

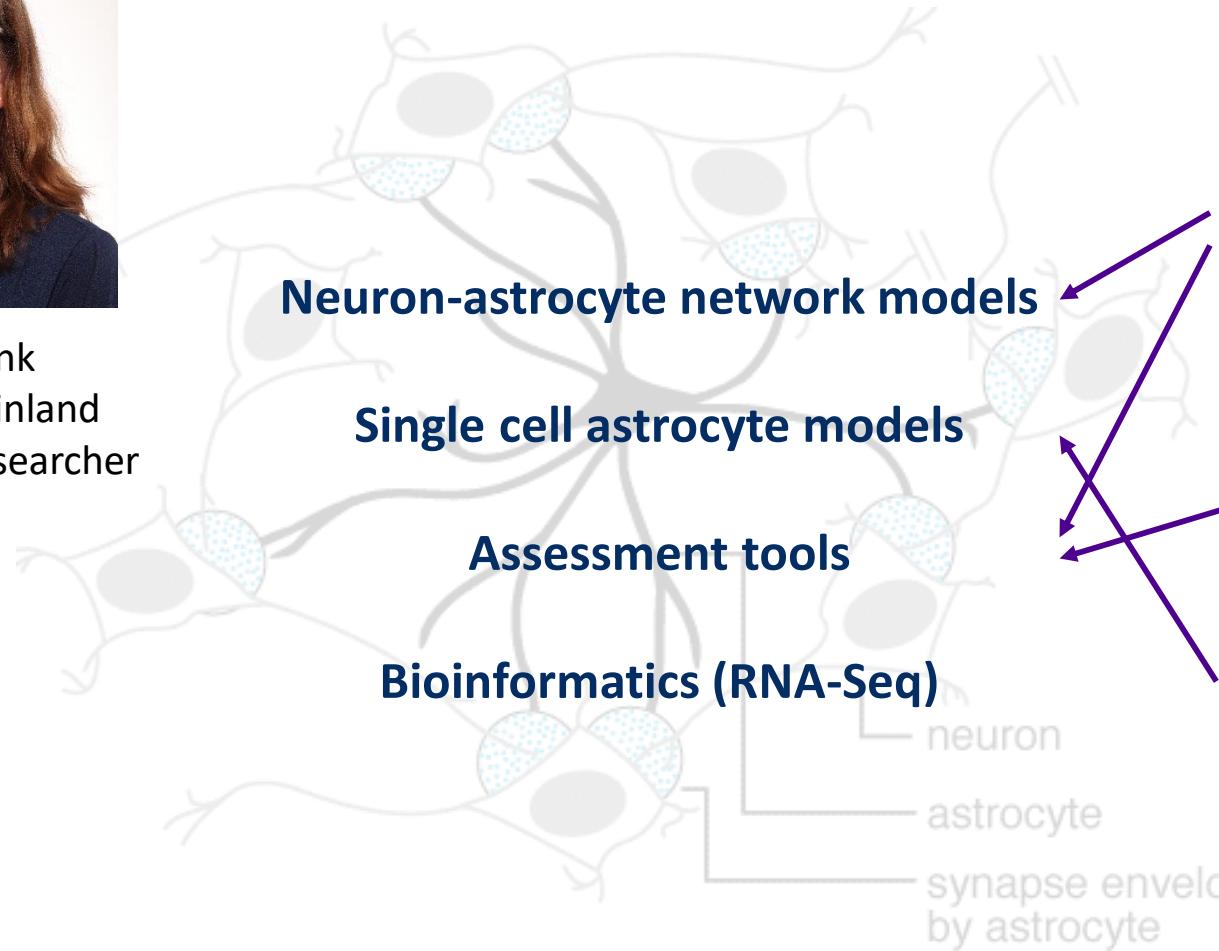
Part 2: Computational Models of Single Cell Astrocytes and Neuron-Astrocyte Interactions

Dr. Kerstin Lenk
Tampere University, Finland
Faculty of Medicine and Health Technology

Astrocyte centered modeling (current members)



Kerstin Lenk
Academy of Finland
Postdoctoral Researcher



Barbara Genocchi
PhD student

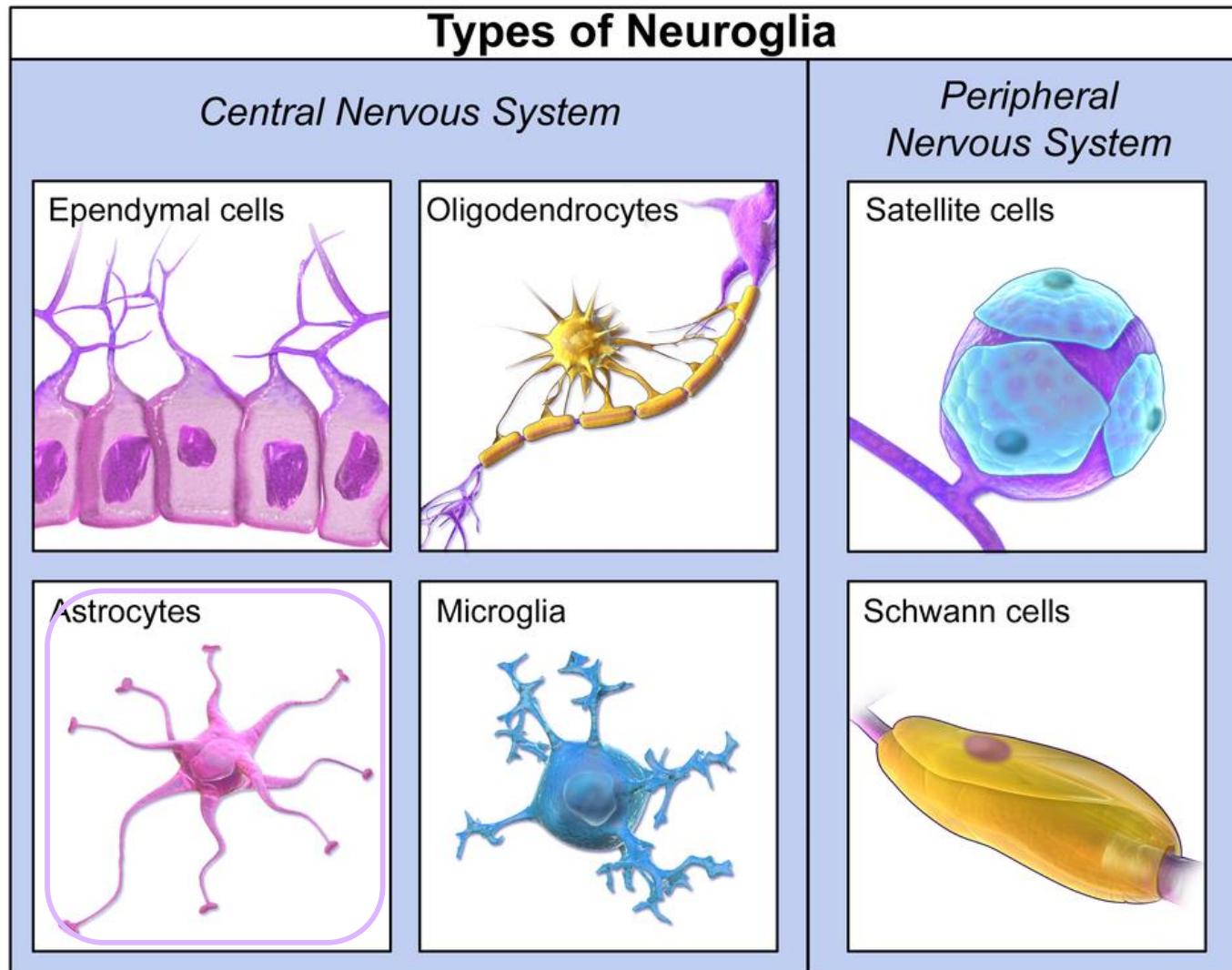


Sama Saeid
Master's student



Aapo Tervonen
PhD student

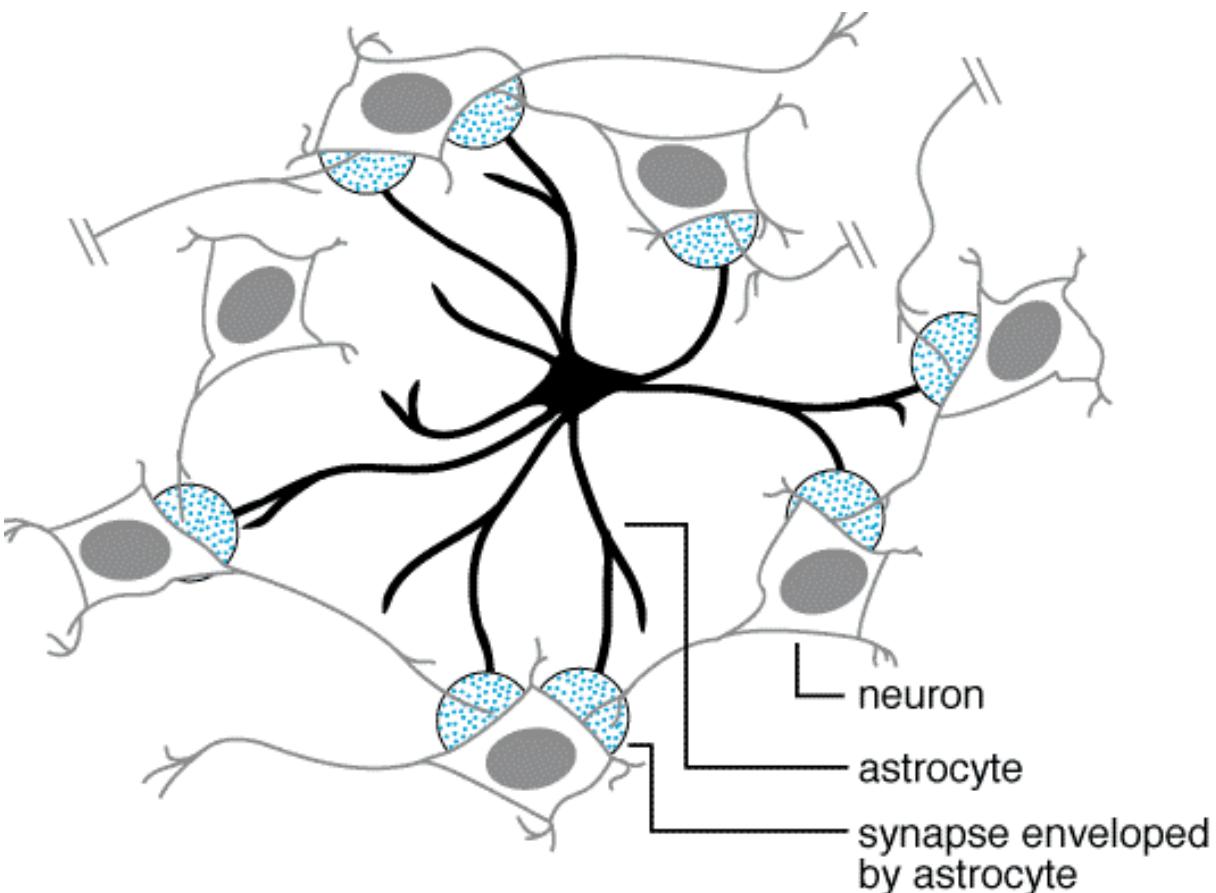
Glia cell types



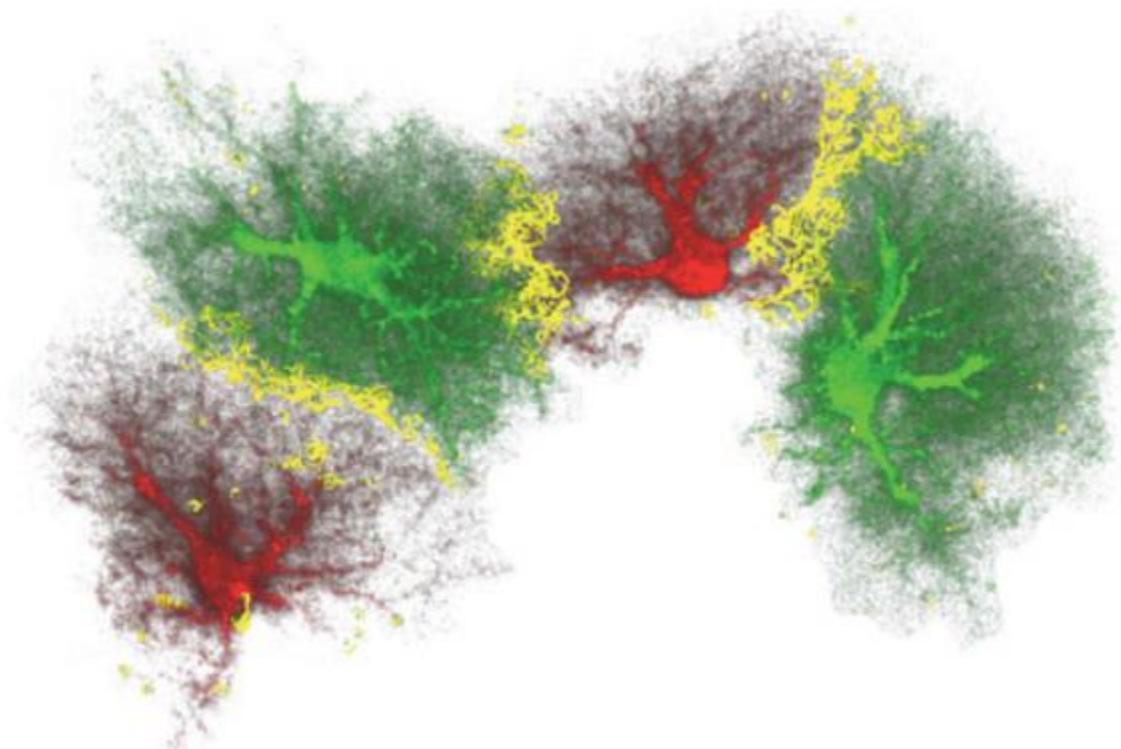
- Ependymal cells – spinal cord, blood-cerebrospinal fluid barrier
- Oligodendrocyte – insulation
- Microglia – immune response, synapse formation/pruning
- Astrocyte – tight junctions, nutrients, modulation of neuronal activity
- Satellite cells – regulate the external chemical environment
- Schwann cell – insulation of axons in peripheral nervous system

Astrocytes are more than support cells

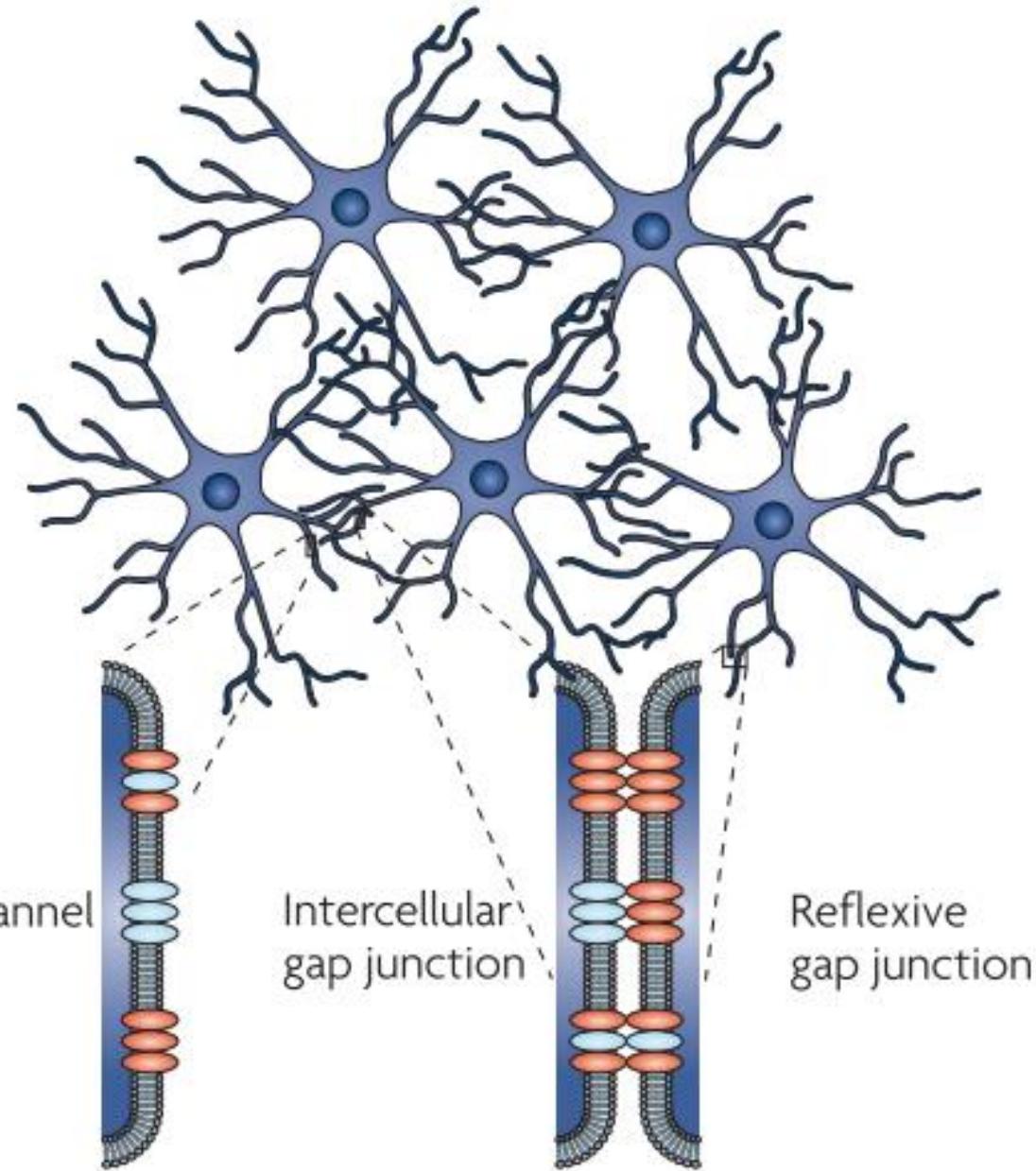
Neuron-astrocyte connections



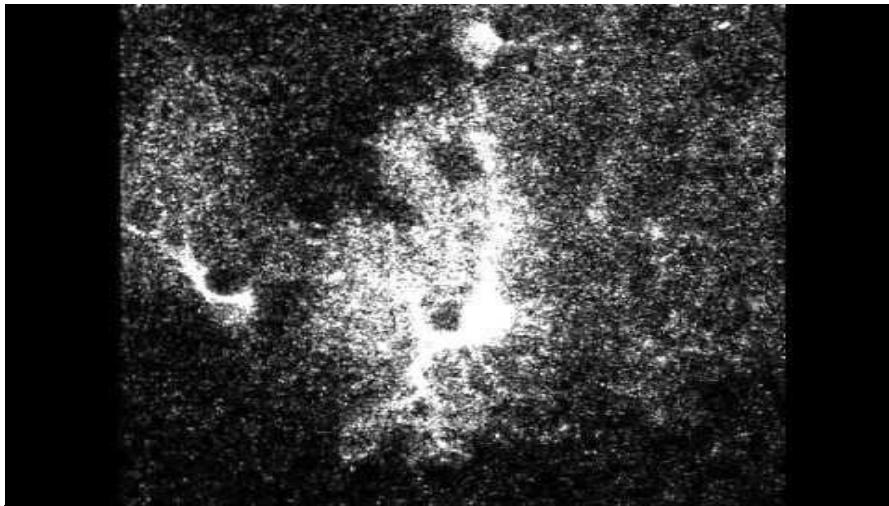
Astrocyte-astrocyte connections



Gap junction coupling between astrocytes



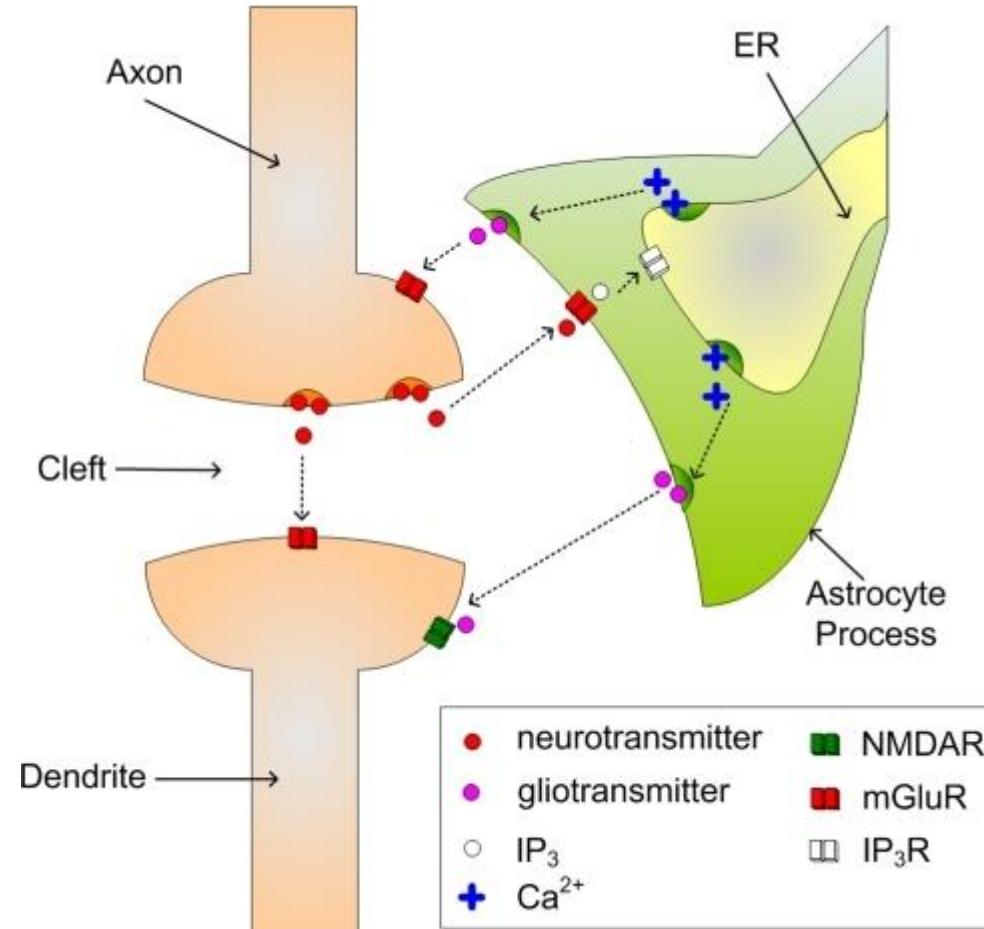
Calcium signalling in the tripartite synapse



