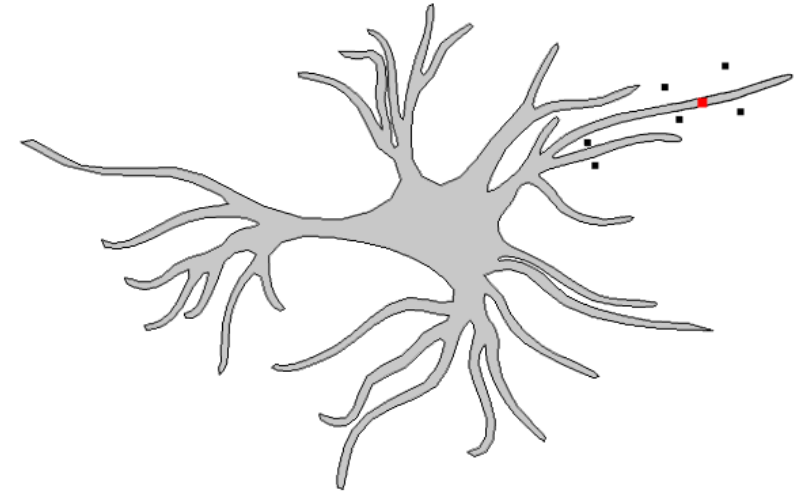
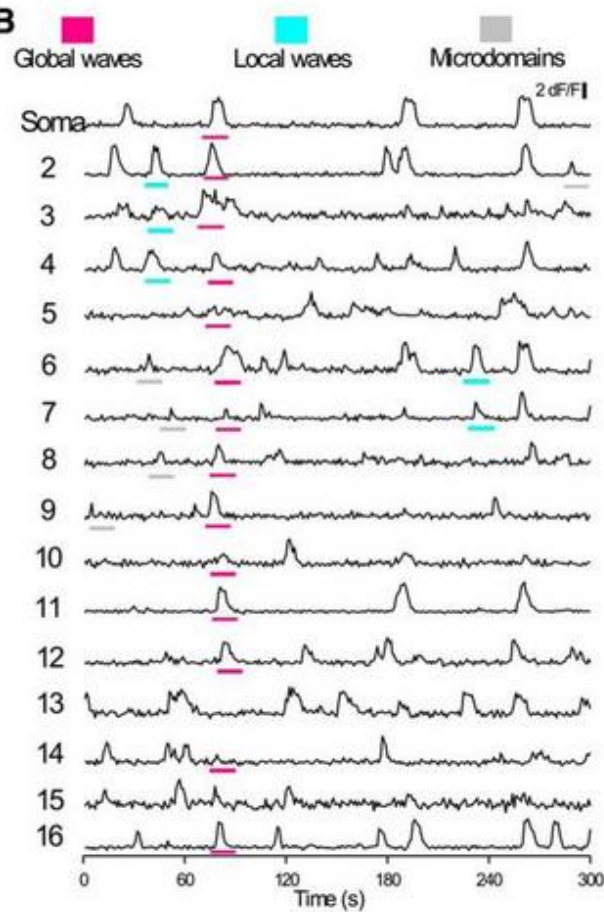
Astrocyte Ca^{2+} activation in “epileptic” neuronal activity