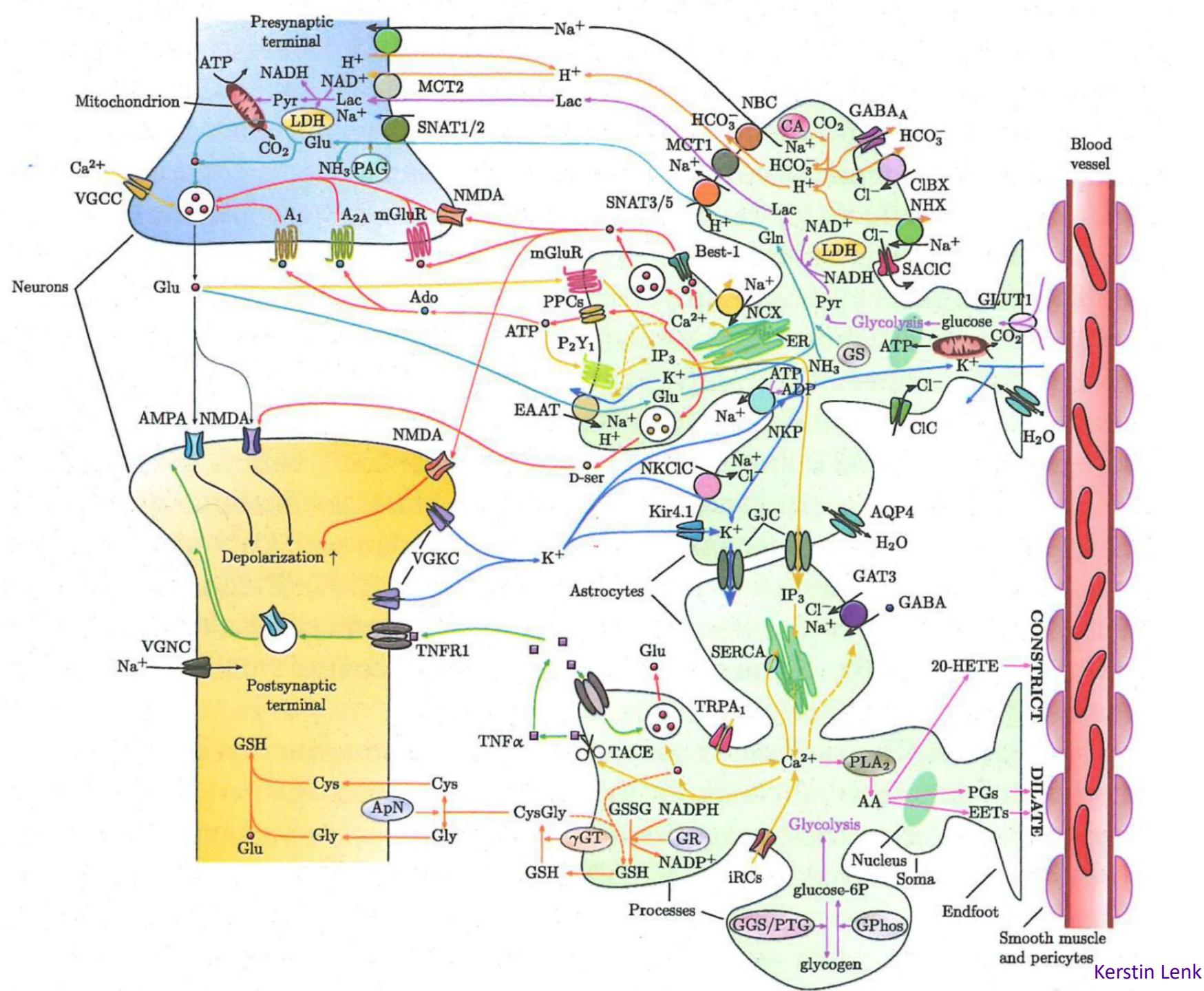
Video:

<https://www.youtube.com/watch?v=y7Yg1mlvLlc>

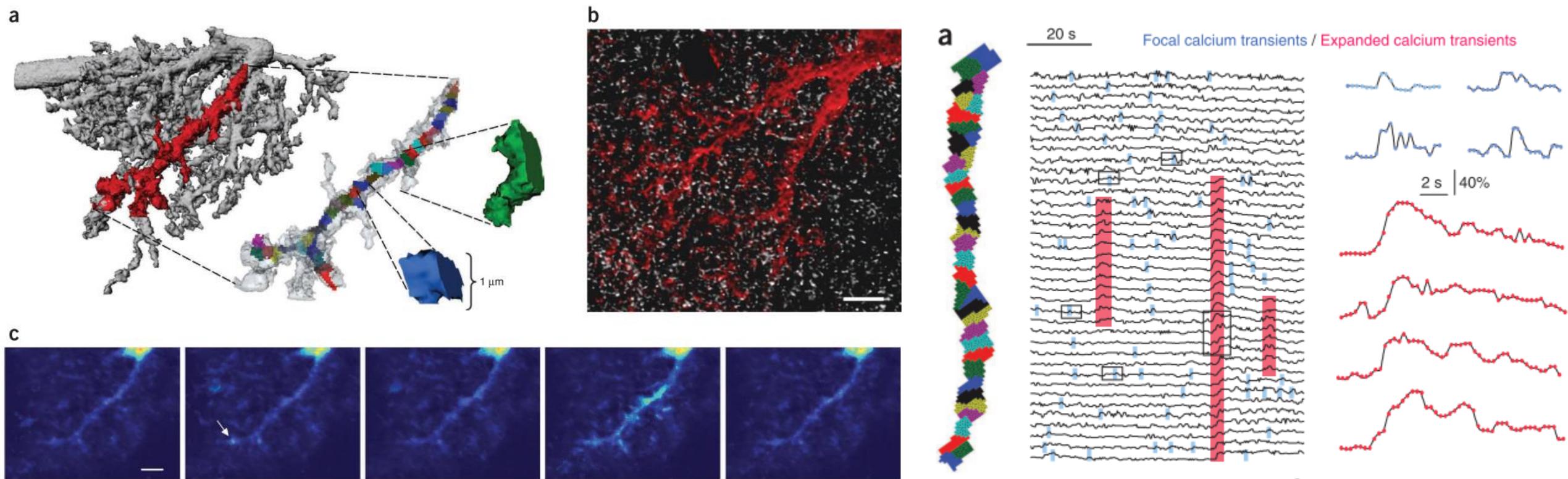
- Neurotransmitters trigger IP₃ release in astrocytes
- IP₃ triggers calcium release from the endoplasmic reticulum
- IP₃ can diffuse through gap junctions; calcium only locally in the astrocytes



Astrocyte communication with neurons and vasculature



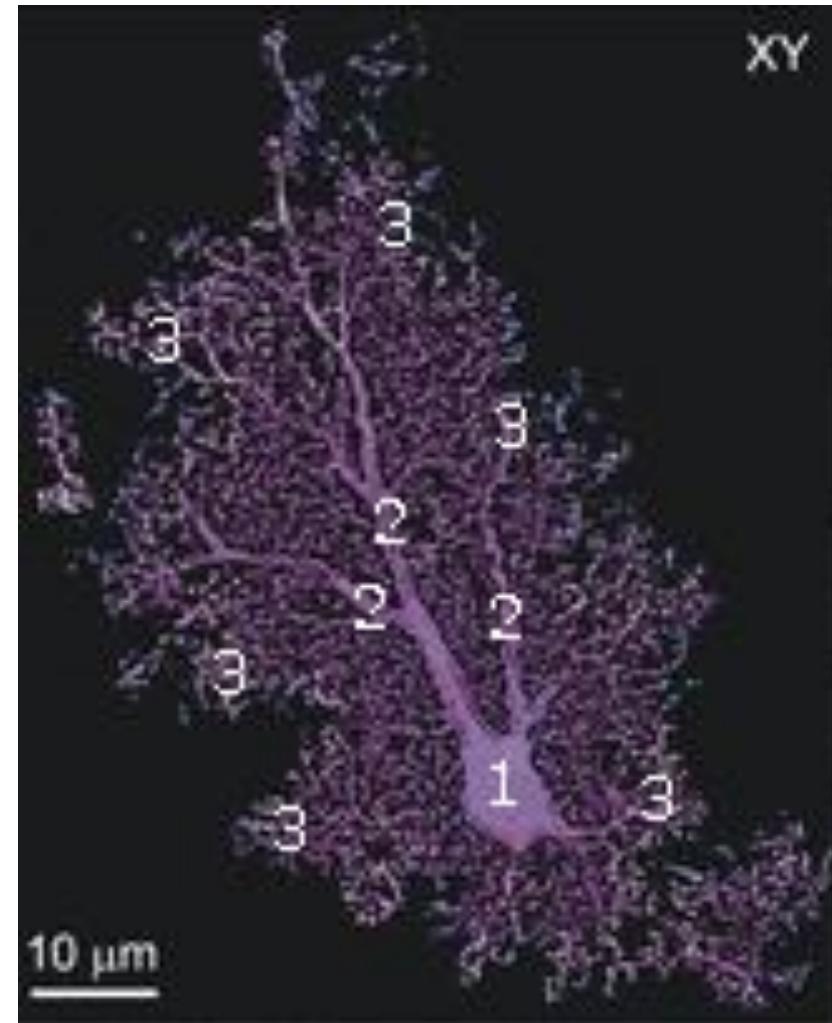
Different calcium signals within one astrocyte?



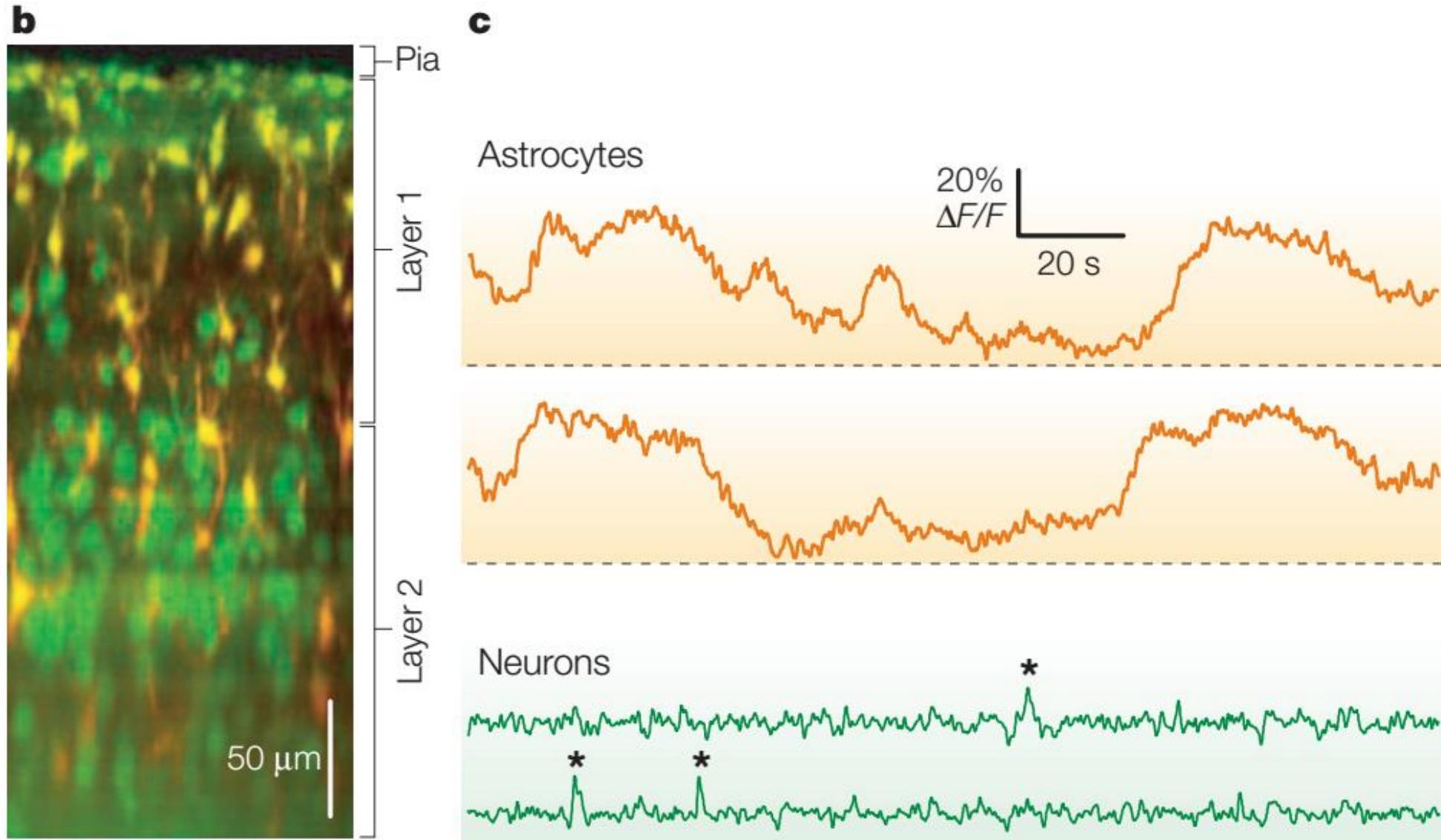
- ✓ Focal Ca^{2+} events depend on spontaneous synaptic release
- ✓ Expanded Ca^{2+} events are mostly the result of an individual action potential fired by an axon

Potentially four levels of calcium dynamics

- 1) the **thinnest processes/branchlets** form an almost nano-scale dense sponge-like network that can be imaged only with electron microscopy or specific Ca^{2+} indicators *in situ*,
- 2) the **main largest (10-20) processes** that are seen in classical microscopy with dyes or immunostaining,
- 3) the **cell body/ soma**, and
- 4) in **cellular networks**



Different time course of astrocytic Ca^{2+} and neuronal potentials



Gliotransmission?

The Journal of Neuroscience, January 3, 2018 • 38(1):3–13 • 3

Dual Perspectives

Dual Perspectives Companion Paper: Gliotransmission: Beyond Black-and-White, by Iaroslav Savtchouk and Andrea Volterra

Multiple Lines of Evidence Indicate That Gliotransmission Does Not Occur under Physiological Conditions

14 • The Journal of Neuroscience, January 3, 2018 • 38(1):14–25

 Todd A. Fiacco¹ and Ken D. McCarthy²

Dual Perspectives

Dual Perspectives Companion Paper: Multiple Lines of Evidence Indicate That Gliotransmission Does Not Occur under Physiological Conditions, by Todd A. Fiacco and Ken D. McCarthy

Gliotransmission: Beyond Black-and-White

 Iaroslav Savtchouk and  Andrea Volterra

Kerstin Lenk

Co-release of gliotransmitters?



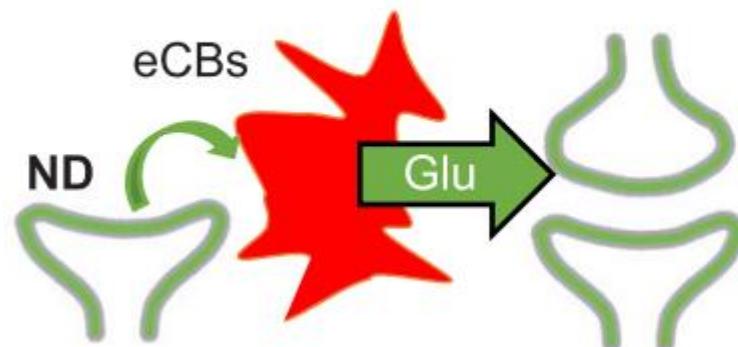
RESEARCH ARTICLE



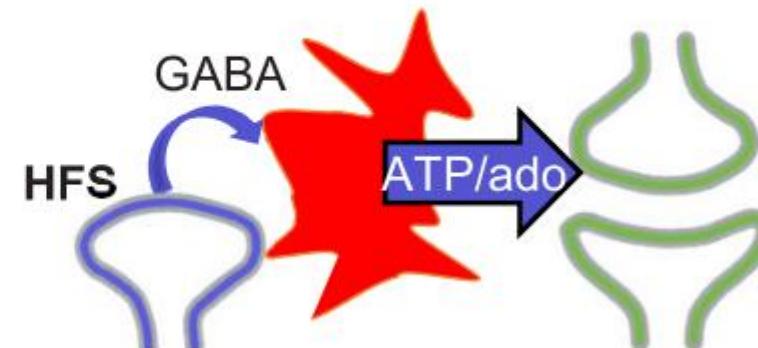
Neuronal activity determines distinct gliotransmitter release from a single astrocyte

Ana Covelo, Alfonso Araque*

eCB synaptic potentiation

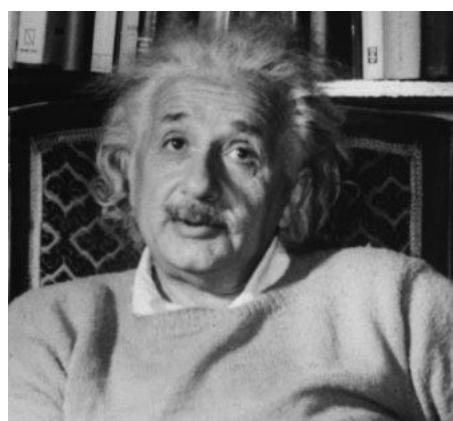


Heterosyaptic depression



Astrocyte numbers across species

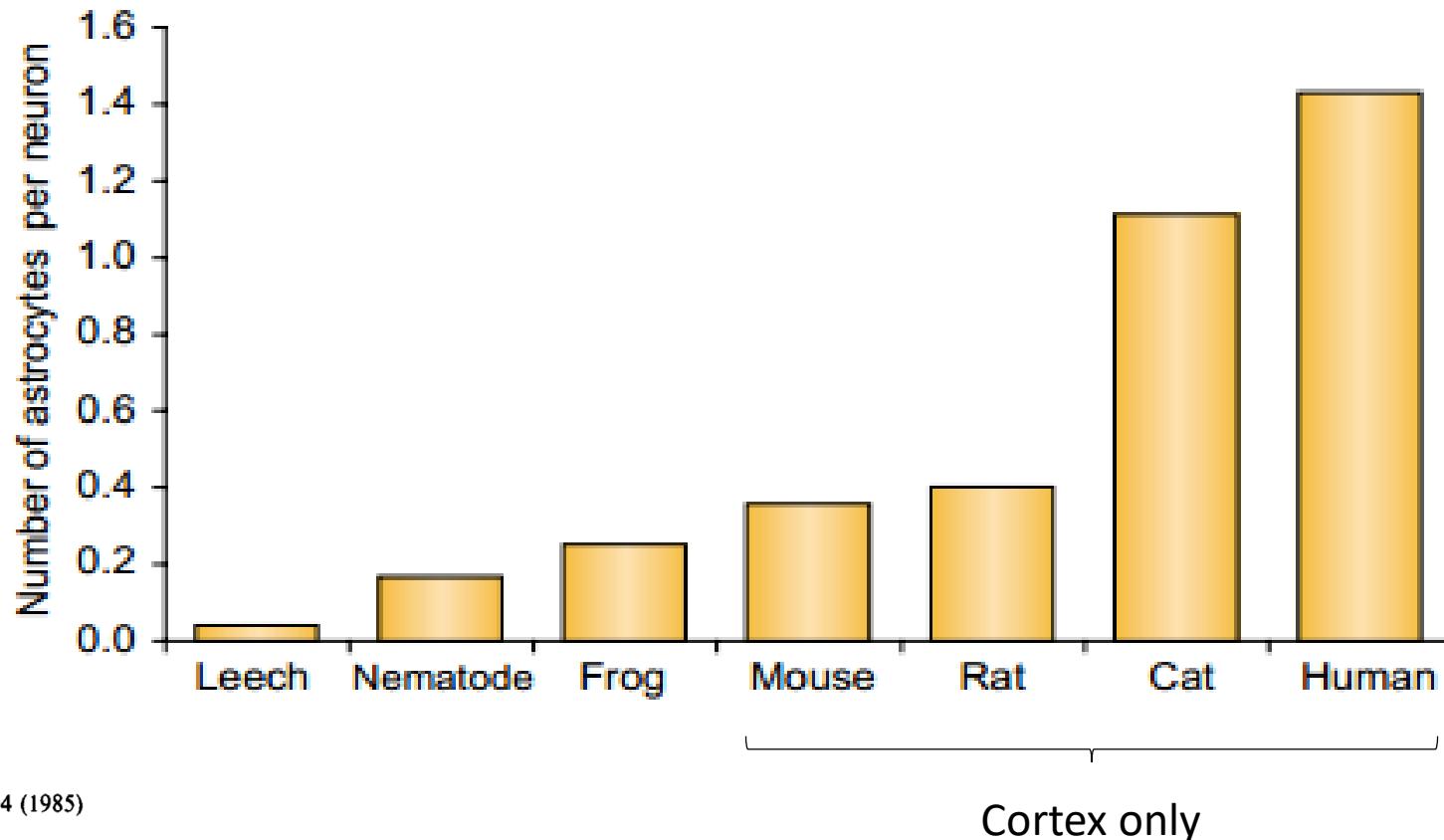
- *C. elegans* possesses 302 neurons, but only 56 glial cells (Oikonomou and Shaham 2011), astrocyte/neuron ratio is **~0.2**.
- **Rat cerebral cortex** contains a mean astrocyte/neuron ratio of **0.4** (Bass et al. 1971).
- The **whole human adult brain** has a **one-to-one ratio** (Azevedo et al. 2009).
- **Human cerebral cortex** has a **ratio of 1.4** (Friede 1954; Pelvig et al. 2008).