Single cell astrocyte model

A

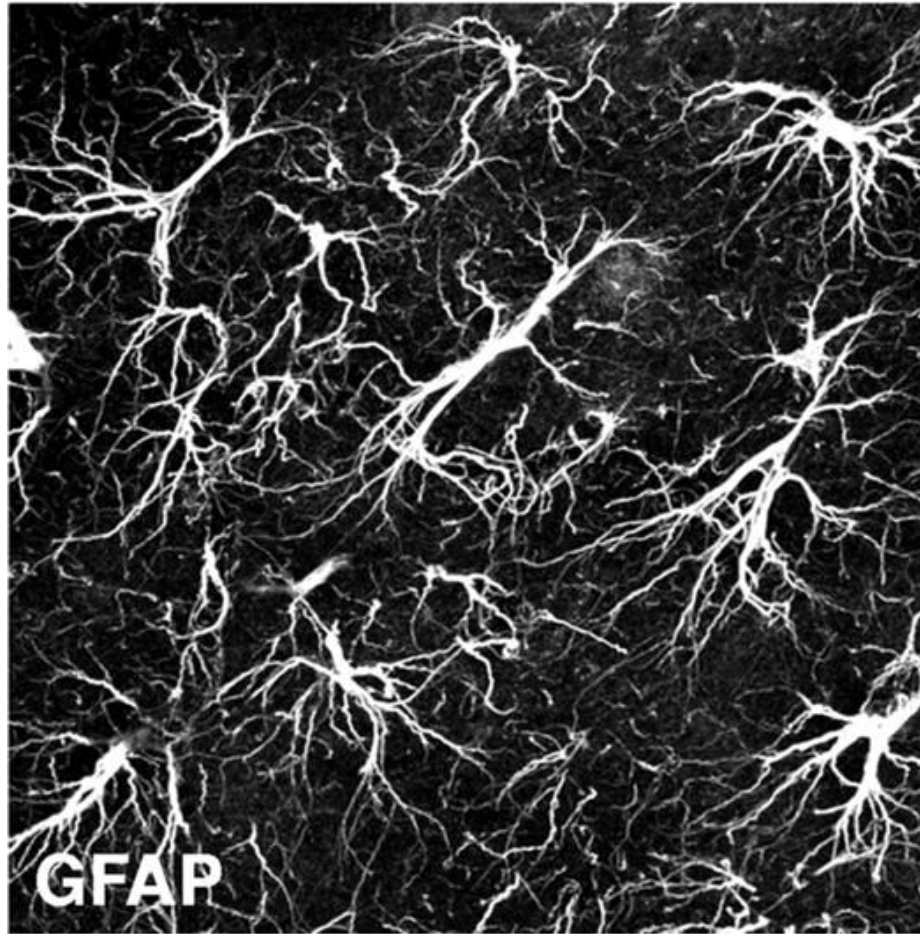


B

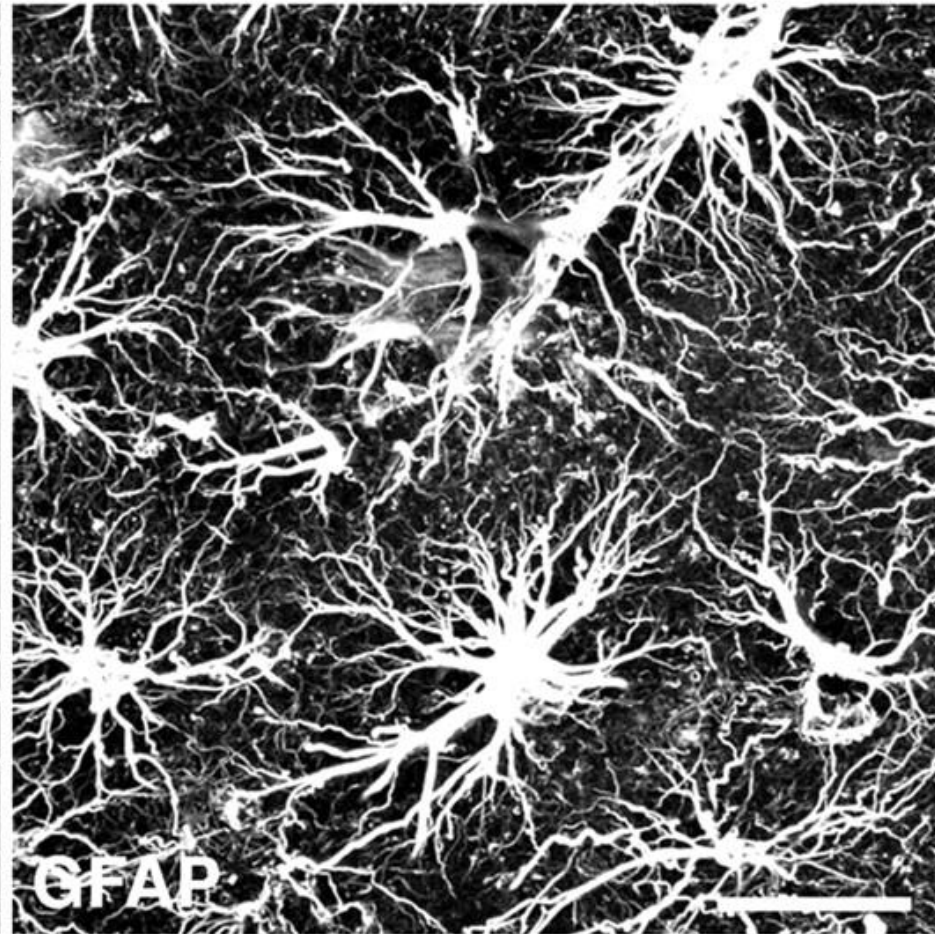


In Alzheimer's disease, astrocytes undergo morphological and functional changes

Nonreactive astrocytes

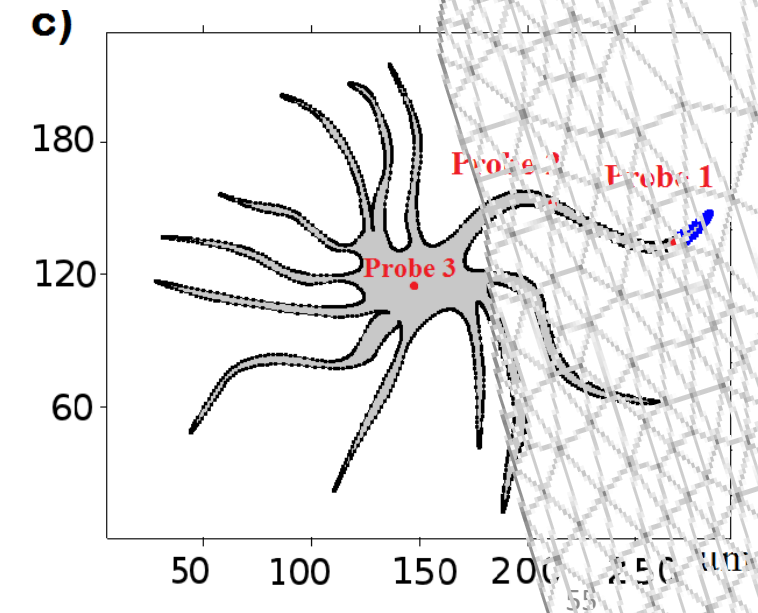


Reactive astrocytes



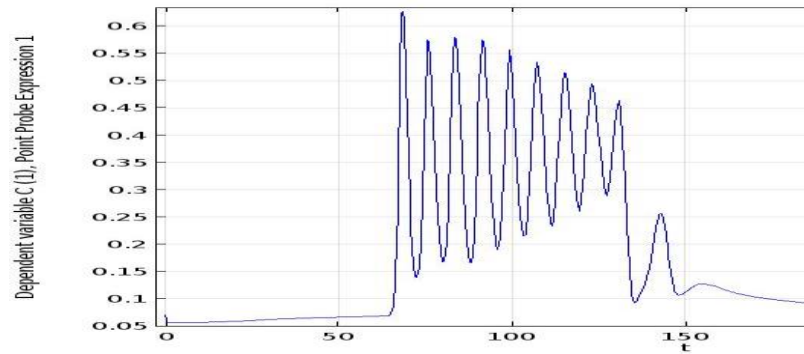
Model implementation as 2D FEM

- Model Based on G-ChI model of De Pitta et al., 2009
- Implementation into COMSOL Multiphysics
- Addition: Diffusion of the IP_3 and calcium in cell
- Boundary condition: input of glutamate e.g. from synapses