EXPERIMENTAL NEUROLOGY 88, 198–204 (1985)

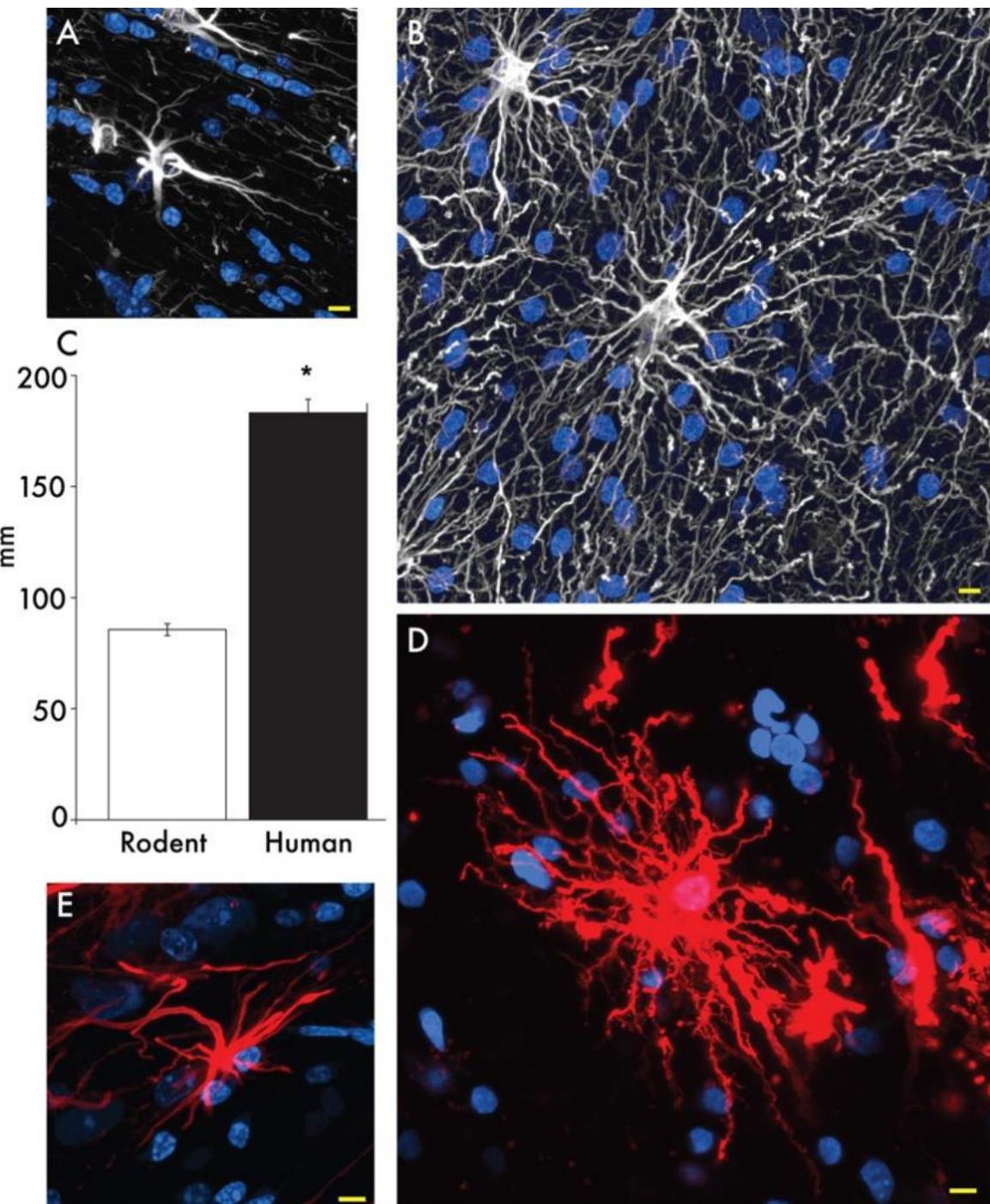
On the Brain of a Scientist: Albert Einstein

MARIAN C. DIAMOND,* ARNOLD B. SCHEIBEL,†
GREER M. MURPHY, JR.,‡ AND THOMAS HARVEY¹

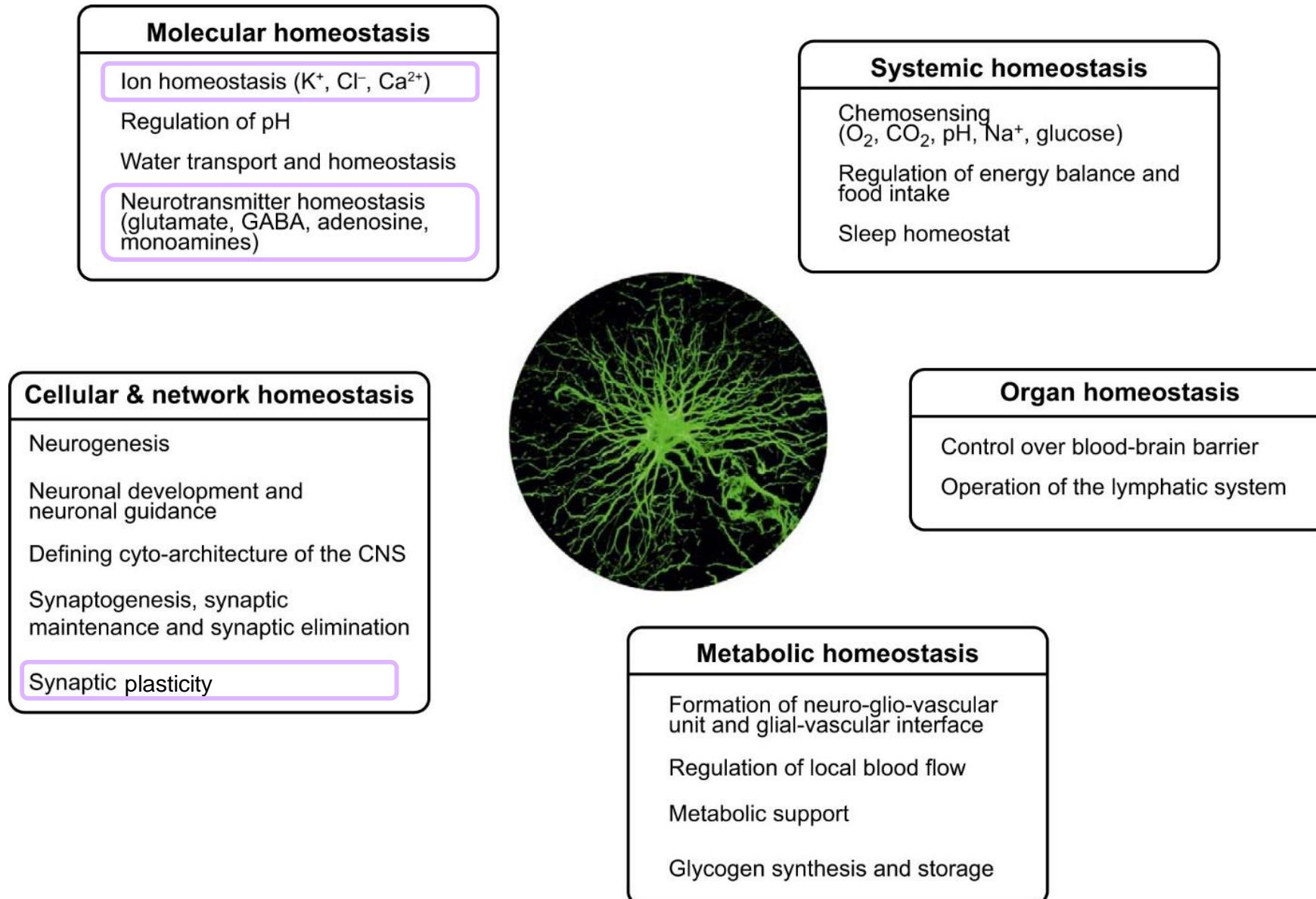


Human vs. mouse astrocytes

- A) Mouse fibrous astrocyte in white matter.
GFAP; white, sytox; blue. SB=10 μ m.
- B) Human fibrous astrocytes in white matter.
SB=10 μ m.
- C) Human fibrous astrocytes are approximately 2.14 fold larger in diameter than the rodent counterpart. *p<0.0001; t-test.
- D) Human fibrous astrocyte labeled with Dil revealing the full structure of the cell. Dil; red, Sytox; blue. SB=10 μ m.
- E) Mouse fibrous astrocyte labeled with Dil.
SB=10 μ m.



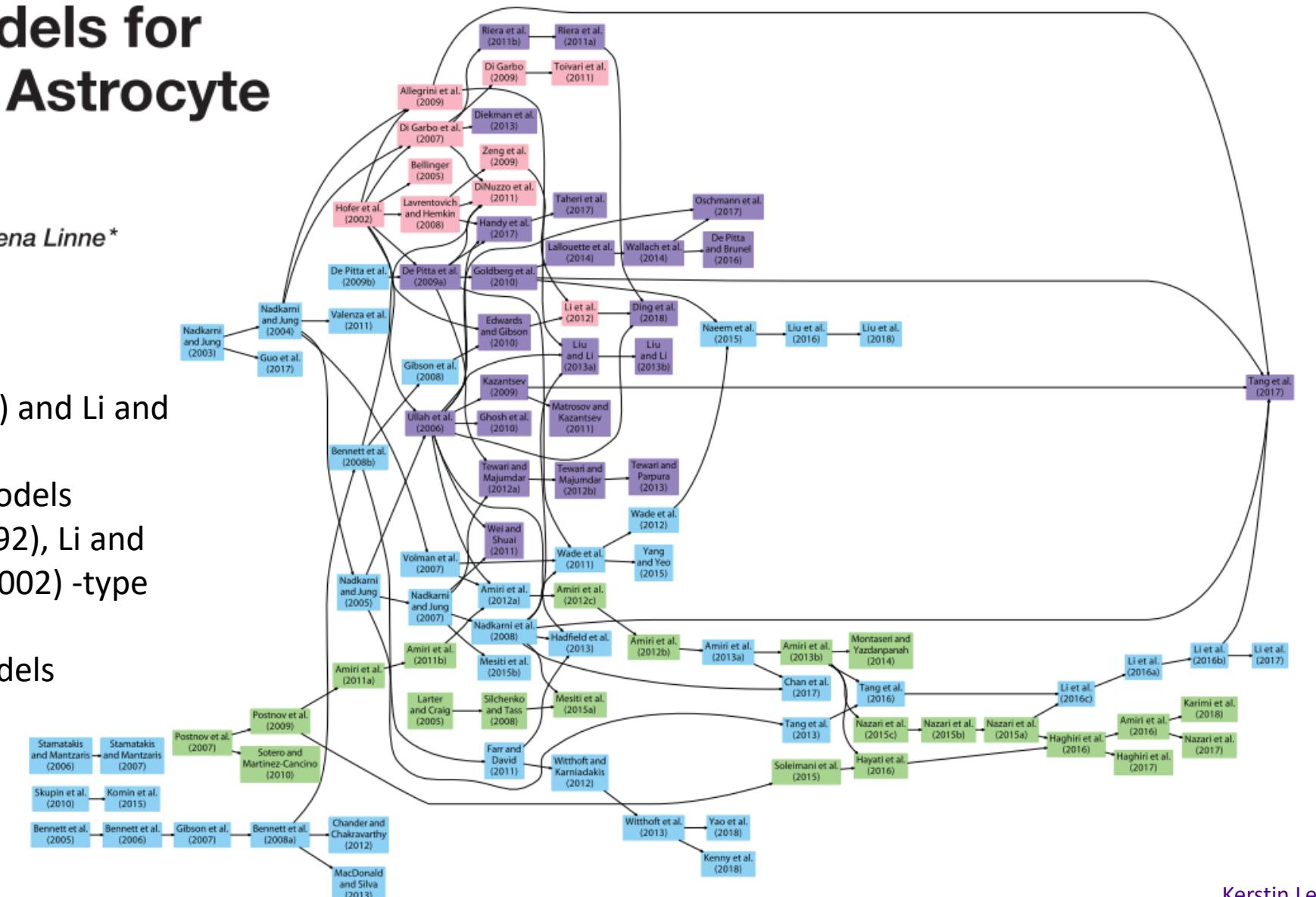
Homeostatic functions of astrocytes



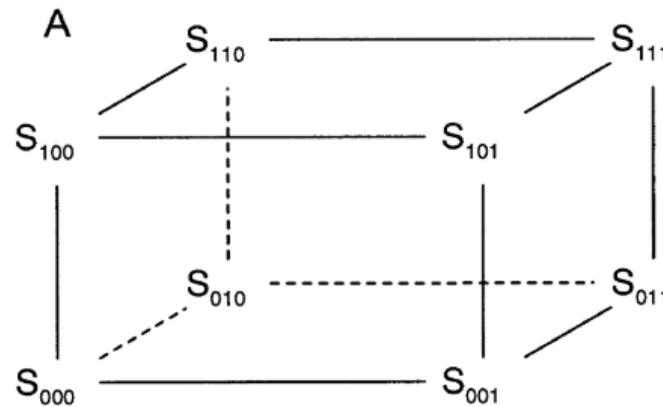
Computational Models for Calcium-Mediated Astrocyte Functions

Tiina Manninen*, Riikka Havela and Marja-Leena Linne*

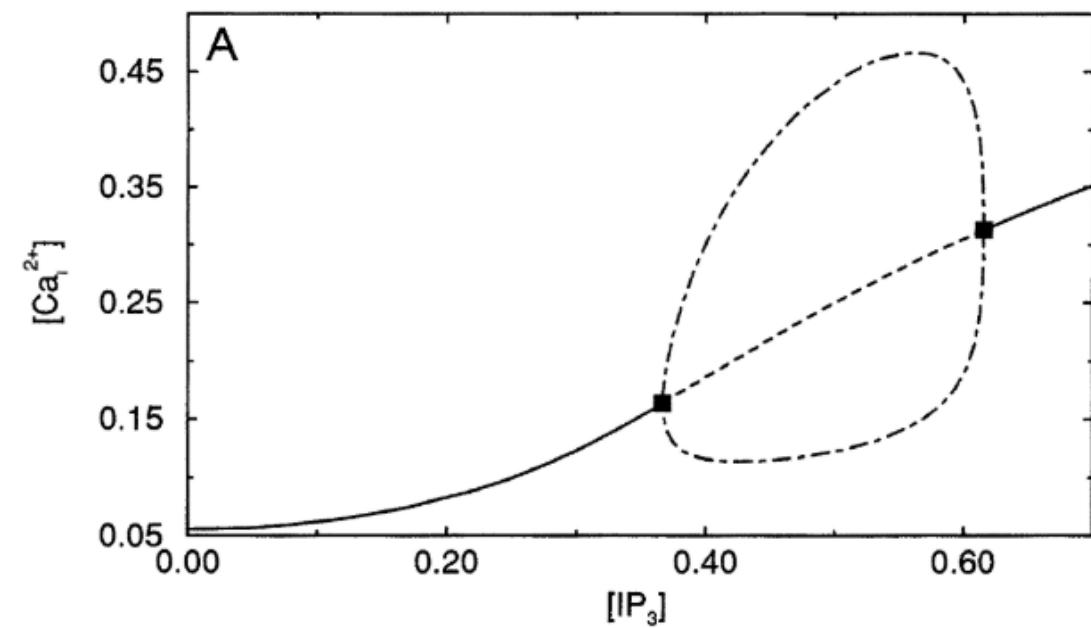
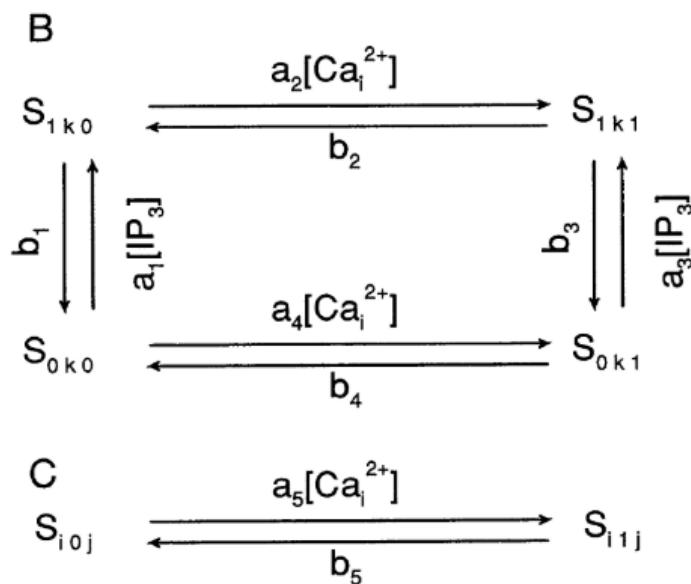
- Blue: De Young and Keizer (1992) and Li and Rinzel (1994) -type models
 - Pink: Höfer et al. (2002) -type models
 - Purple: De Young and Keizer (1992), Li and Rinzel (1994), and Höfer et al. (2002) -type models
 - Green: all the other types of models



De Young and Keizer model (1992)



State $x_{yz} = S_{xyz}$
 x = activating IP_3 binding site
 y = activating Ca^{2+} binding site
 z = inactivating Ca^{2+} binding site
 0 = unoccupied binding site
 1 = occupied binding site



**Channel is open
when 3 subunits are open:**

$$\rho = \frac{N_{Open}}{N_{Total}} = (x_{110})^3$$

Li and Rinzel model (1994)

$$\frac{dC}{dT} = -V_1 m_\infty^3 h^3 (C - C_0)$$

$$-V_2(C - C_0) - \frac{V_3 C^2}{1 + C^2}$$

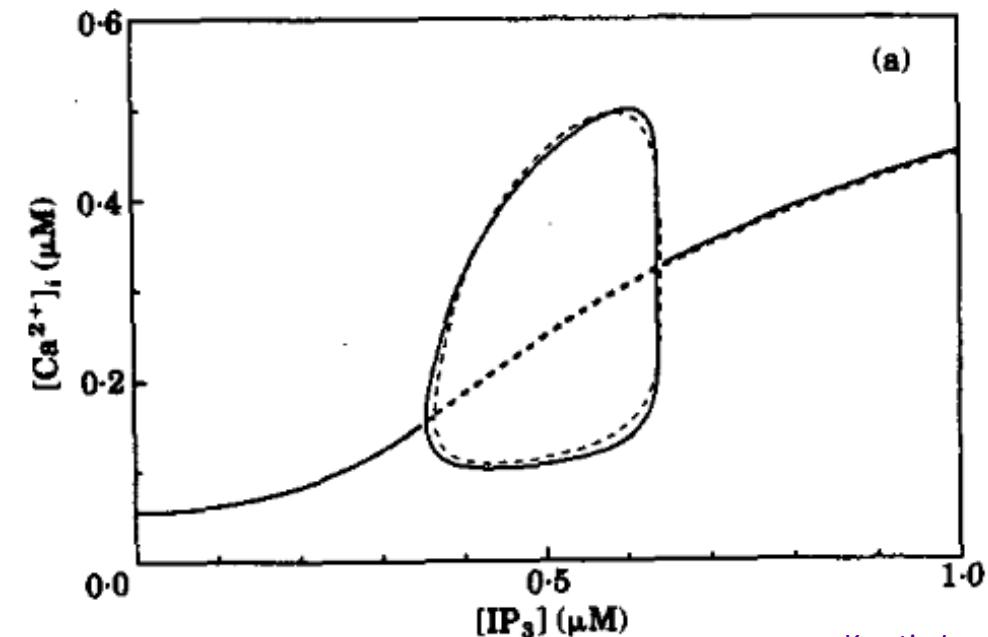
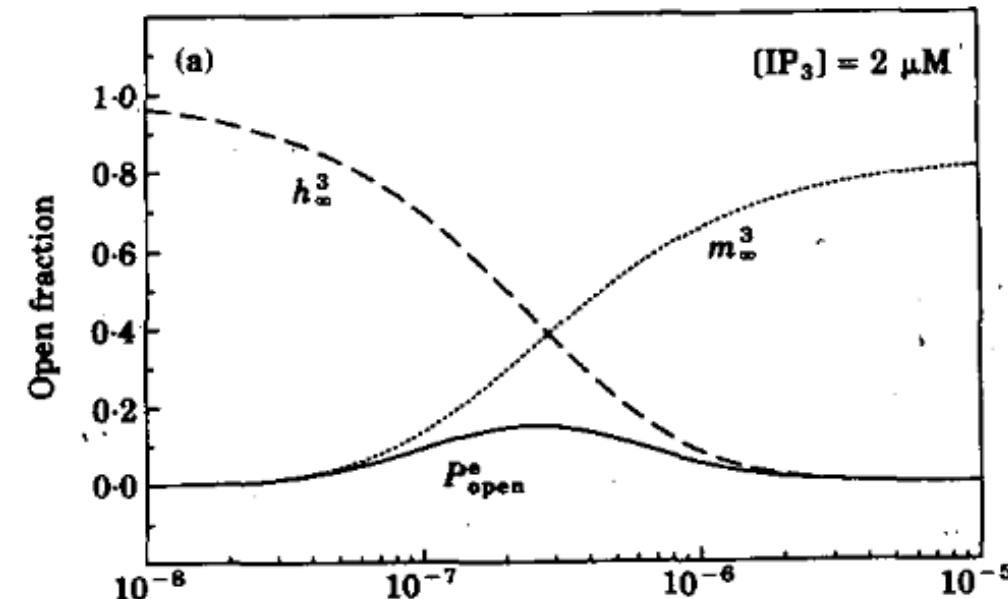
$$\frac{dh}{dT} = \frac{h_\infty - h}{\tau_h}$$

$$m_\infty = \left(\frac{[IP_3]}{[IP_3] + d_l} \right) \left(\frac{[Ca]}{[Ca] + d_s} \right)$$

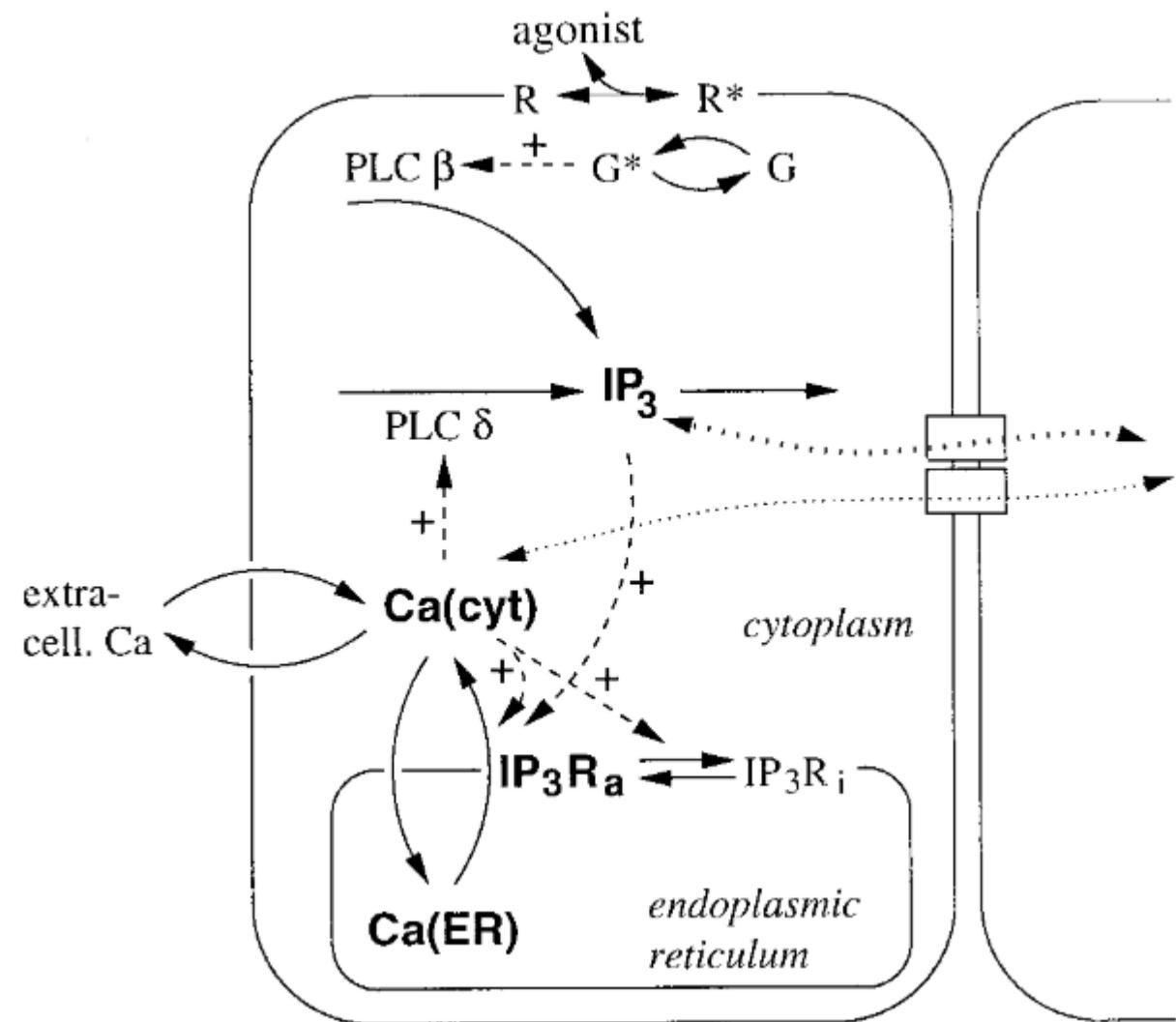
Hodkin-Huxley like equations to describe IP_3 induced Ca^{2+} release

Slow, time dependent inactivation

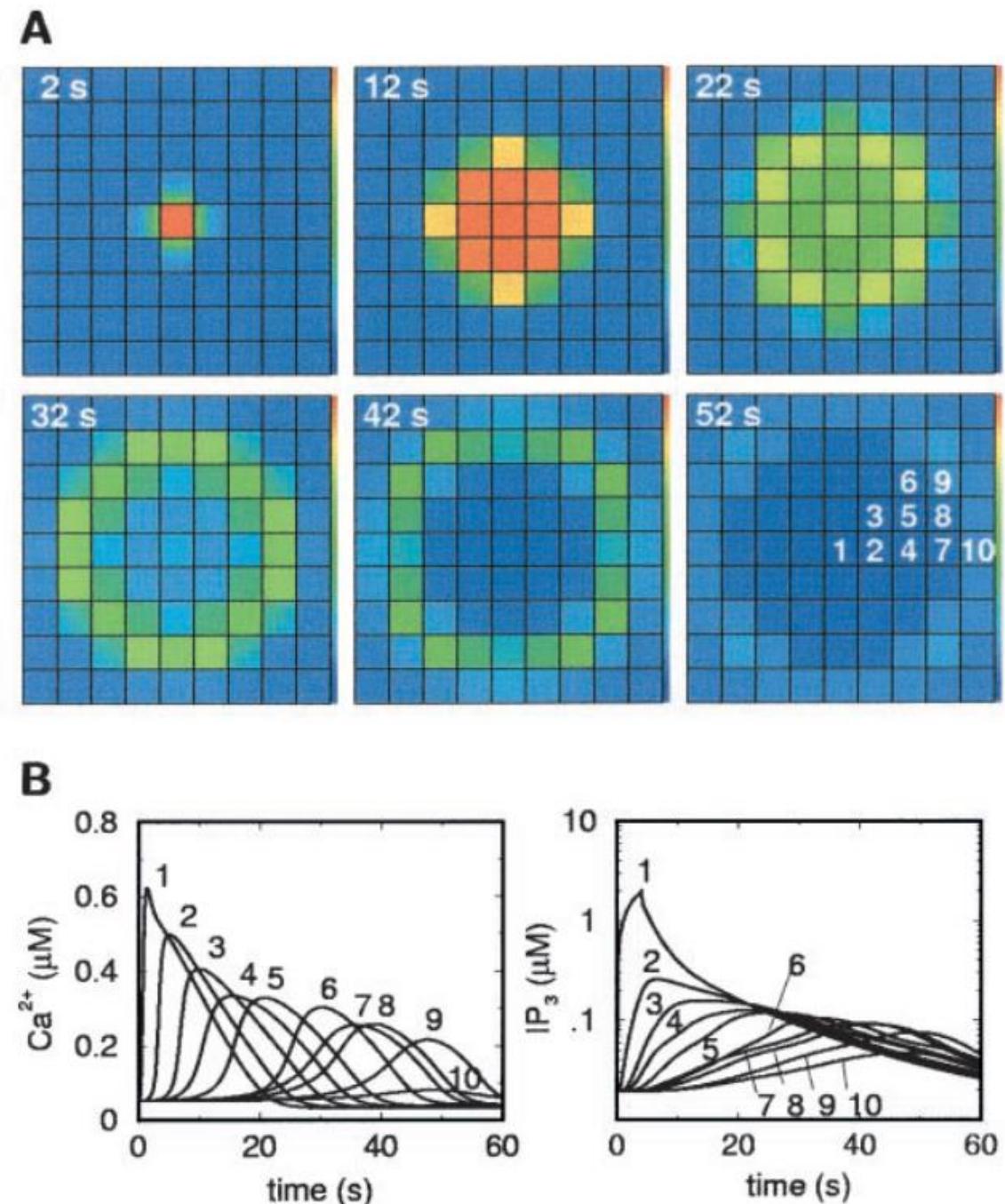
Fast, time independent activation by Ca^{2+} and IP_3



Höfer et al. model (2002)



System of balance equations for the four variables: cytosolic Ca²⁺ concentration (C), ER store Ca²⁺ concentration (S), IP₃ concentration (I), and active fraction of IP₃R (R).

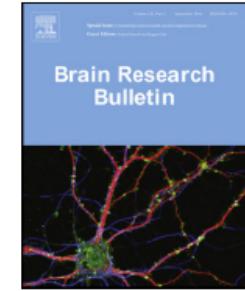




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Brain Research Bulletin

journal homepage: www.elsevier.com/locate/brainresbull



Review

From in silico astrocyte cell models to neuron-astrocyte network models: A review



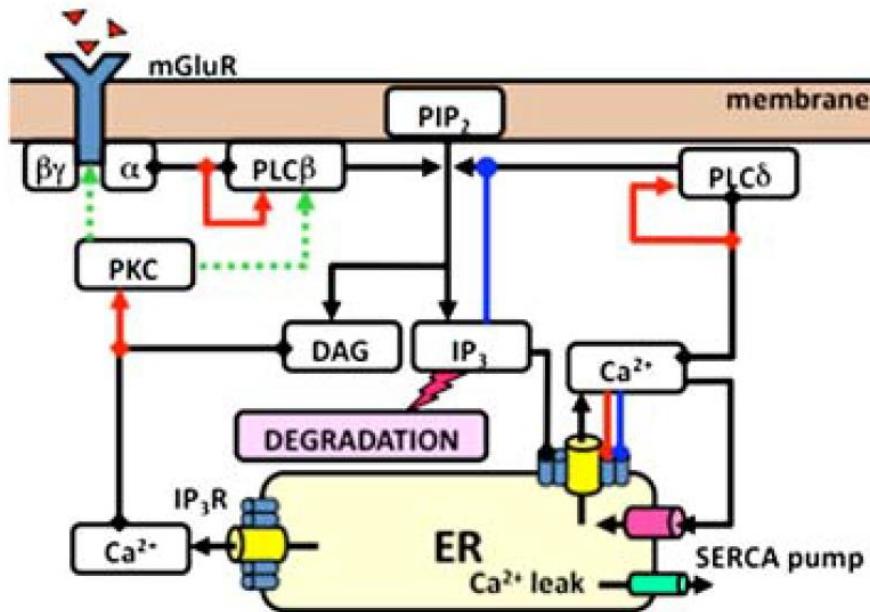
Franziska Oschmann ^{a,b}, Hugues Berry ^{c,d}, Klaus Obermayer ^{a,b}, Kerstin Lenk ^{e,*}

35 models investigated:

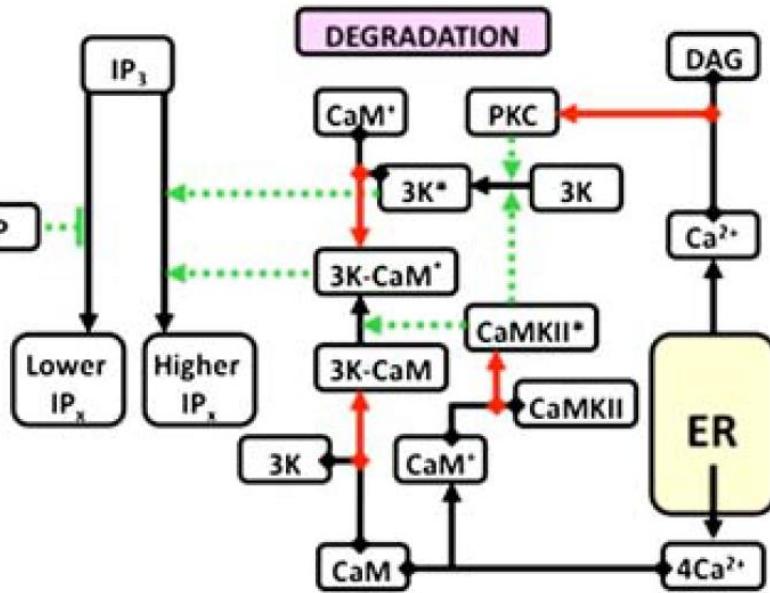
1. Single astrocytic cell models
2. Tripartite synapse models
3. Astrocyte network models
4. Neuron-astrocyte network models

Single astrocytic cell model by De Pittà et al., 2009

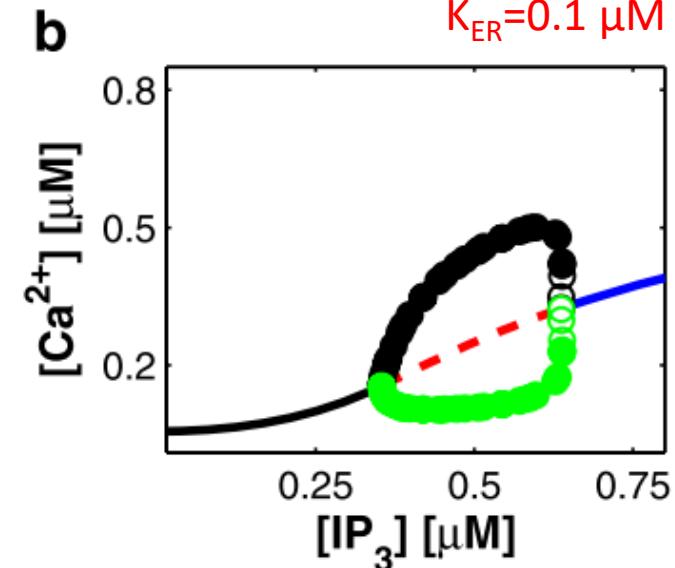
a



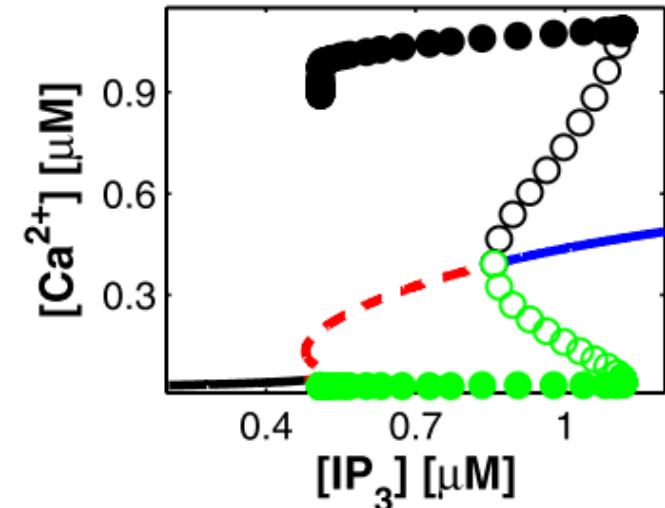
b



b



e

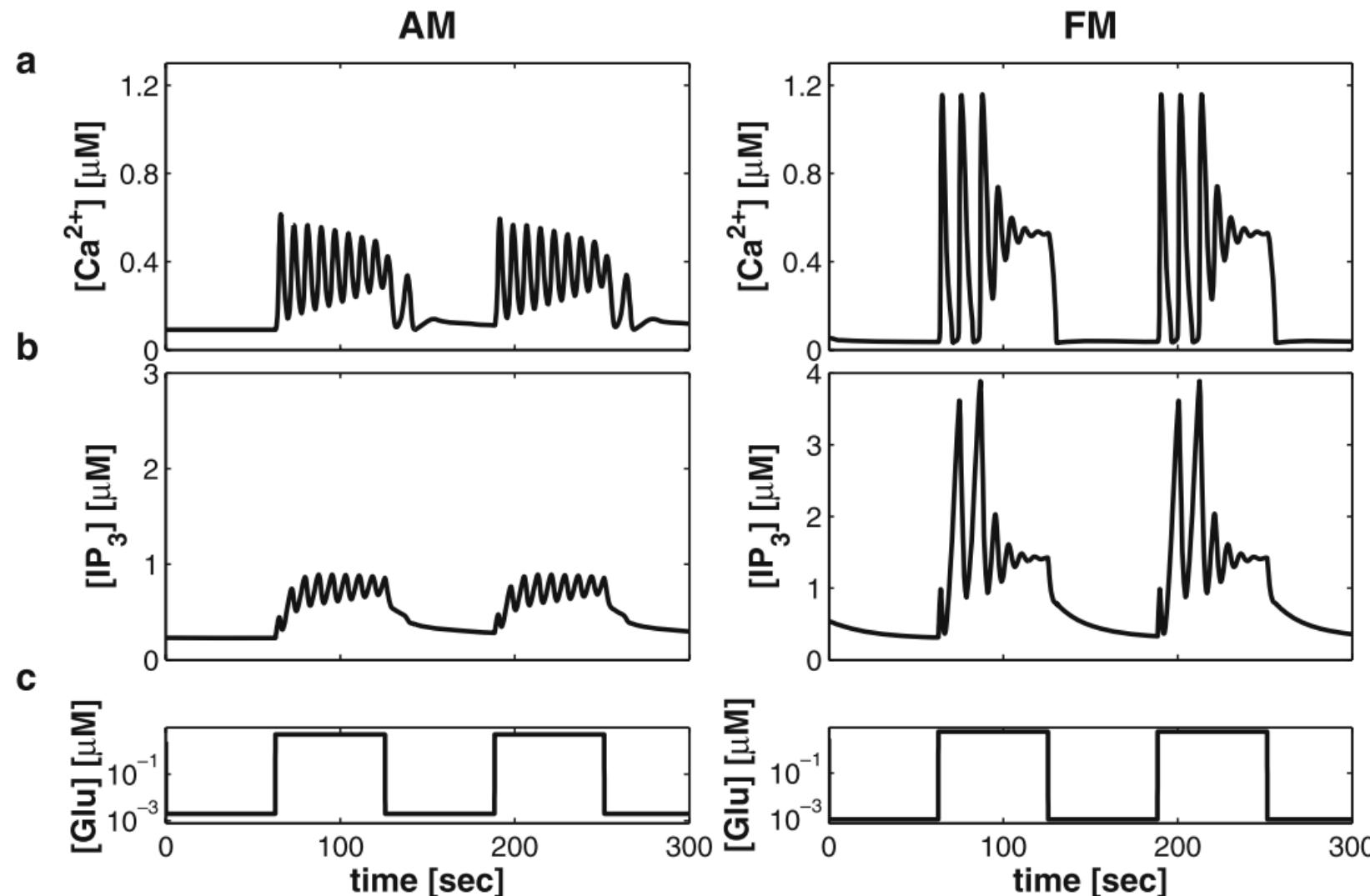


- Based on De Young & Keizer, Li-Rinzel and Höfer et al. models
- Three pathways: glutamate induced IP_3 , Ca^{2+} induced Ca^{2+} activation, and reduction through IP_3 degradation