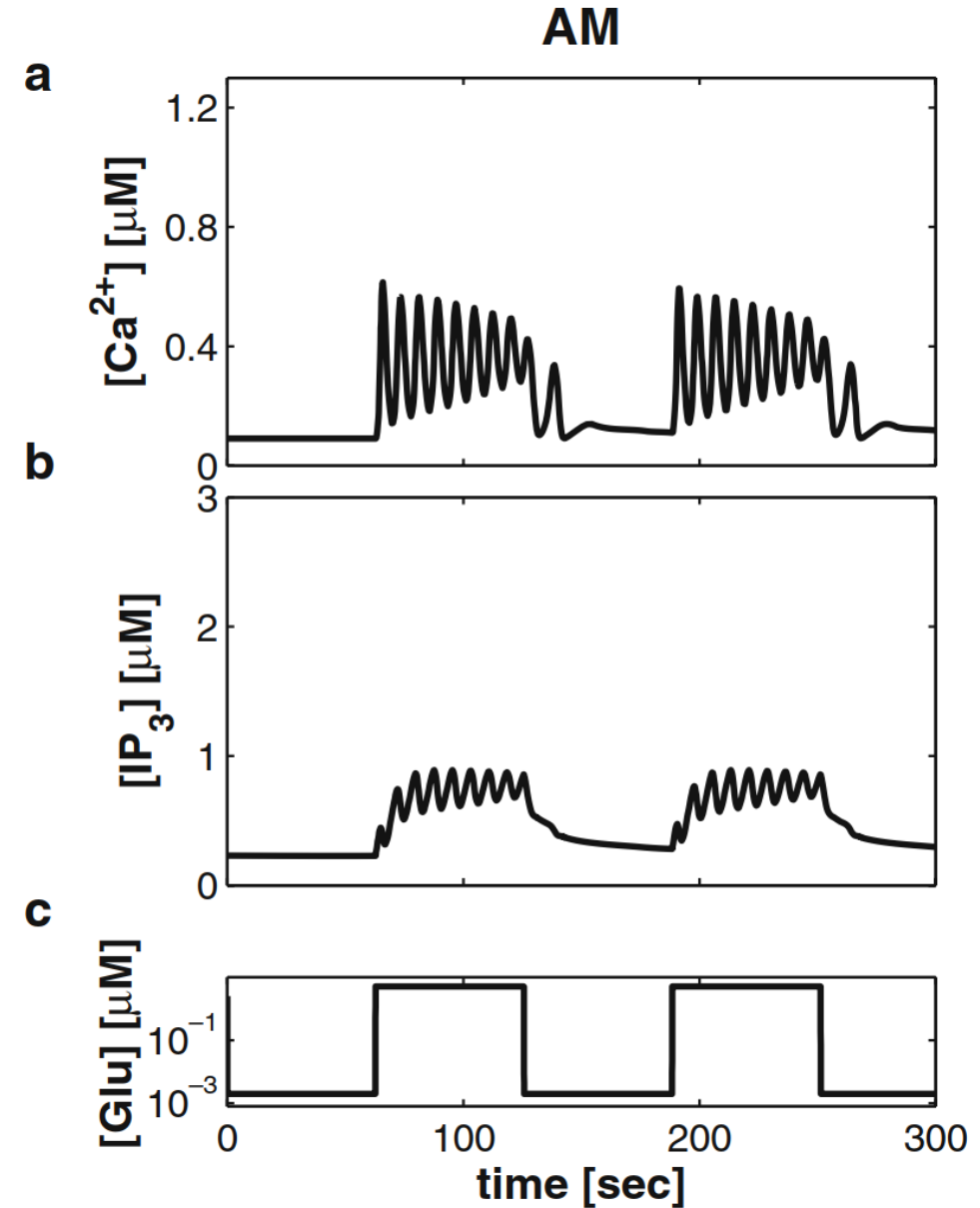
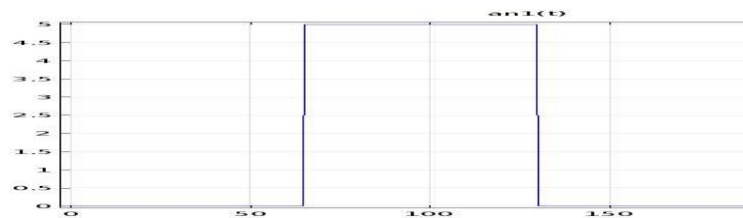


Replication of De Pitta – FEM simulation without spatial dimensions ("0D")