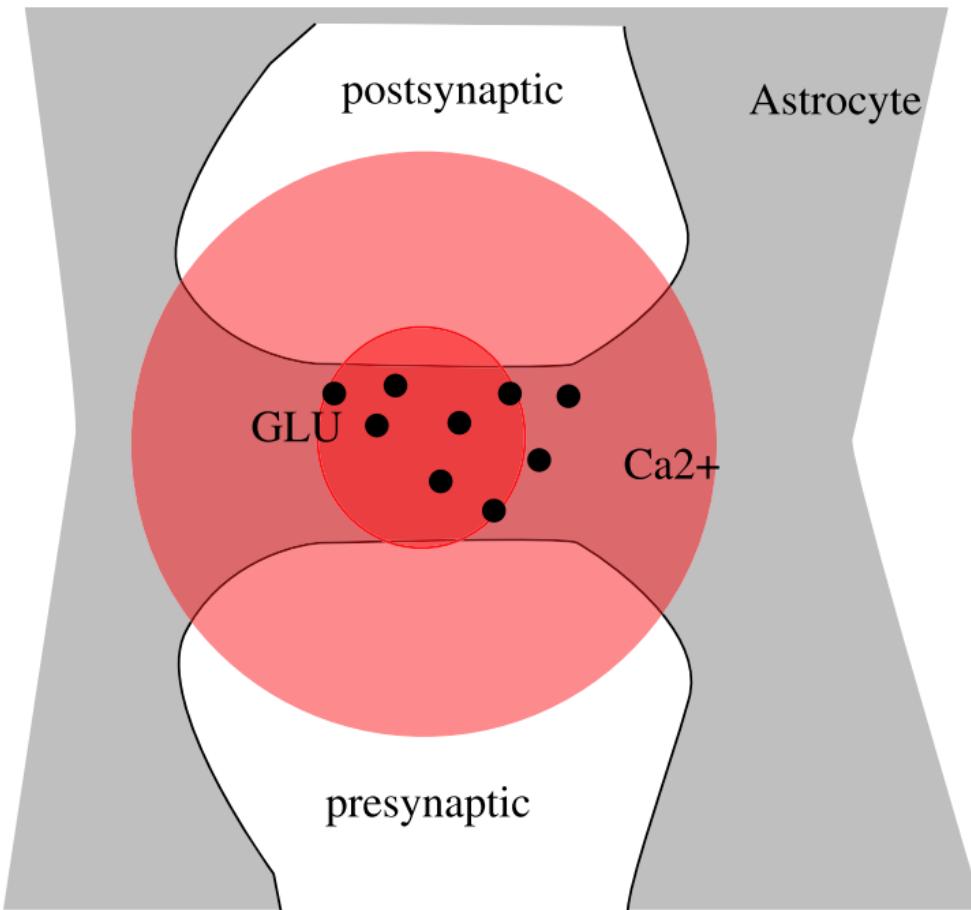
K_{ER} is the SERCA Ca^{2+} affinity

Kerstin Lenk

Single astrocytic cell model by De Pittà et al., 2009

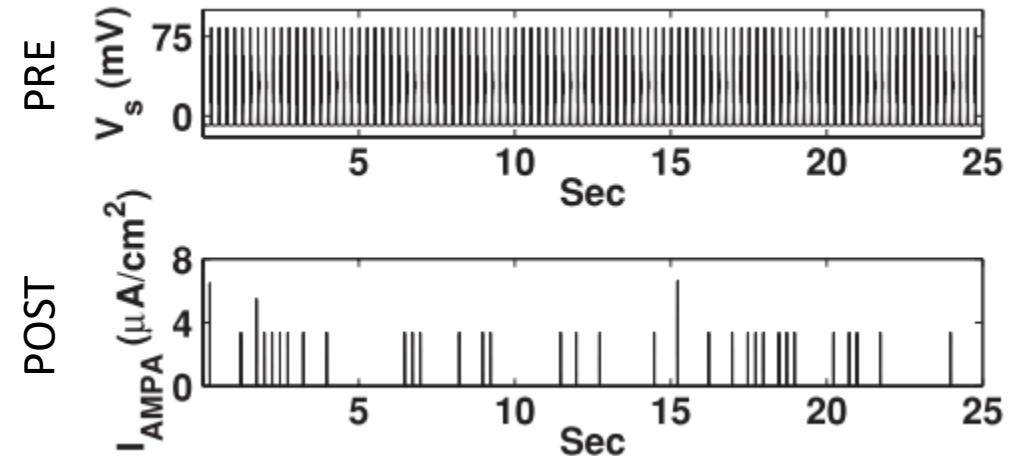


Tripartite synapse model by Nadkarni and Jung, 2007

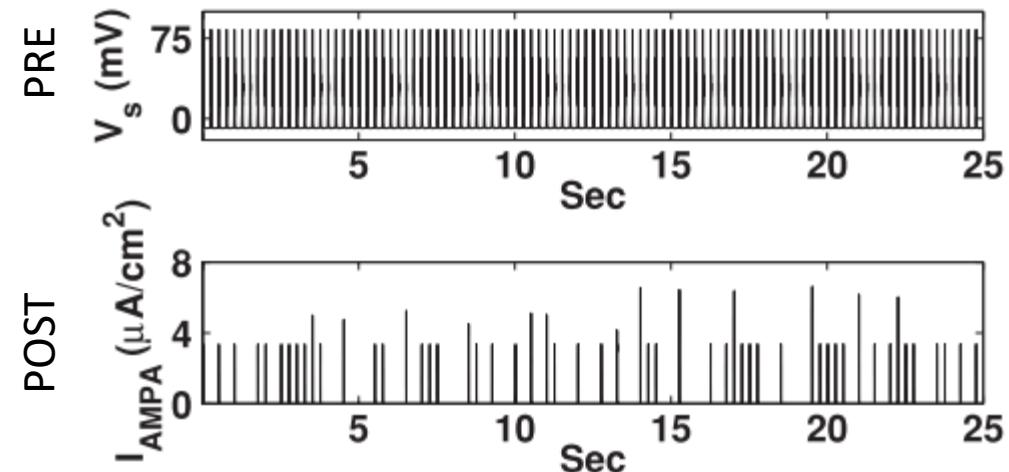


De Young & Keizer and Li and Rinzel -type model
Neuron-astrocyte interaction

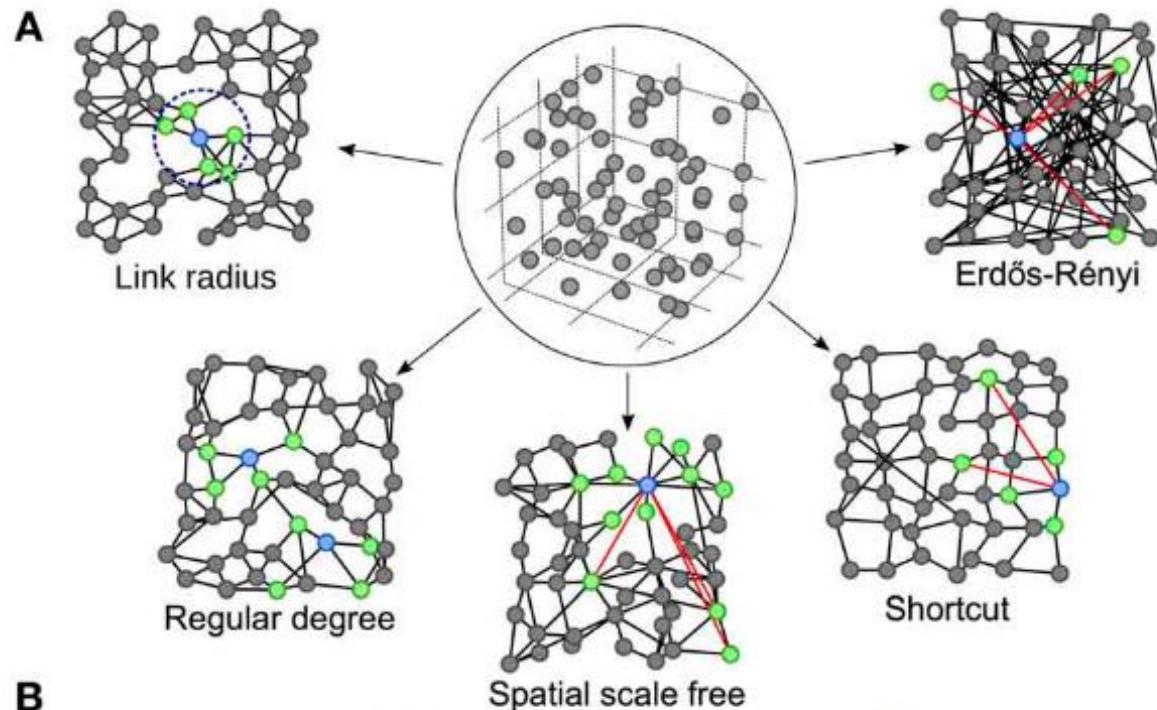
Without astrocyte:



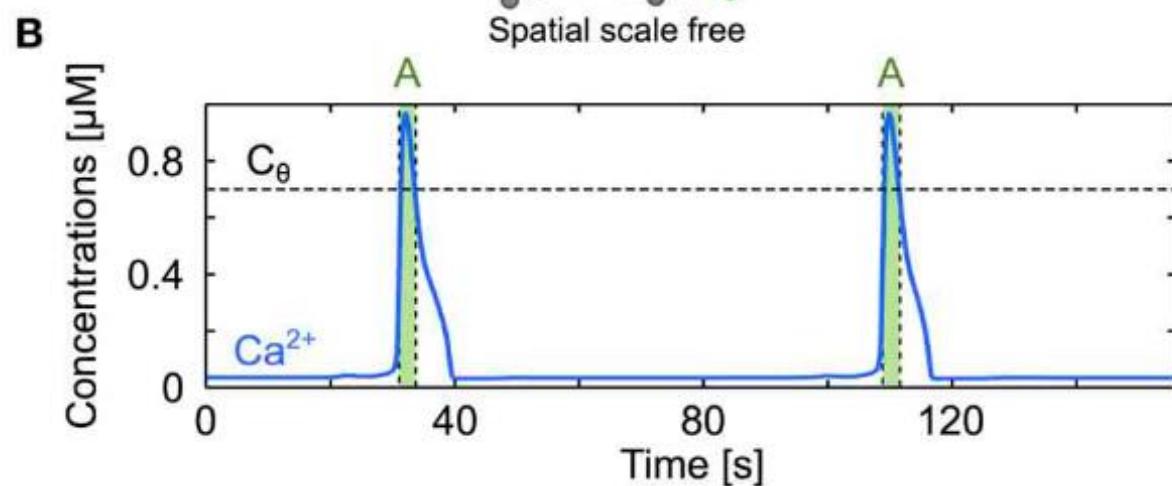
With astrocyte:



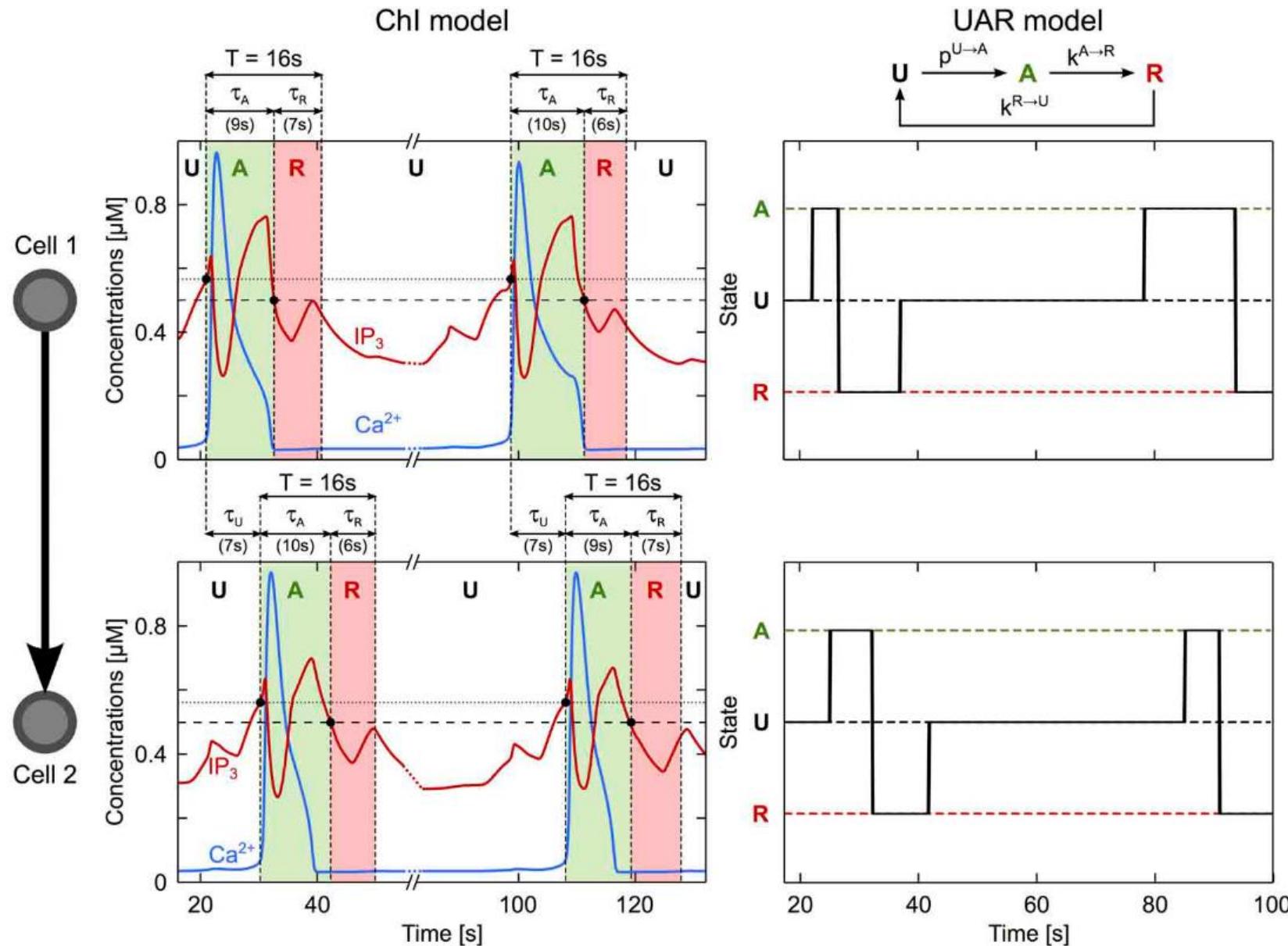
Astrocyte network model by Lallouette et al., 2014



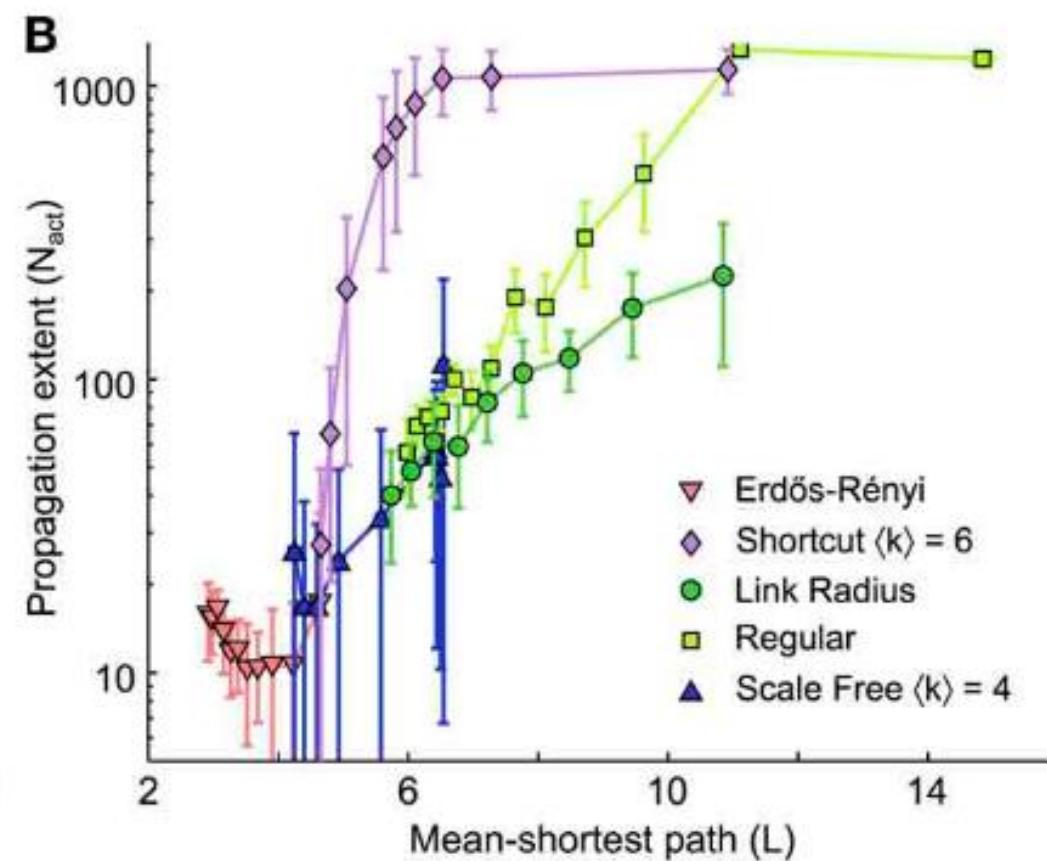
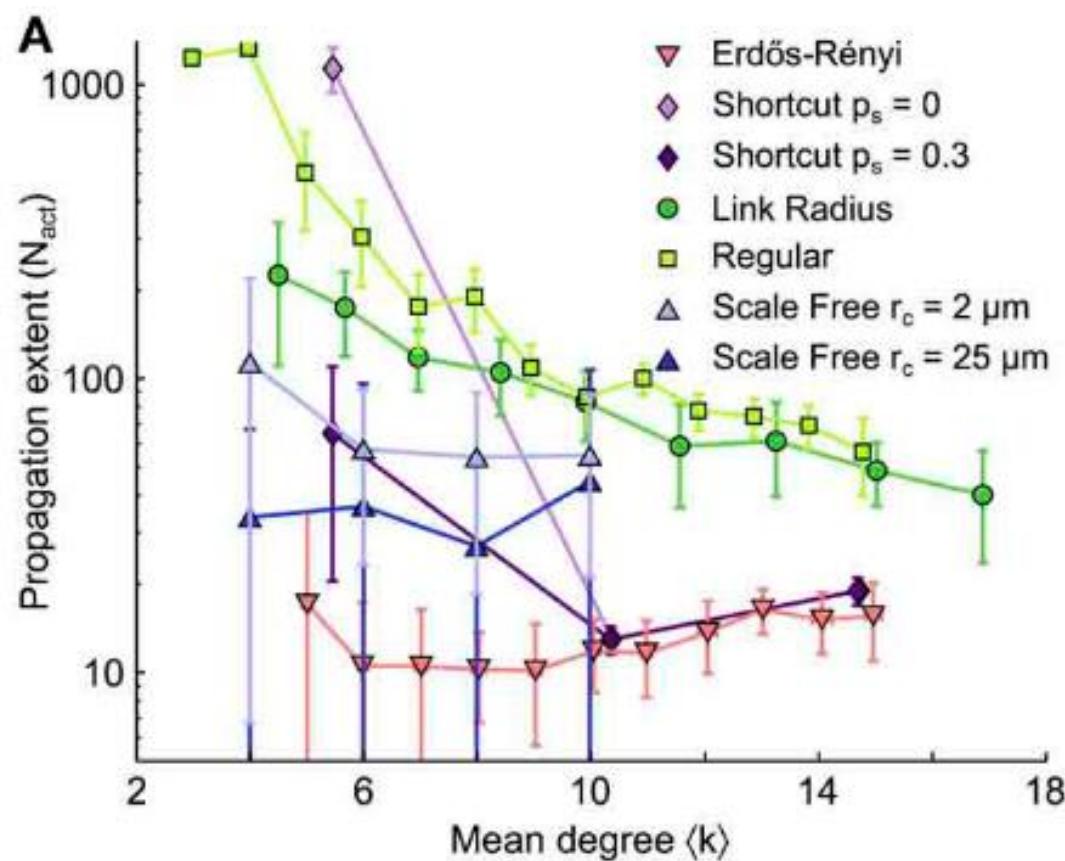
Based on De Pittà et al., 2009 and 2012



Astrocyte network model by Lallouette et al., 2014



Astrocyte network model by Lallouette et al., 2014



Neuron-astrocyte network model



A computational model of interactions between neuron and astrocyte networks: role of astrocytes on stability of the neuronal firing rate

Kerstin Lenk^{1,†,*}, Eero Satuvuori^{1,2,3,4,†}, Jules Lallouette^{5,6}, Antonio Ladrón-de-Guevara¹,
Hugues Berry^{5,6}, Jari AK Hyttinen¹

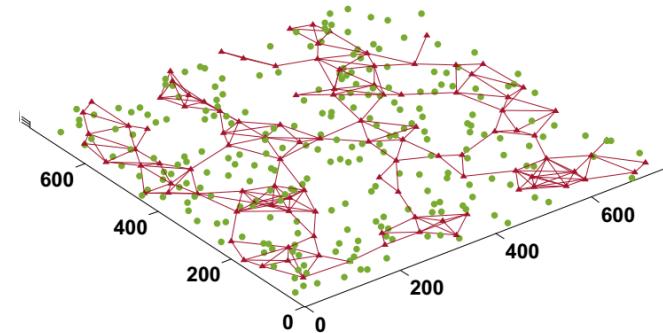
(submitted)

Motivation

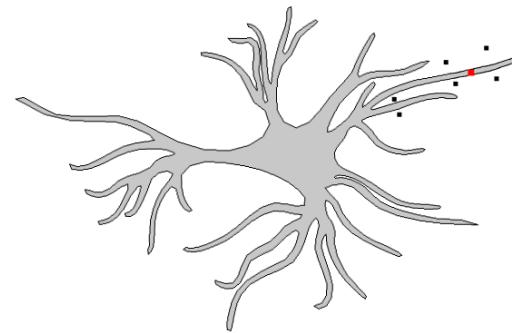
- Astrocytes may influence neuronal network function → What are the mechanism/ pathways? How do astrocytes change the neuronal activity and vice versa?
- How are the astrocytic calcium dynamics influenced by morphology and topology?
- Role and functions of astrocytes in epilepsy and Alzheimer's?



Neuron-astrocyte network model

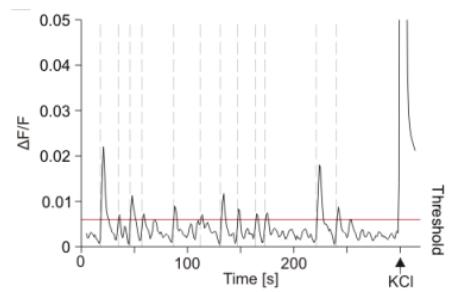
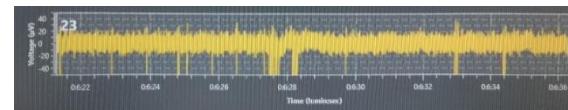
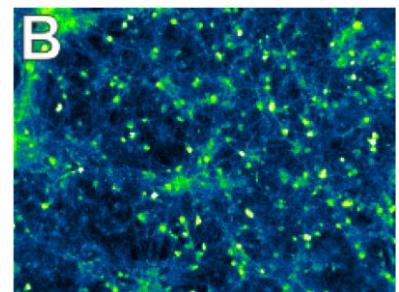
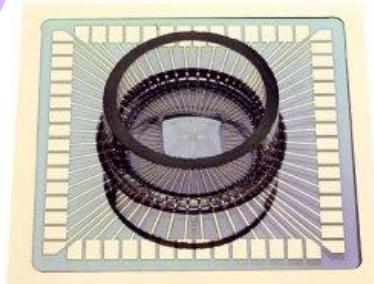


Single cell astrocyte model



Our modeling approach

Experiments



RESEARCH ARTICLE
Spatial separation of two different pathways accounting for the generation of calcium signals in astrocytes

Francesca Dostert¹*, Konstantinos Mergenlis², Evelyn Angelaki³

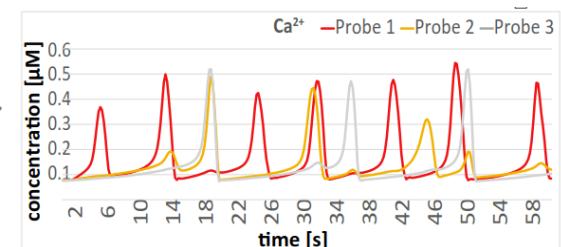
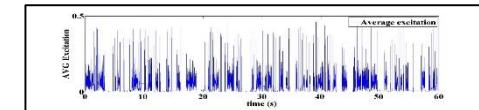
From **1** Department of Cell Biology, University of California, San Francisco, San Francisco, California, United States of America, **2** Department of Cell Biology, University of California, San Francisco, San Francisco, California, United States of America, **3** Department of Otolaryngology, University of California, San Francisco, San Francisco, California, United States of America

E-mail: angelaki@otolaryngology.ucsf.edu

Abstract
Astrocytes are a primary source of calcium (Ca^{2+}) signals in response to increasing information levels during synaptic transmission. The generation of Ca^{2+} signals is mainly attributed to Ca^{2+} currents because these currents are elicited by an increase in the concentration of extracellular calcium ($[Ca^{2+}]_o$). However, the mechanism underlying the generation of Ca^{2+} signals in the activity of the glial membrane (cellular) calcium channels is not fully understood. We used a combination of patch-clamp recordings and calcium imaging to study the generation of Ca^{2+} signals in two different astrocytic compartments: the soma and the processes. Our results show that the generation of Ca^{2+} signals in the soma is mainly produced by Ca^{2+} release from internal Ca^{2+} stores (cellular-dependent pathway), whereas the generation of Ca^{2+} signals in the processes is mainly produced by Ca^{2+} entry into the plasma membrane (cellular-independent pathway). This separation is supported by the fact that the generation of Ca^{2+} signals in the soma is mainly produced by Ca^{2+} entry from the extracellular space, whereas the generation of Ca^{2+} signals in the processes is mainly produced by Ca^{2+} release from the surface membrane of the synapses. We conclude that the spatial separation of the two different pathways accounting for the generation of Ca^{2+} signals in the soma and the processes is mainly produced by the different mechanisms underlying the generation of Ca^{2+} signals in the two compartments. The model allows to study the balance of Ca^{2+} responses during the different activity levels and to predict the effect of the different factors that modulate the generation of Ca^{2+} signals in the soma and the processes. This model will be useful for the understanding of the impact of chronic diseases on the interaction of health pathways and on the Ca^{2+} signaling.

Author summary
Astrocytes are considered as active partners in neural information processing, because they receive and process information from the environment and the brain. New visual information influences below the generation of Ca^{2+} signals in astrocytes. The

Computational models



$$\frac{d[Ca^{2+}]_i}{dt} = \frac{A}{F \cdot Vol} \cdot I_{NCX} + \frac{A \cdot \sqrt{ratio_{ER}}}{F \cdot Vol} \cdot (I_{IP_3R} - I_{SERCA} + I_{CaLeak})$$

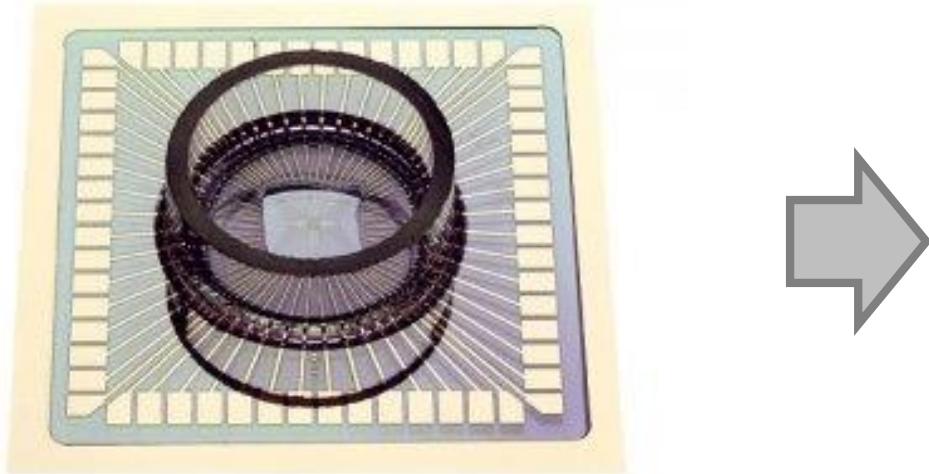
Table 1. Initial values of the ion concentrations, the membrane voltage, IP_3 and the fraction of the activated IP_3 receptor channels. For the calculation of $[Ca^{2+}]_{ER}$, $[IP_3]$ and h see Model section Model parameters.

Parameter	Value	Source
$[Ca^{2+}]_i$	0.073 μM	[23]
$[Ca^{2+}]_{ER}$	25 μM	see text
$[Ca^{2+}]_o$	1800 μM	[18]
$[Na^+]$	15 mM	[19]
$[Na^+]_o$	145 mM	[19]
$[K^+]$	100 mM	[19]
$[K^+]_o$	3 mM	[19]
V	-85 mV	[24]
$[P_0]$	0.15659 μM	see text
h	0.7892	see text

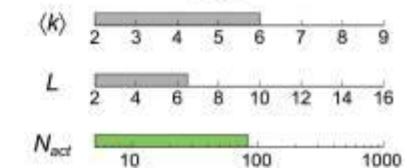
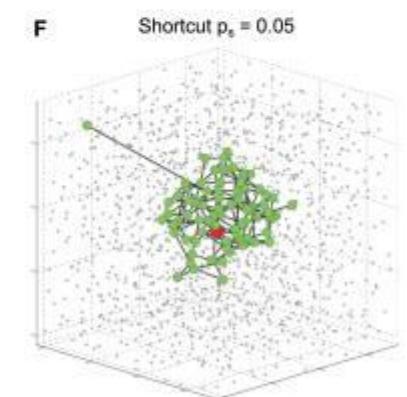
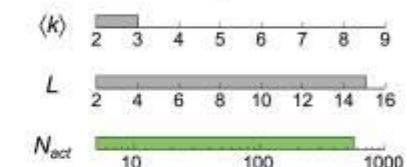
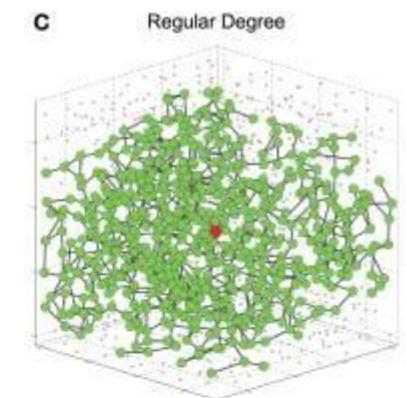
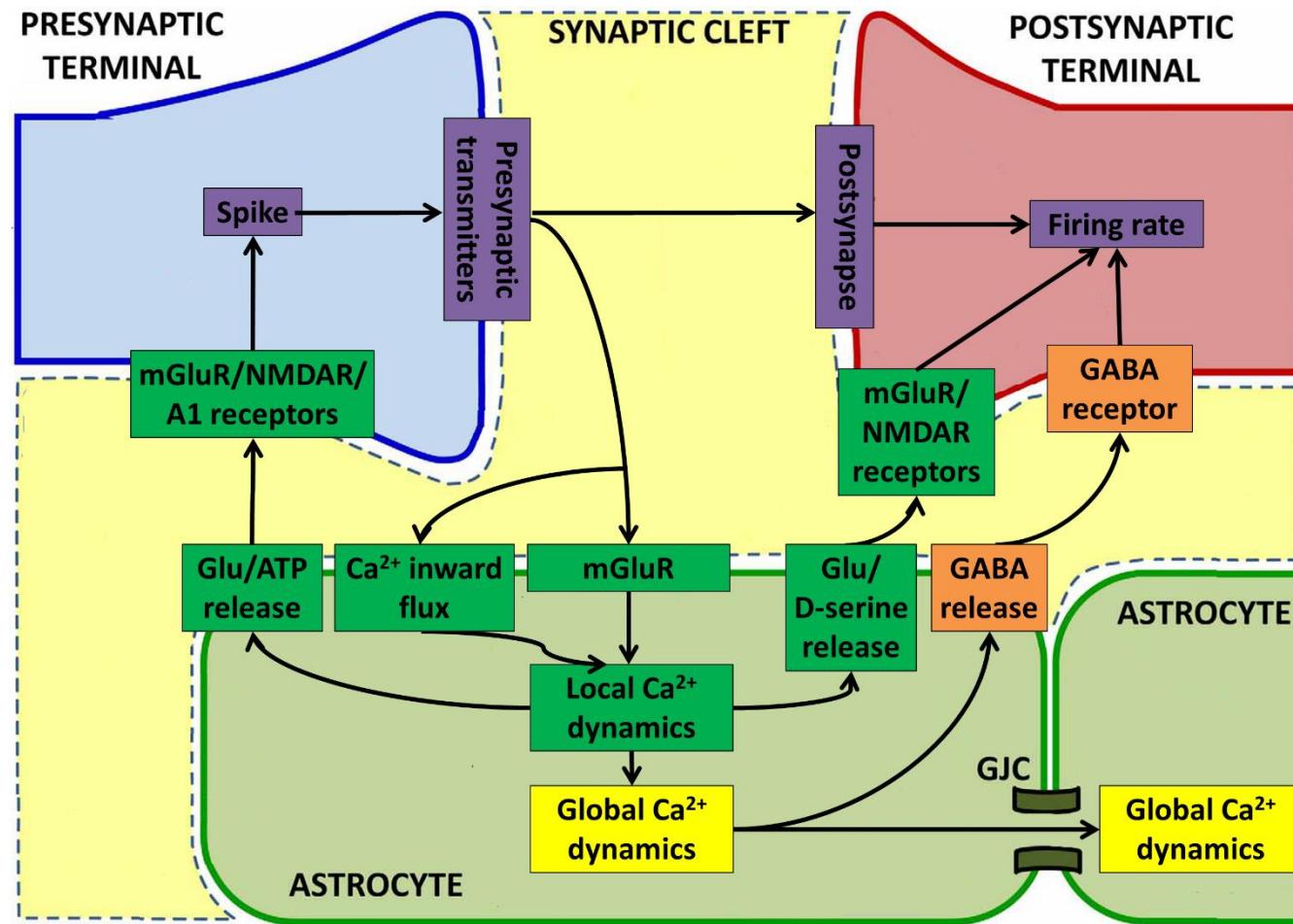
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V	-85 mV	[24]
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h	0.7892	see text

Neuron-astrocyte network model



Model with presynaptic and astrocytic calcium dynamics



Oschmann et al., Brain Res Bull. 2017

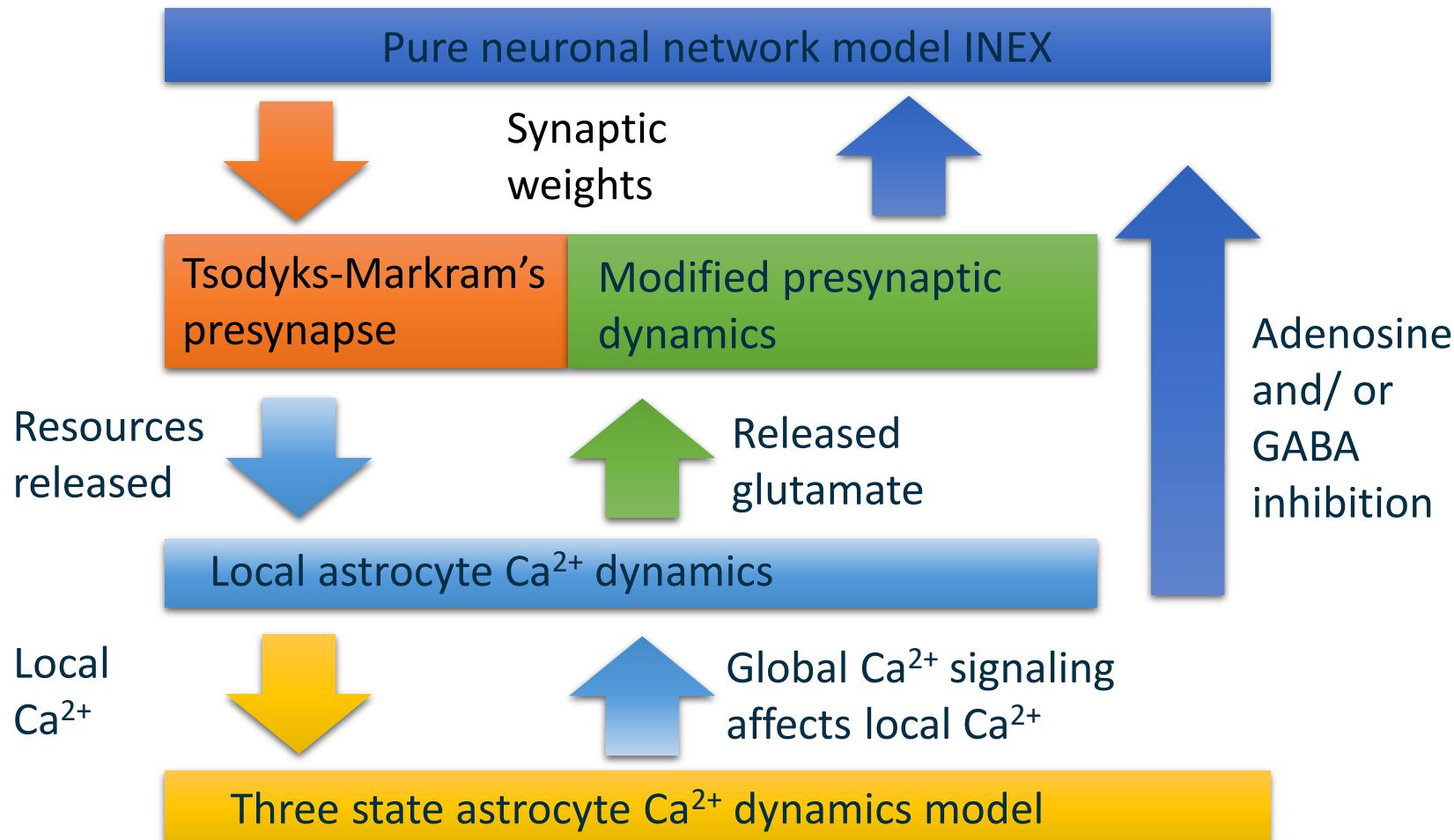
De Pittà et al., PLoS Comput Biol 2011

De Pittà et al., Frontiers in Comput Neurosci 2012

Lallouette et al., Front. Comput Neurosci 2014

Kerstin Lenk

Neuron-astrocyte network model INEXA



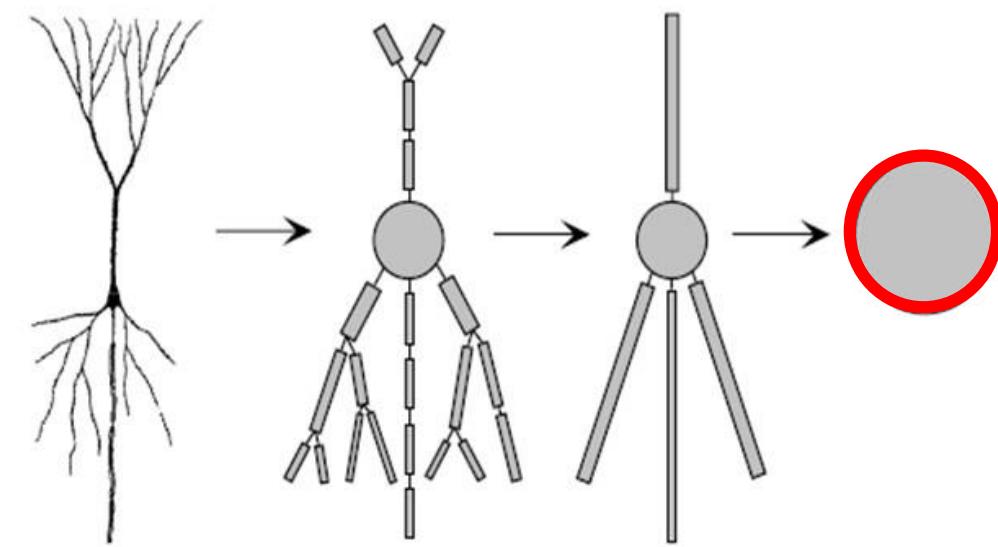
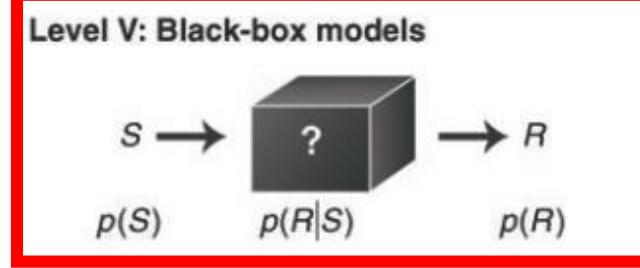
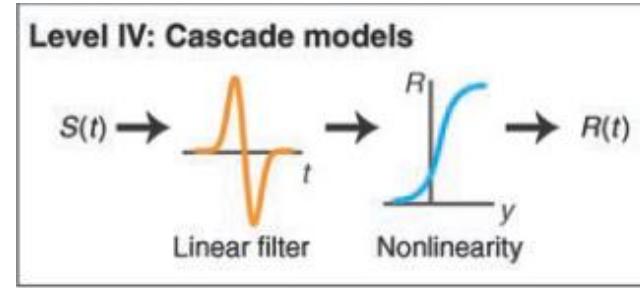
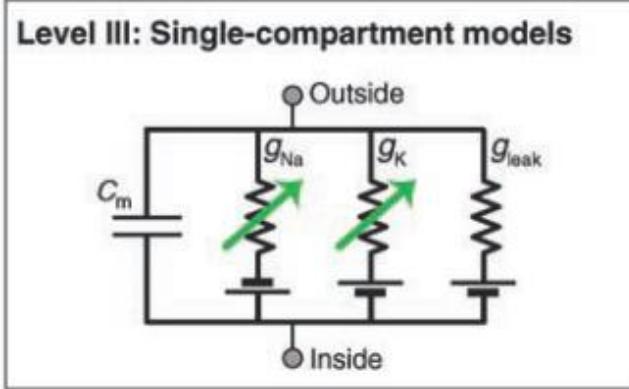
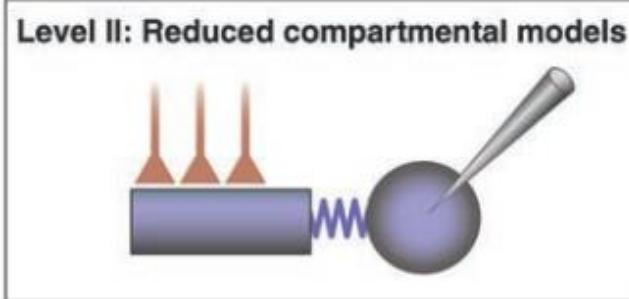
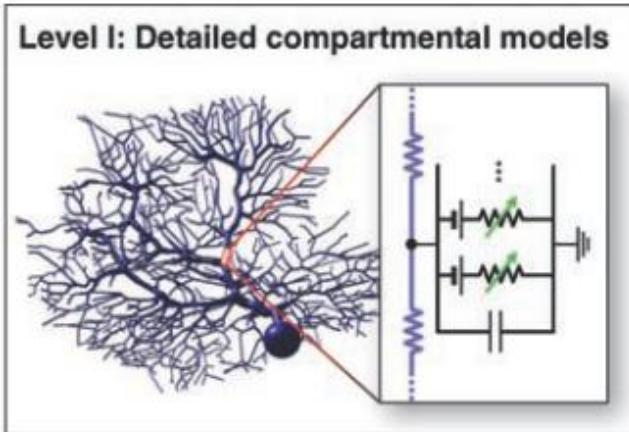
Lenk, 2011