Resulting
Calcium in
astrocyte

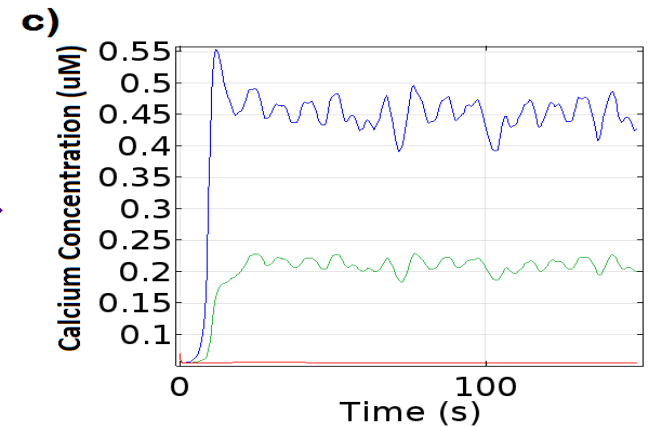
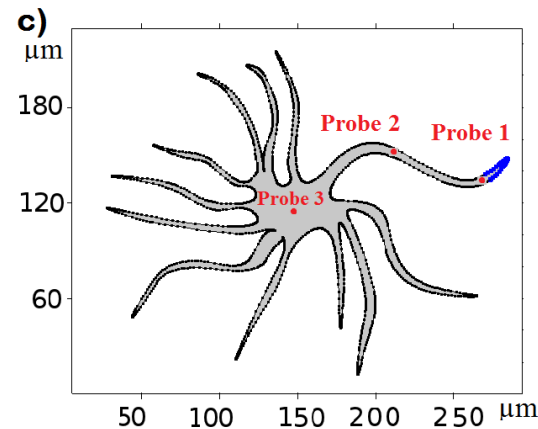
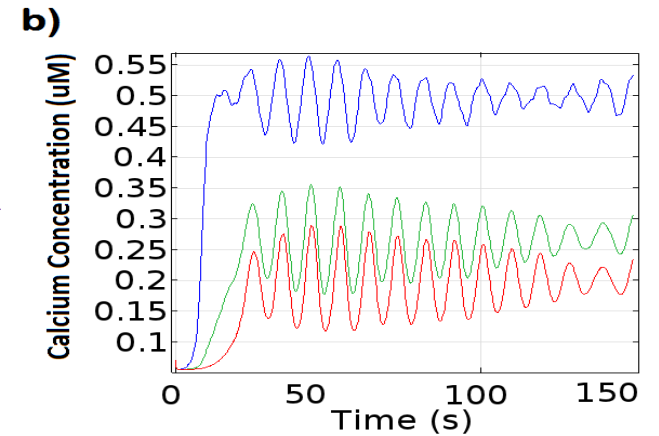
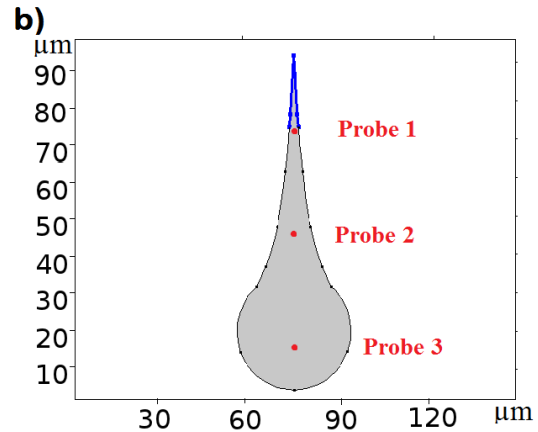
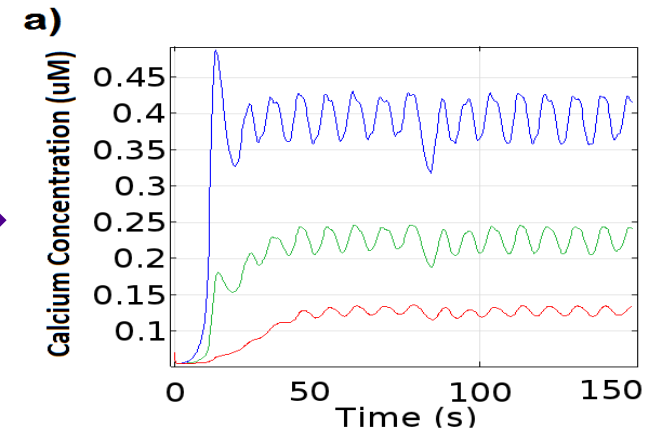
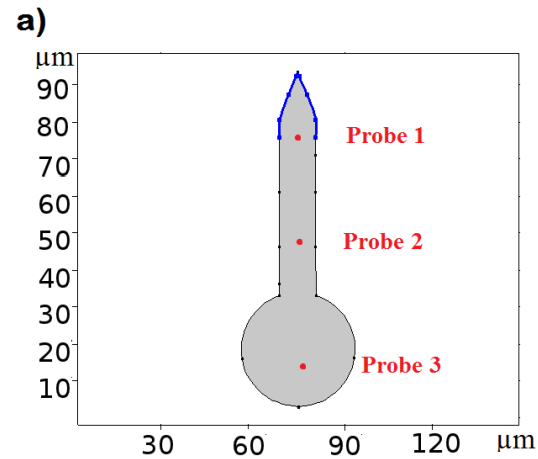
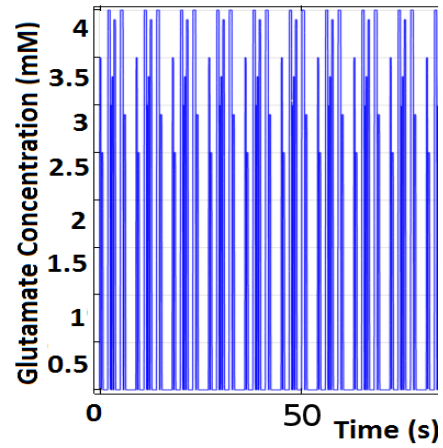


Glutamate
stimulus

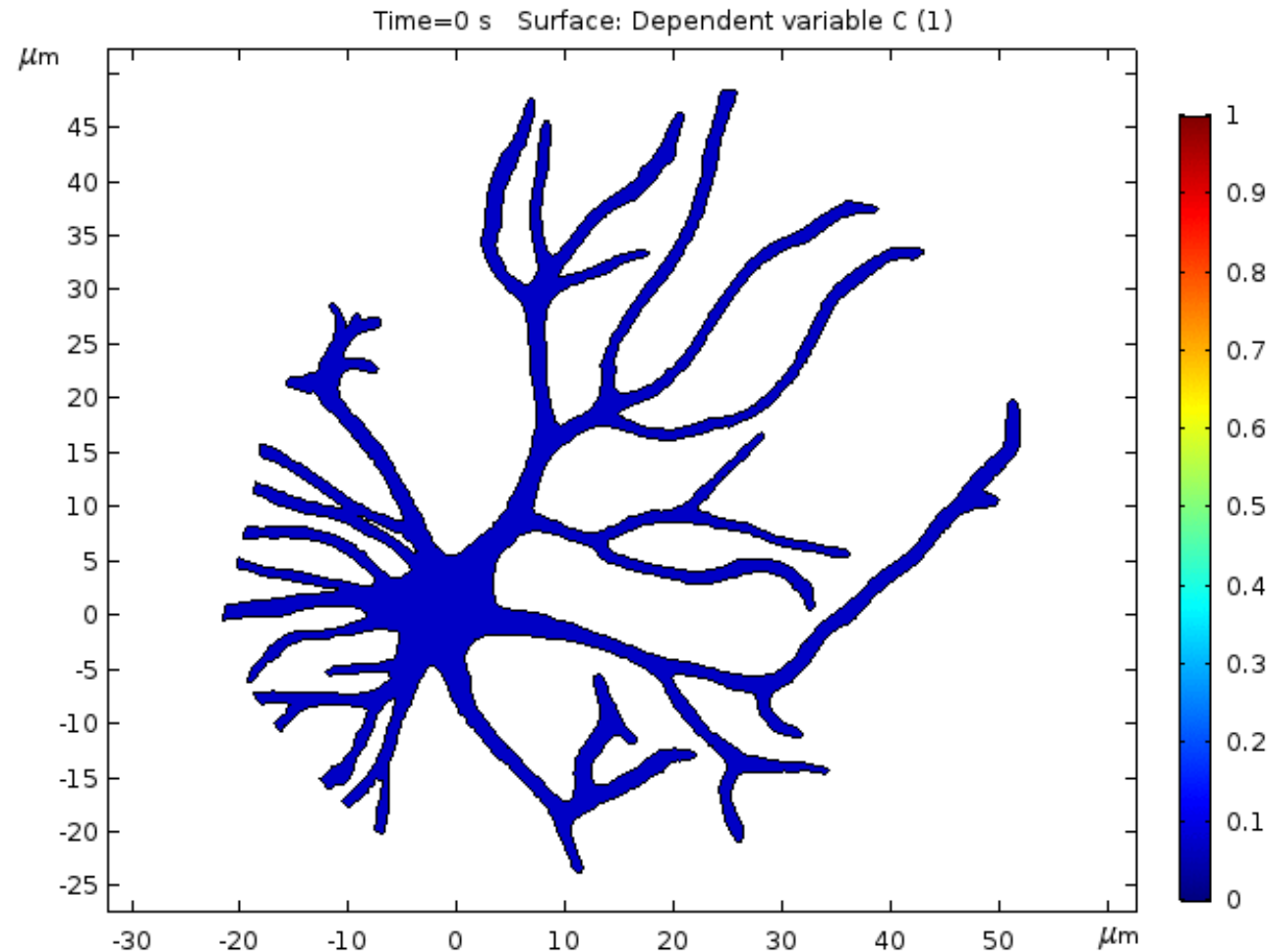


Different geometries

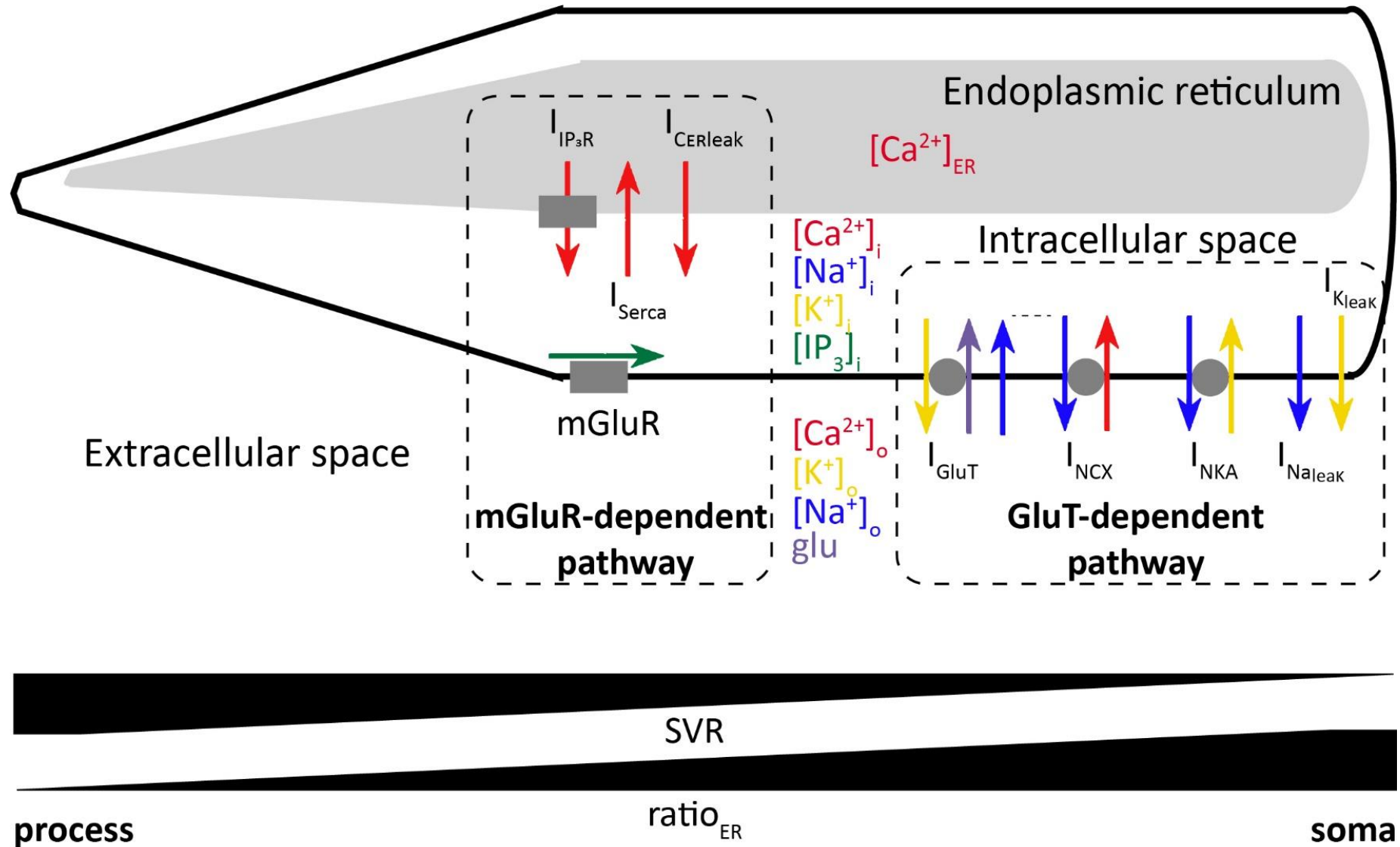
Input



Astrocyte calcium after "synaptic" local release of glutamate



Implementation of glutamate pathways and ER distribution



Governing equation

$$\frac{d[Ca^{2+}]_i}{dt} = \frac{A}{F \cdot Vol} \cdot I_{NCX} + \frac{A \cdot \sqrt{ratio_{ER}}}{F \cdot Vol} \cdot (I_{IP_3R} - I_{Serca} + I_{CERleak})$$