De Pittà et al., PLoS Comput. Biol. 2011

De Pittà et al., Frontiers in Comput. Neurosci. 2012

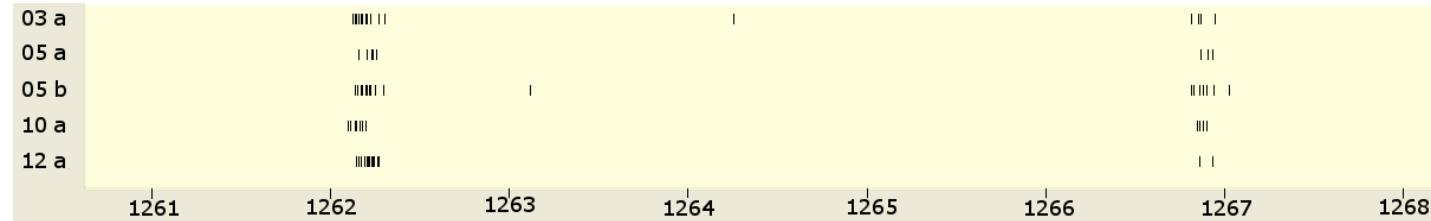
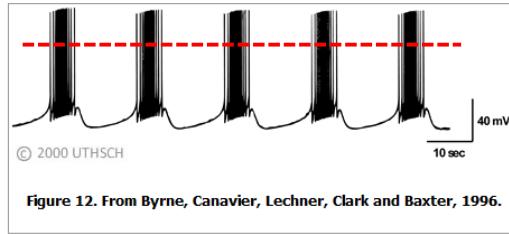
Lallouette et al., Front. Comput. Neurosci. 2014

We start from the neuronal network



Relevant model characteristics

Target: Neuronal model for simulating neuronal activity as observed in *in vitro* experiments with MEAs

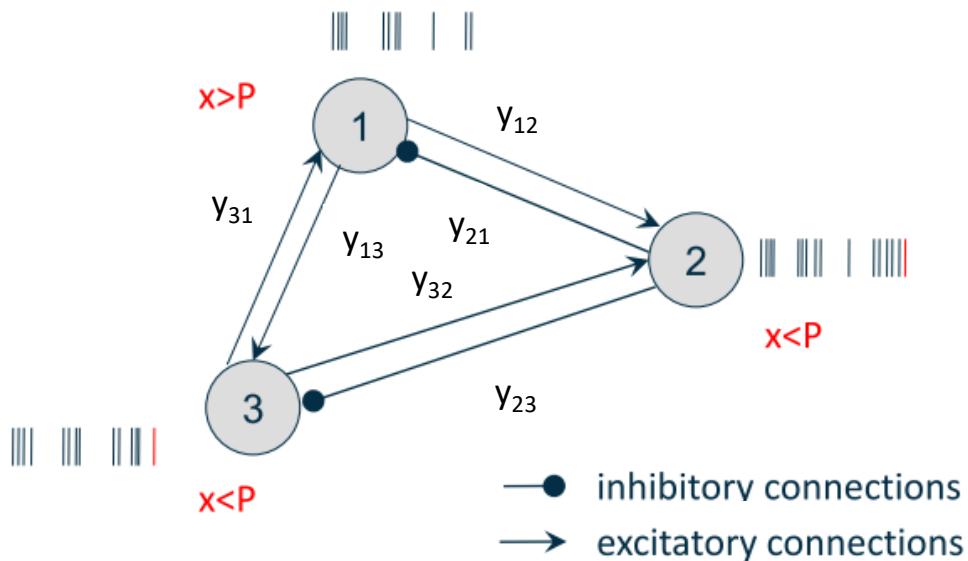
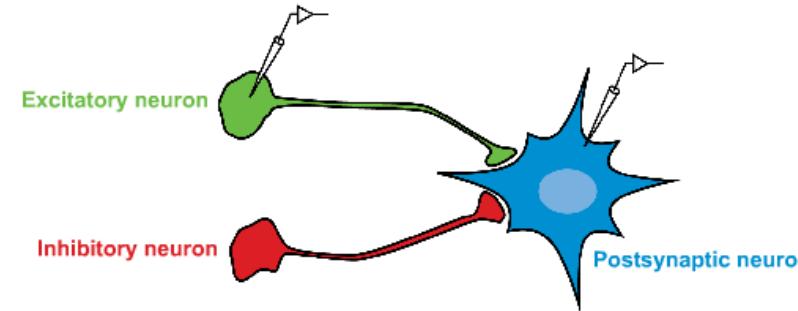


Following characteristics:

- Simulation of a whole neuronal network
- Bursts
- Spontaneous activity
- Noise
- Simple model with a few parameters

INEX model consists of Poisson neurons

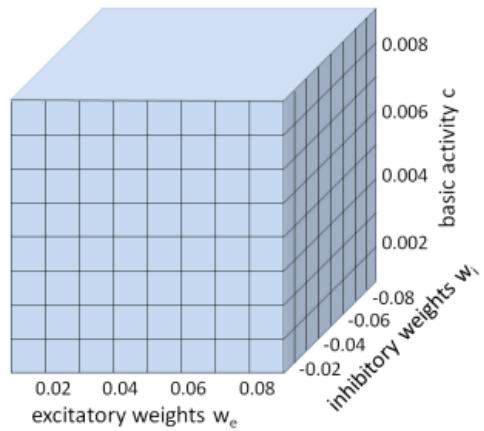
- Phenomenological model
- Cellular automaton
- Firing rate:
$$\lambda_i(t_k) = c_i + \sum_j y_{ji} s_j(t_{k-1})$$
- Inhomogeneous Poisson processes:
$$P_i\{1 \text{ spike within } \Delta t\} = e^{-\lambda_i \Delta t} \cdot \lambda_i \Delta t$$
- Spike Time History
- Parameters obtained by brute force approach with the goal functions spike and burst rate
- Each neuron makes connection to e.g. 10-30% of the population



INEX model consists of Poisson neurons

Brute Force Approach for Parameter

Search:



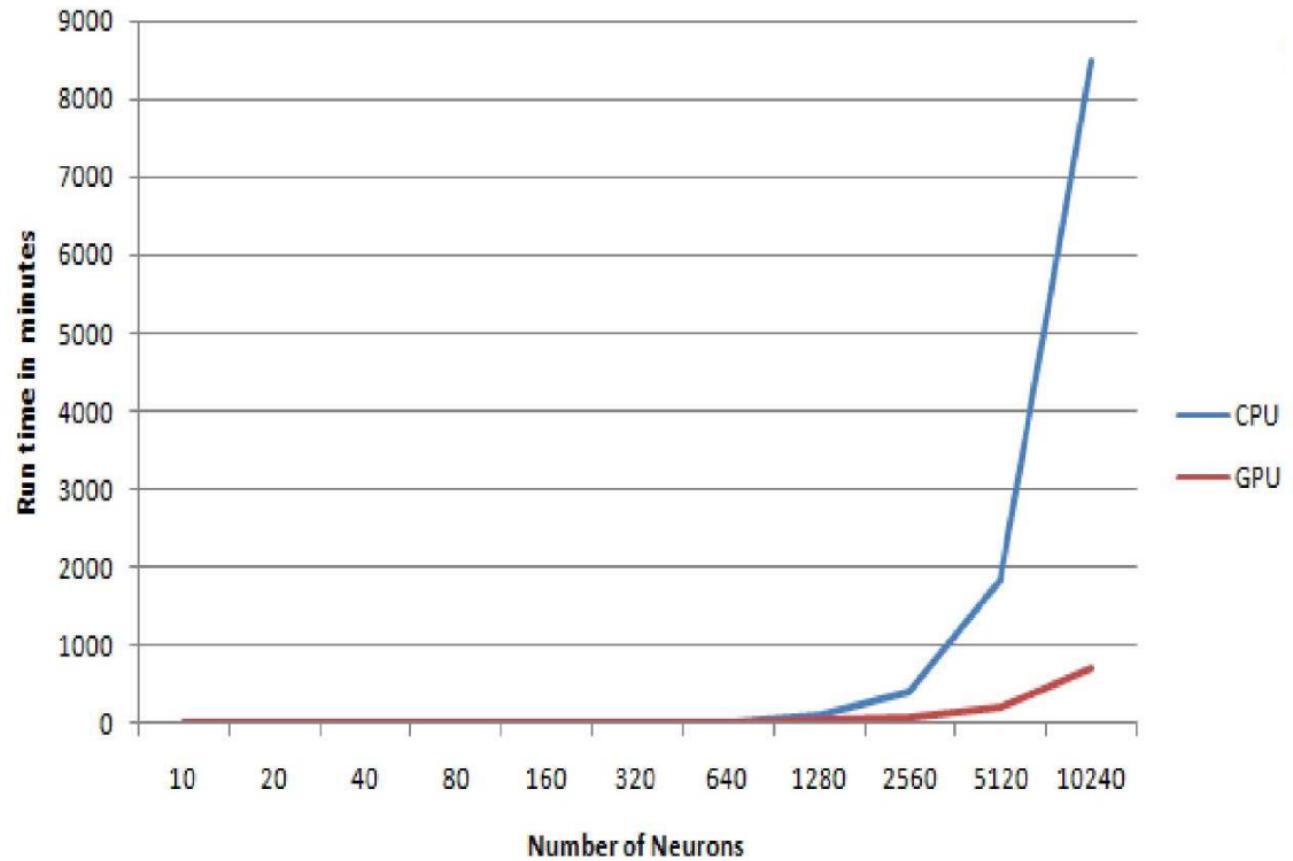
Goal functions:

spike rate + burst rate

Validation:

4-12 calculated features from experimental data

Performance CPU vs. GPU



RESEARCH

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Simulation of developing human neuronal cell networks

Kerstin Lenk^{1*}, Barbara Priwitzer², Laura Ylä-Outinen³, Lukas H. B. Tietz¹, Susanna Narkilahti³
and Jari A. K. Hyttinen¹

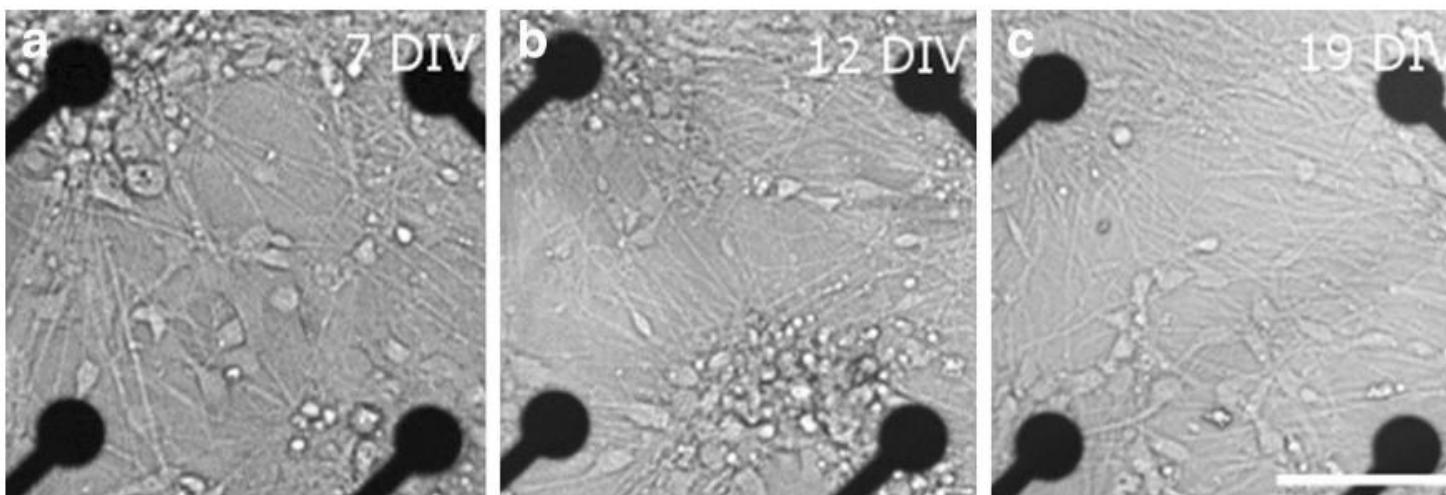
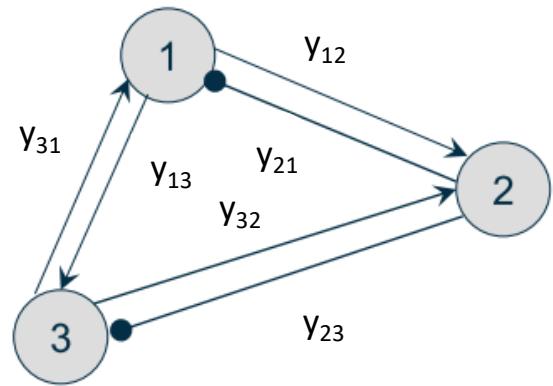


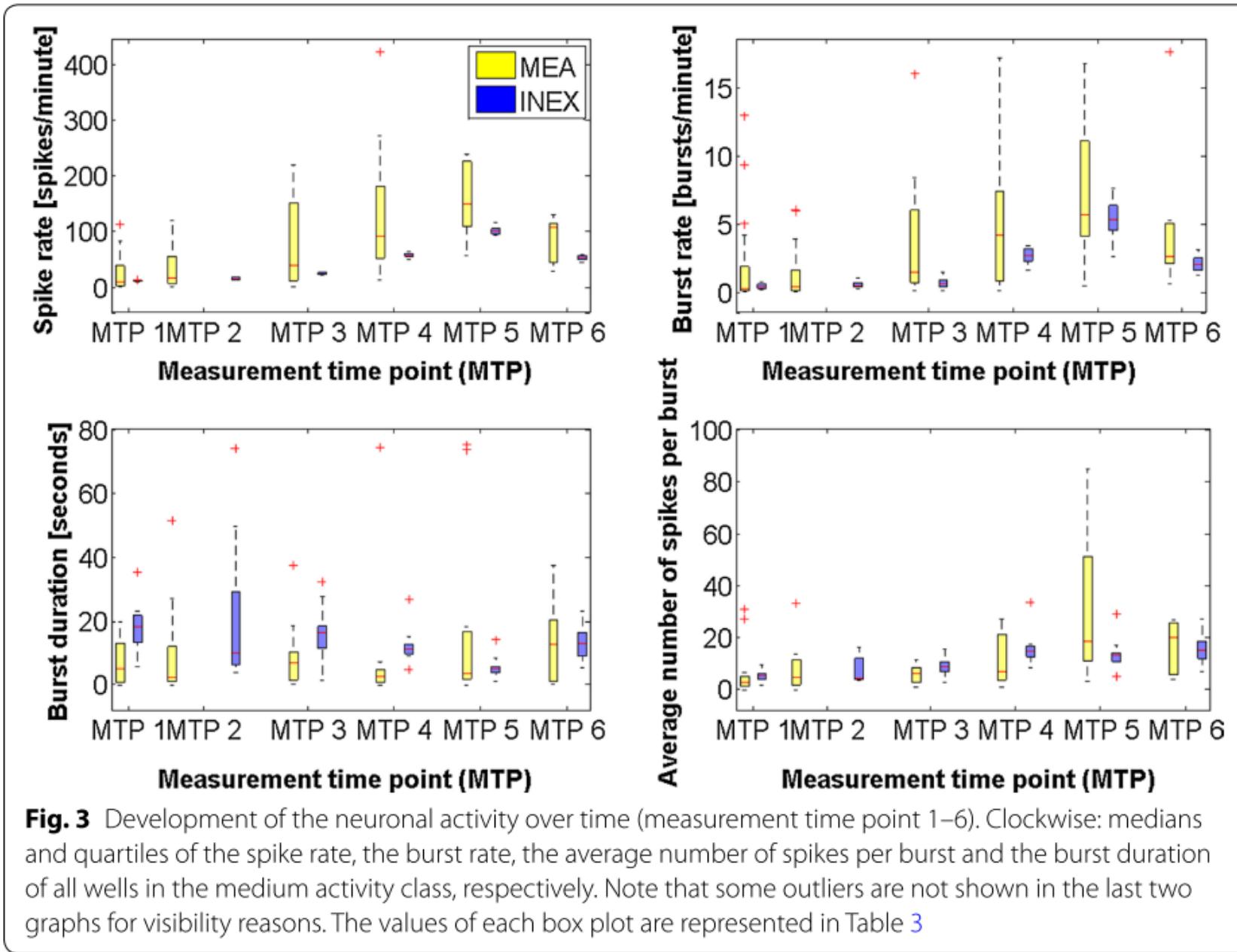
Fig. 1 Neuron distribution of dataset #3 (see Table 1) on the MEA for three points in time **(a** 7 days in vitro (DIV), **b** 12 DIV, and **c** 19 DIV). It is clearly visible that the number of neuronal connections increases and the neurons move over time. The *black dots* indicate the MEA electrodes. The *scale* is 100 μ m

Simulation parameters

- 1000 neurons (80% excitatory/ 20% inhibitory)
- Connectivity is increased linearly between measurement time points (1, 2, 4, 6, 8 and 10 %)
- Brute force approach for synaptic strength and noise term

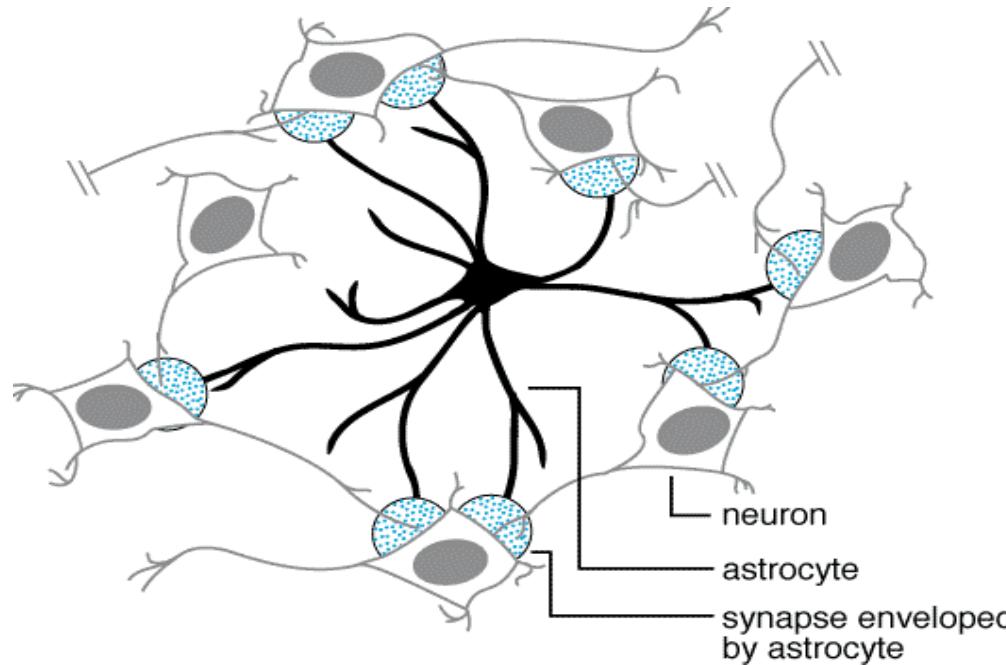


Maturation process reflected by connectivity and synaptic strength

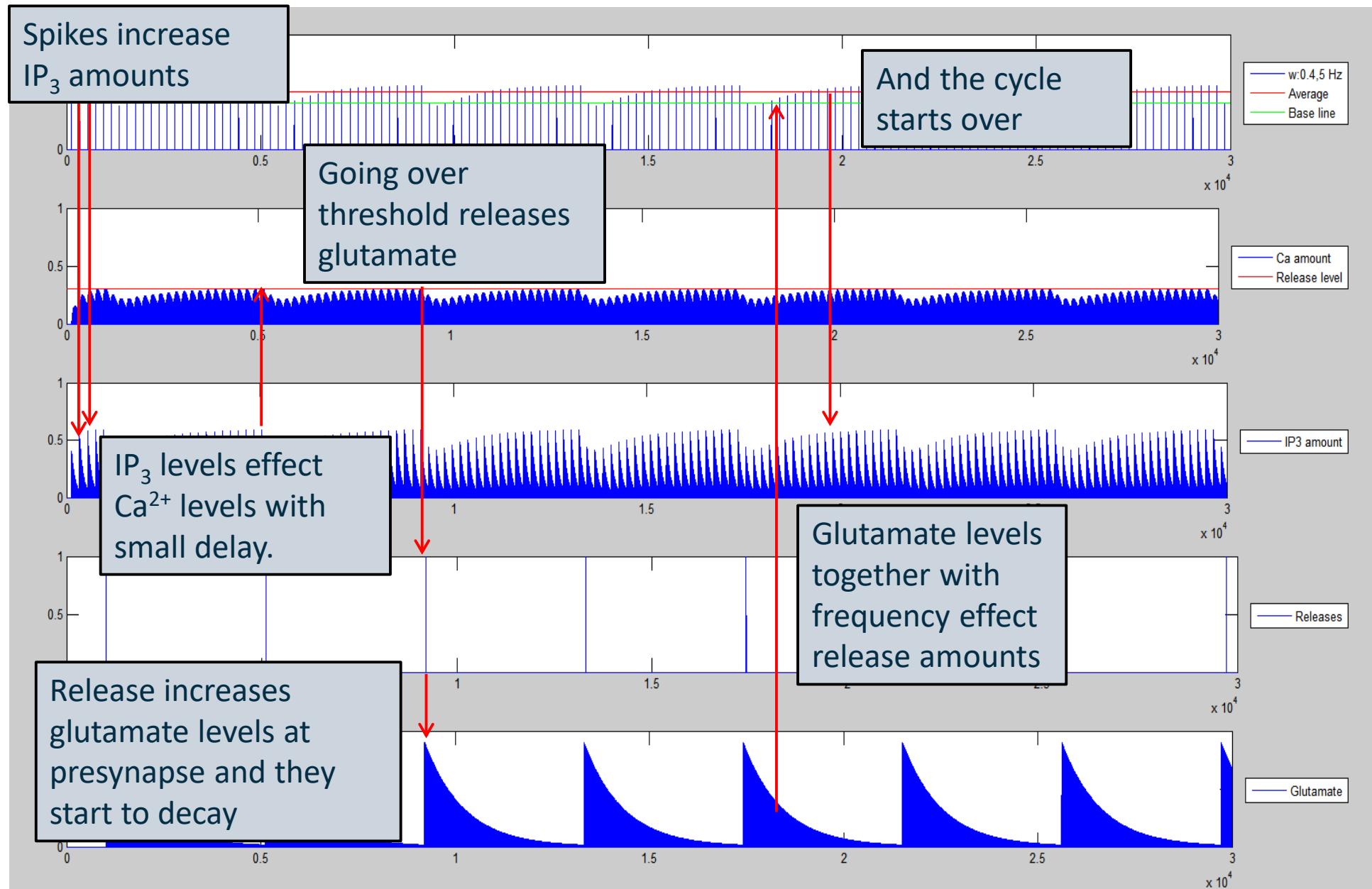


INEXA model: Astrocytes contribution to the neuronal signaling

$$\lambda_i(t_k) = \max(c_i + \sum_j y_{ij} \cdot s_j(t_{k-1}) - \sum_j y_{Astro} \cdot A_{ija}(t_{k-1}), 0)$$