I_{NCX} = Na⁺/Ca²⁺ exchanger

I_{IP_3R} = Ca²⁺ current through the IP3 receptor channel

I_{SERCA} = SERCA pump

$I_{CERleak}$ = Ca²⁺ leak from the ER

A = area of the outer cell membrane

F = Faraday constant

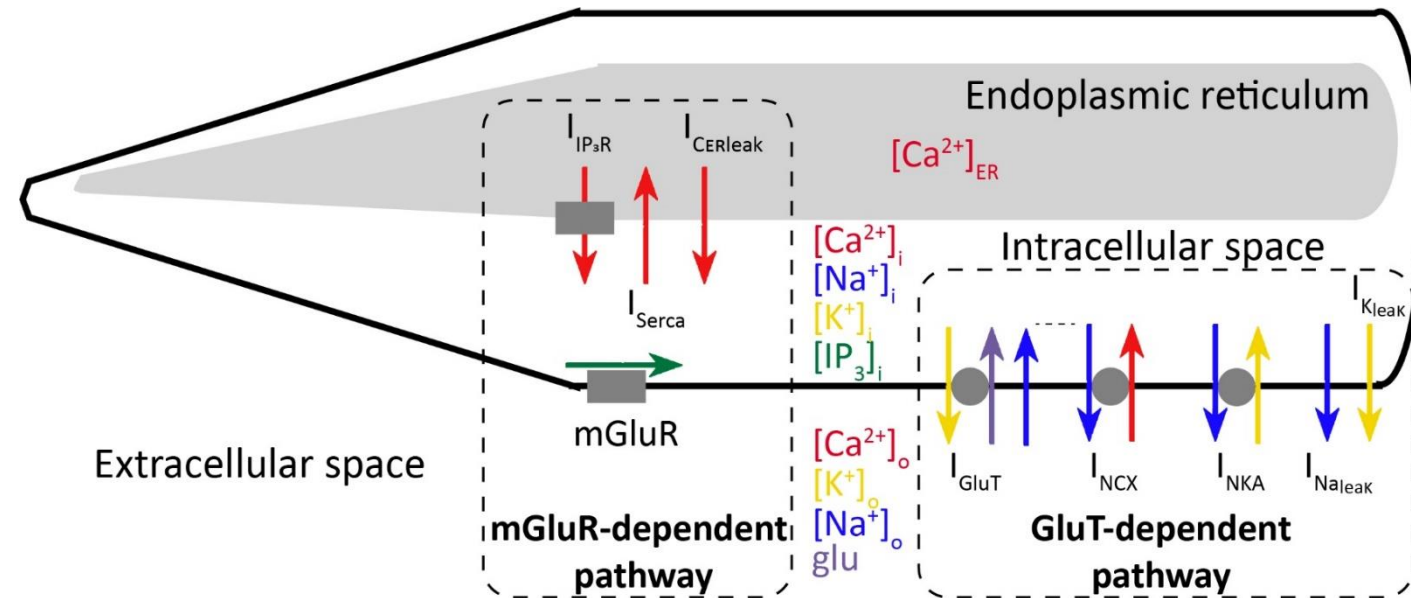
Vol = volume of the intracellular space

$A \cdot \sqrt{ratio_{ER}}$ = area of the internal Ca²⁺ store

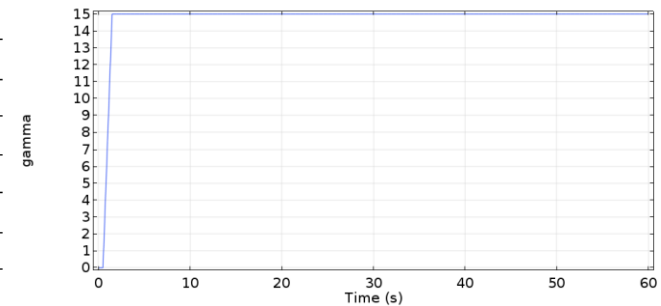
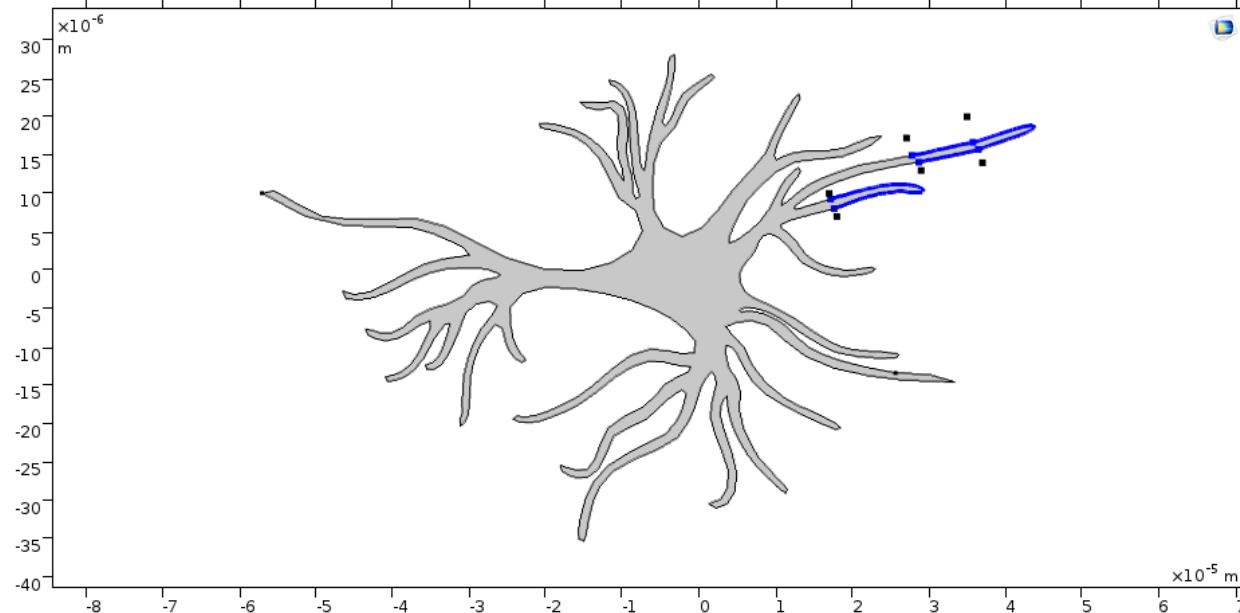
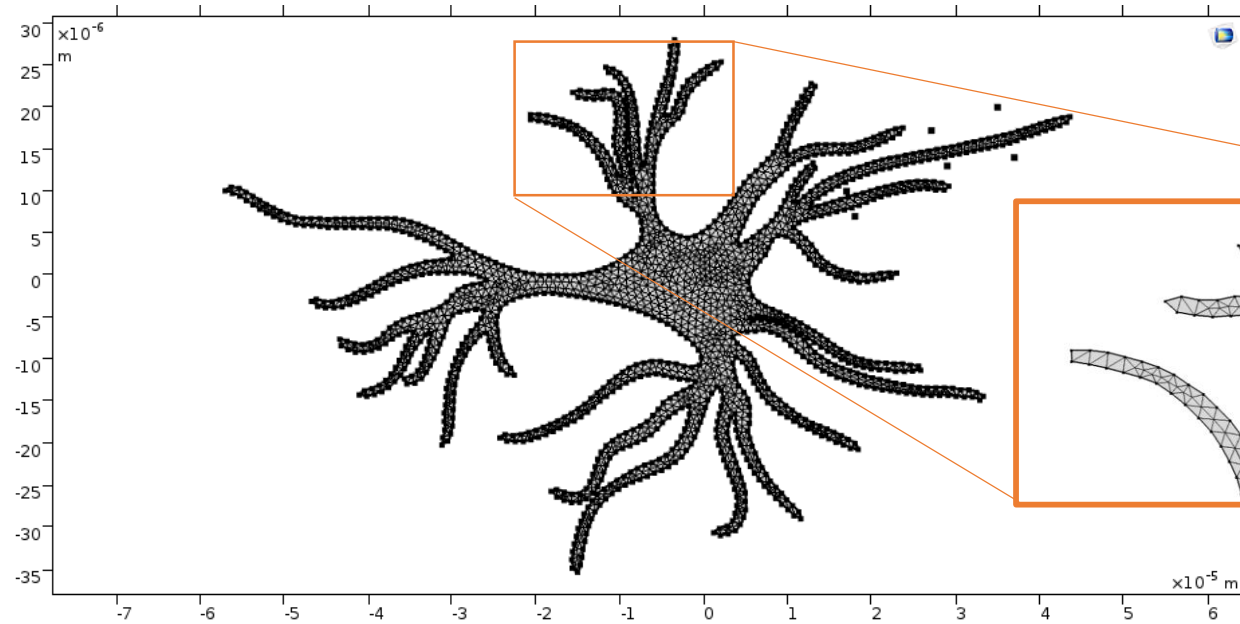
RESEARCH ARTICLE

Spatial separation of two different pathways accounting for the generation of calcium signals in astrocytes

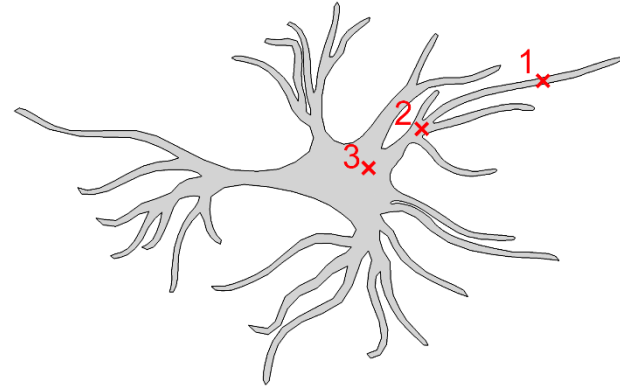
Franziska Oschmann^{1,2*}, Konstantin Mergenthaler¹, Evelyn Jungnickel¹, Klaus Obermayer^{1,2*}



Constant glutamate stimulus at process(es)



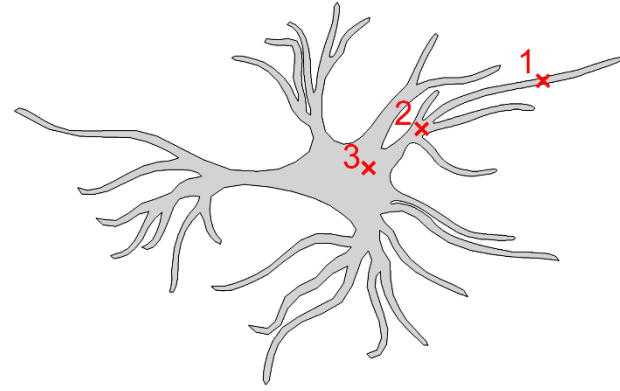
One stimulation site



Work together with Aapo Tervonen

Kerstin Lenk

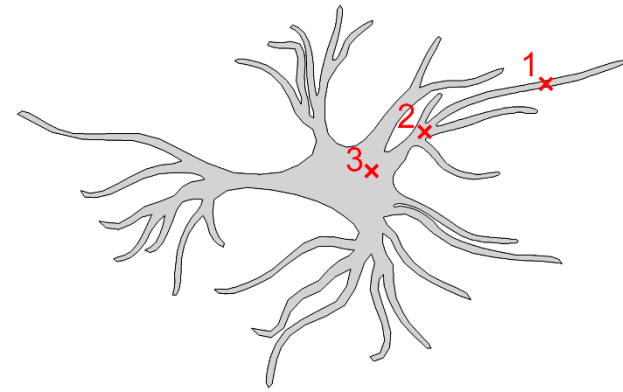
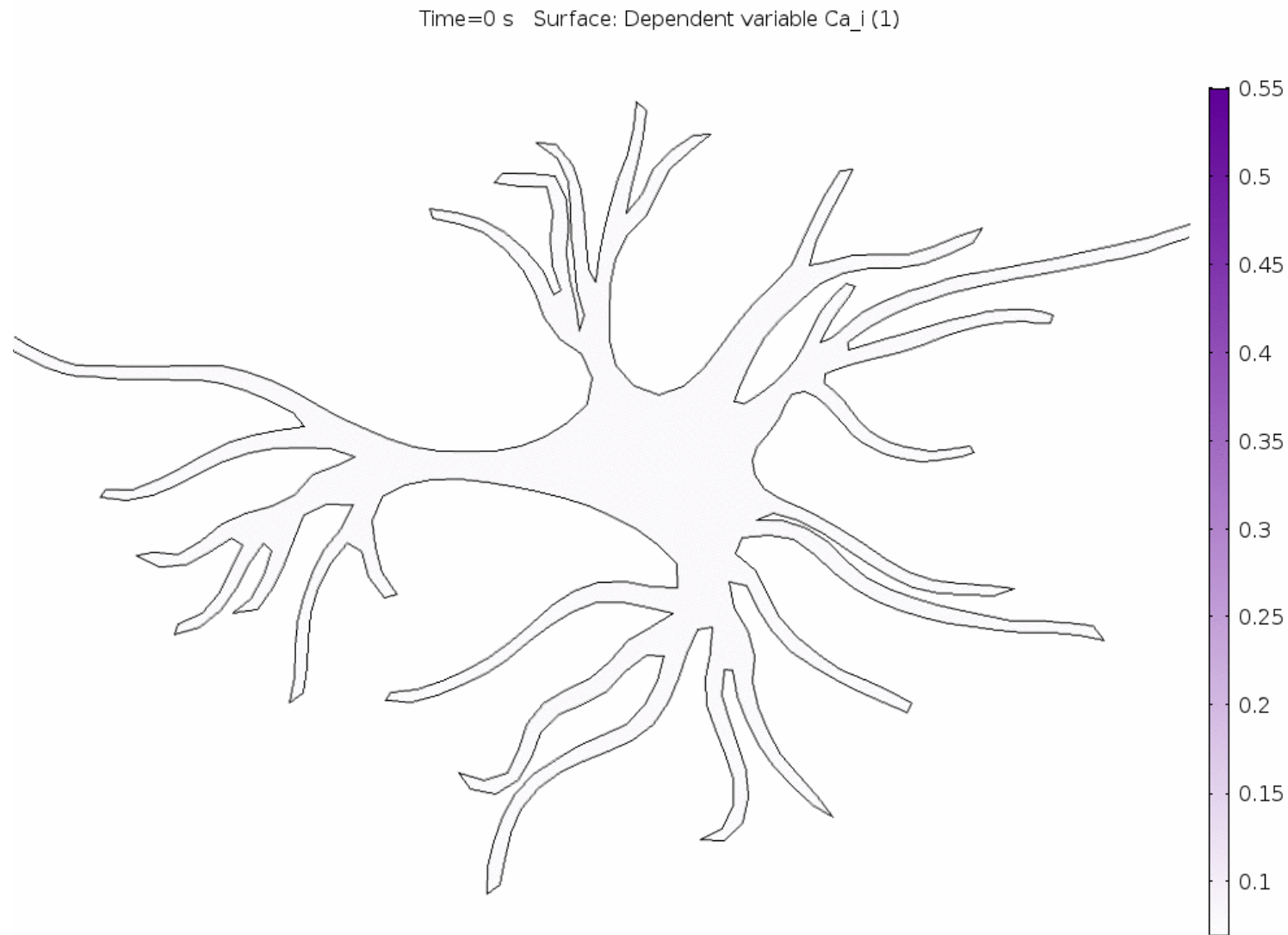
Three stimulation sites



Work together with Aapo Tervonen

Kerstin Lenk

Three stimulation sites



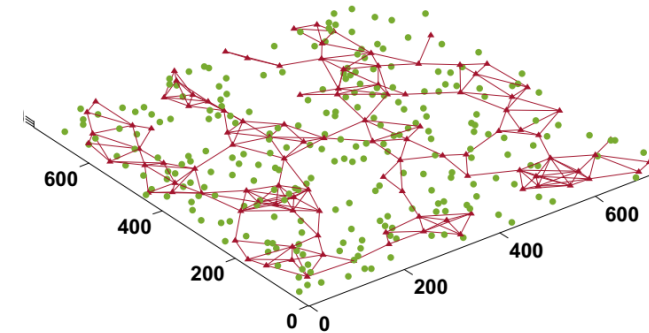
Work together with Aapo Tervonen

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Conclusions

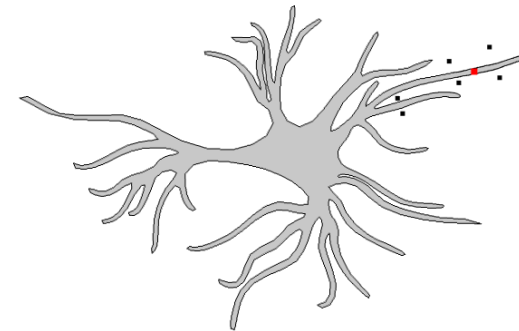
(1) INEXA model:

- One of the first neuron-astrocyte network models where one astrocyte is connected to several hundreds of excitatory synapses
- Astrocyte control over neurons can have profound effects to network behavior → astrocytes prolong the burst duration of neurons, while restricting hyperactivity
- The model is only using part of the pathways astrocytes are known to have



(2) Single cell astrocyte model:

- Calcium spread based on number of input sides
- Next steps: different morphologies, gap junction coupling with adjacent astrocyte, 2D vs 3D



ModelDB - <https://senselab.med.yale.edu/modeldb/>



Submit Model

ModelDB provides an accessible location for storing and efficiently retrieving computational neuroscience models. ModelDB is tightly coupled with [NeuronDB](#). Models can be coded in any language for any environment. Model code can be viewed before downloading and browsers can be set to auto-launch the models. For further information, see [model sharing in general](#) and [ModelDB in particular](#).

Browse or search through over 1000 models using the navigation on the left bar or in the menu button on a mobile device. To search papers instead of models, go [here](#); this may be used to identify models whose paper cites or is cited by a given paper.

Springer Series in Computational Neuroscience

Maurizio De Pittà
Hugues Berry *Editors*

Computational Glioscience

 Springer

Main parts:

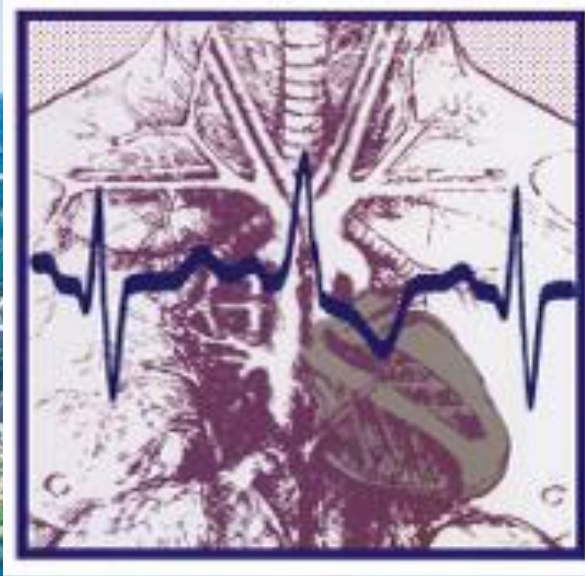
- Introduction
- Calcium Dynamics
- Tripartite Synapse and Regulation of Network Activity
- Homeostasis and Metabolic Coupling
- Computational Tools to Analyze and Model Astrocyte Experiments

Save the date:
Nordic Organ on Chip Workshop
"3rd" NOoC Workshop
22-23 August 2019
Tampere, Finland

Workshop is for PIs and researchers. During the meeting we will arrange two workshop sessions with oral presentations and a poster session/ hands-on training. On Thursday evening we are planning to have a get-together with outdoor activities and dinner.

For more information, contact

mari.pekkanen-mattila@tuni.fi



49th Computing in Cardiology CinC2022

September 2022

Tampere, Finland

Many thanks to ...

Funding



Teke
Human Spare Part 2

Tampere University, Finland

Jari Hyttinen

Eero Satuvuori (Räisänen; now lost to industry)

Antonio Ladron De Guevara (now in Madrid, Spain)

Barbara Genocchi

Aapo Tervonen

Annika Ahtiainen

Sama Saeid

Collaborations

Hugues Berry, INRIA, France

Jules Lallouette, INRIA, France

Katja Nieweg, Philipps-University Marburg, Germany

AND YOU!