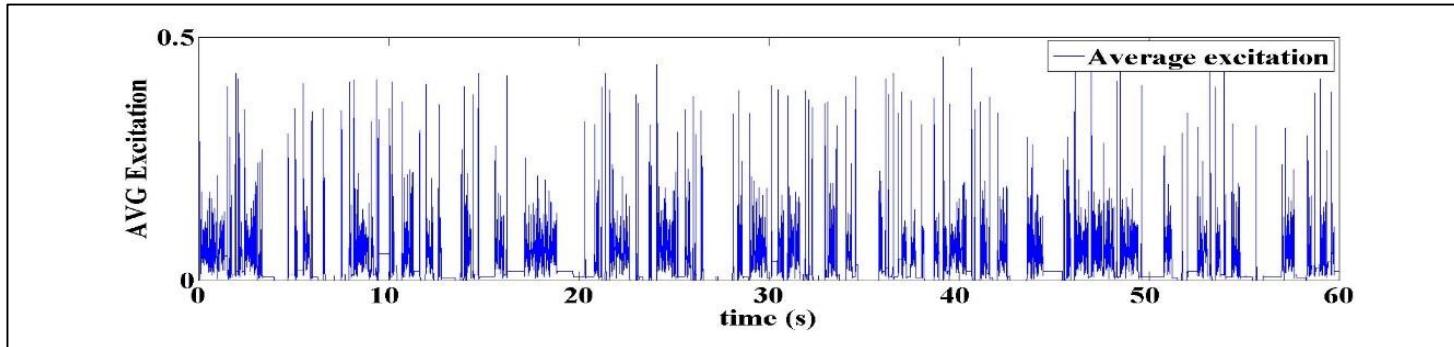


Spike-triggered calcium release

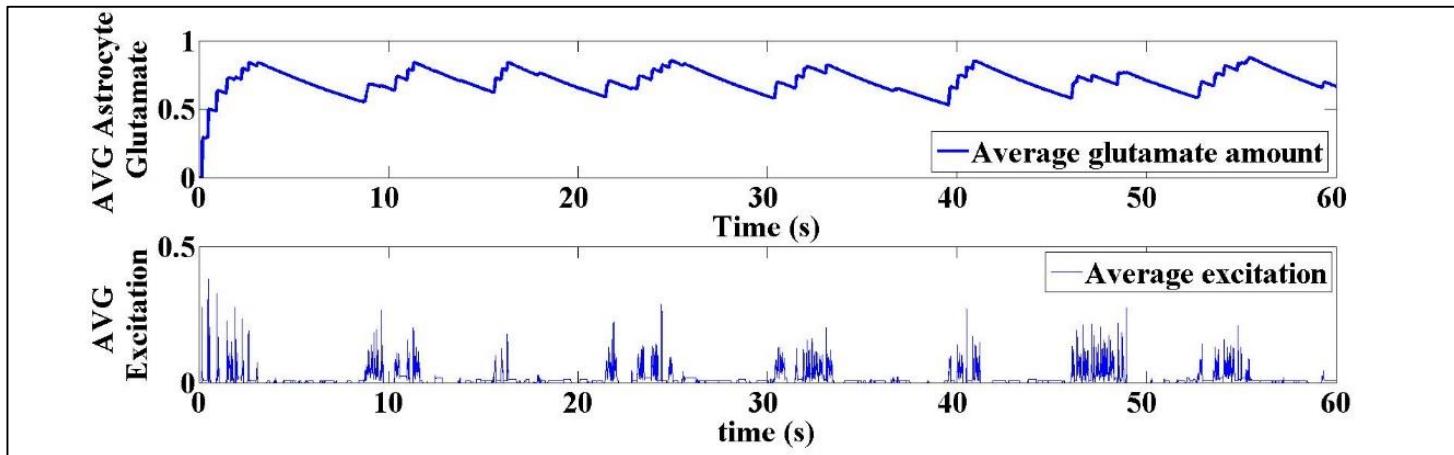


Activity of a single synapse alters from non-bursting behavior to bursting when astrocytes are present

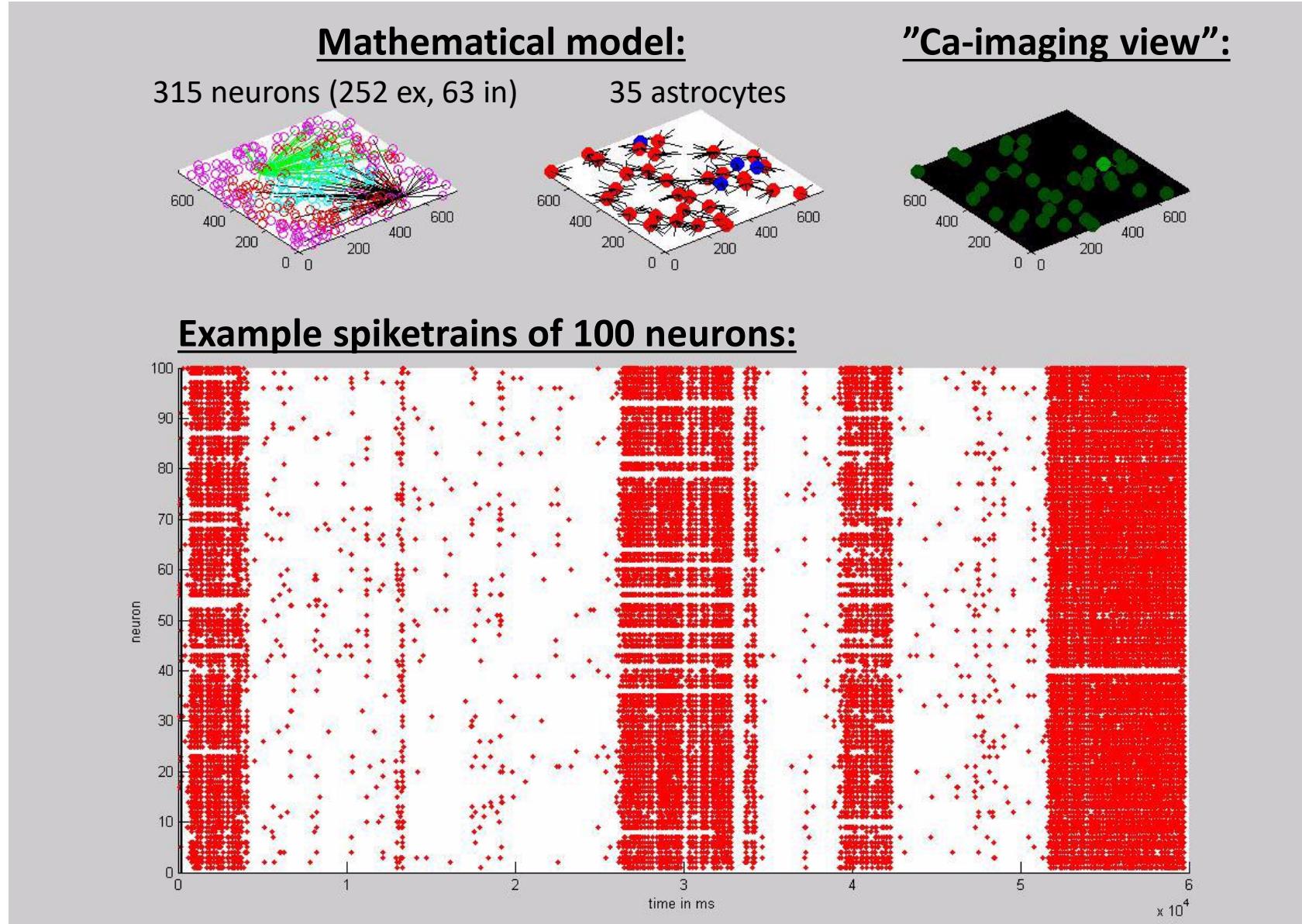
Without astrocyte control (100 neurons)



With astrocyte control (100 neurons, 80 astrocytes)



Neuronal firing follows astrocytic calcium dynamics



Number of astrocytes influences the neuronal network activity

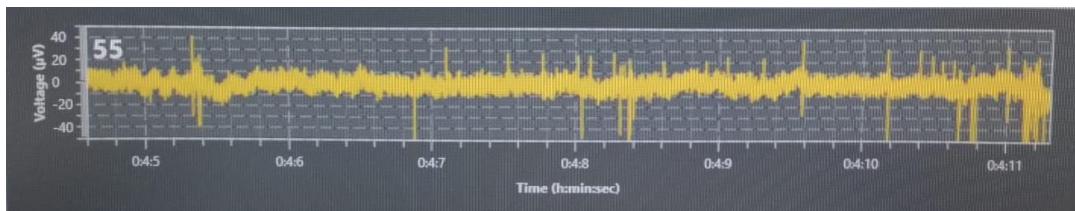
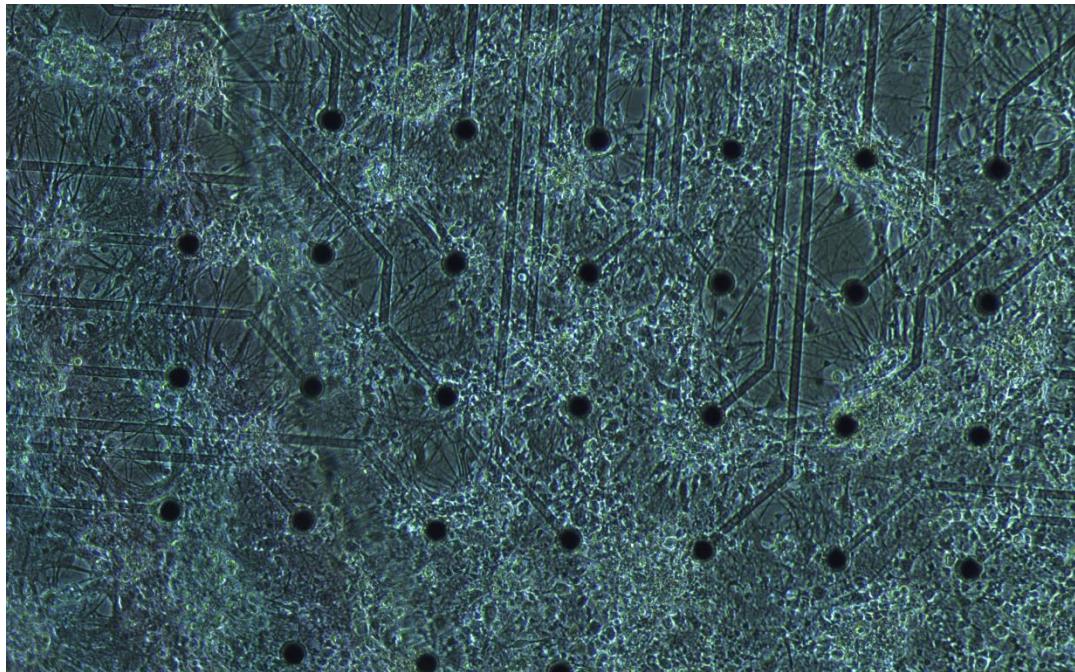
Connectivity

Signaling at the tripartite synapse

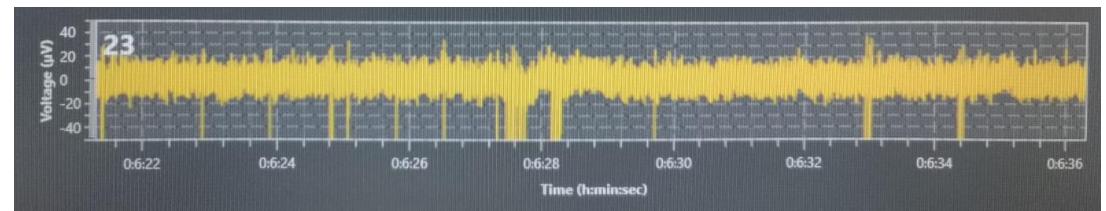
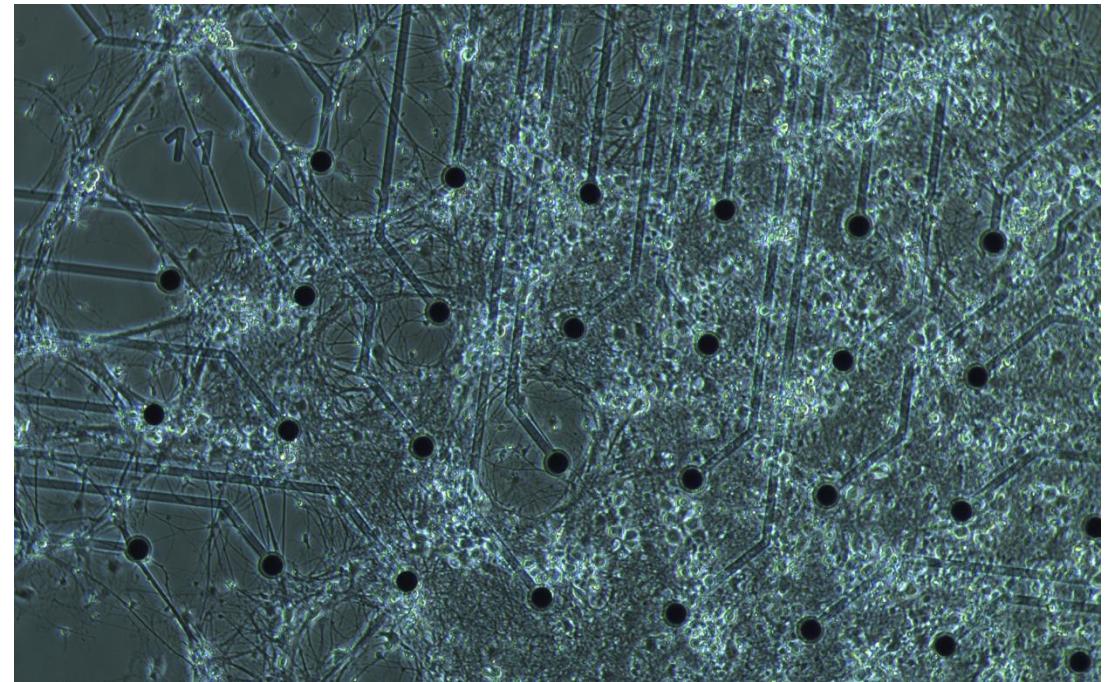
Astrocytes reduce the spike and burst rate but increase the burst duration

Experimental (rat) data on the way

90% neurons, 10% astrocytes

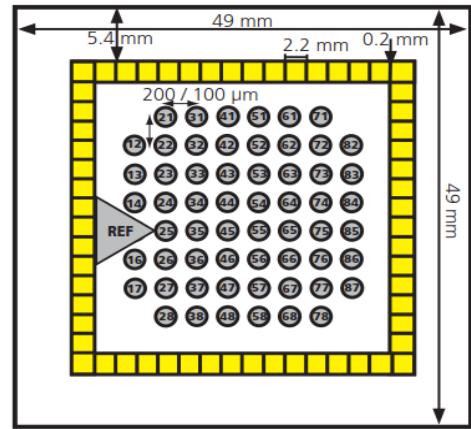
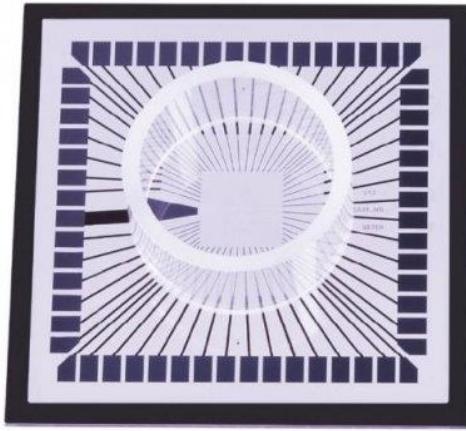


70% neurons, 30% astrocytes



First example of our current work: epilepsy model

Second example of our current work: responses to stimuli

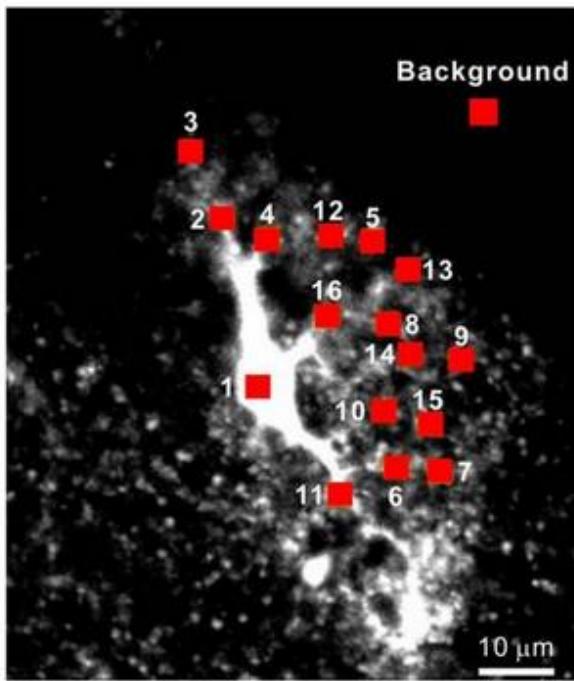


Astrocyte Ca activation; neuronal system driven by noise vs. stimulus

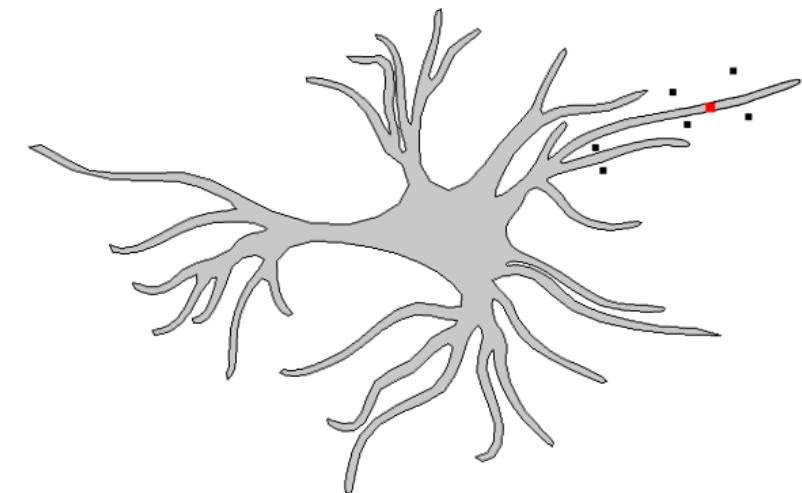
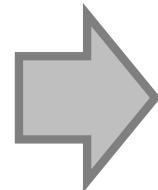
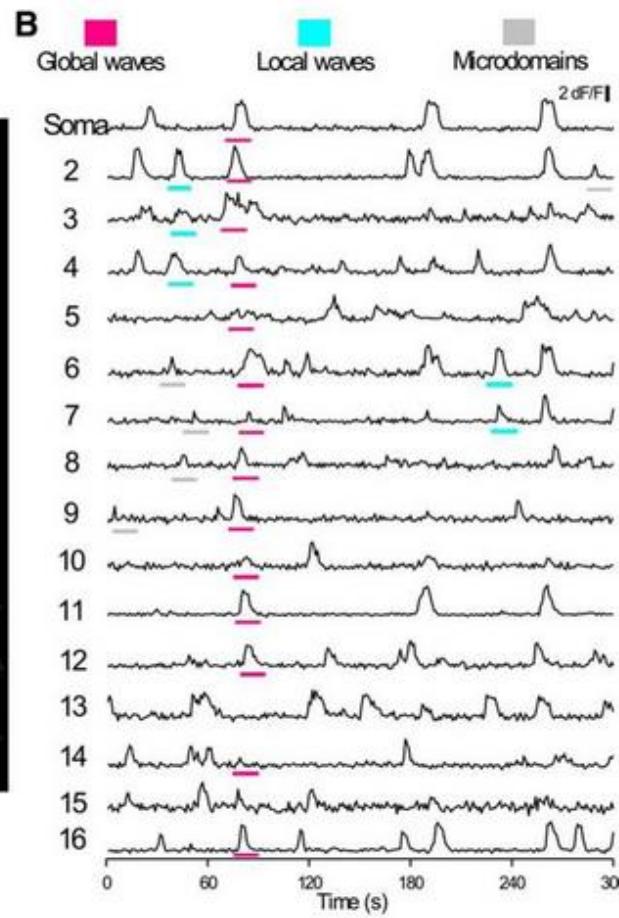
Astrocyte Ca^{2+} activation in "epileptic" neuronal activity

Single cell astrocyte model

A

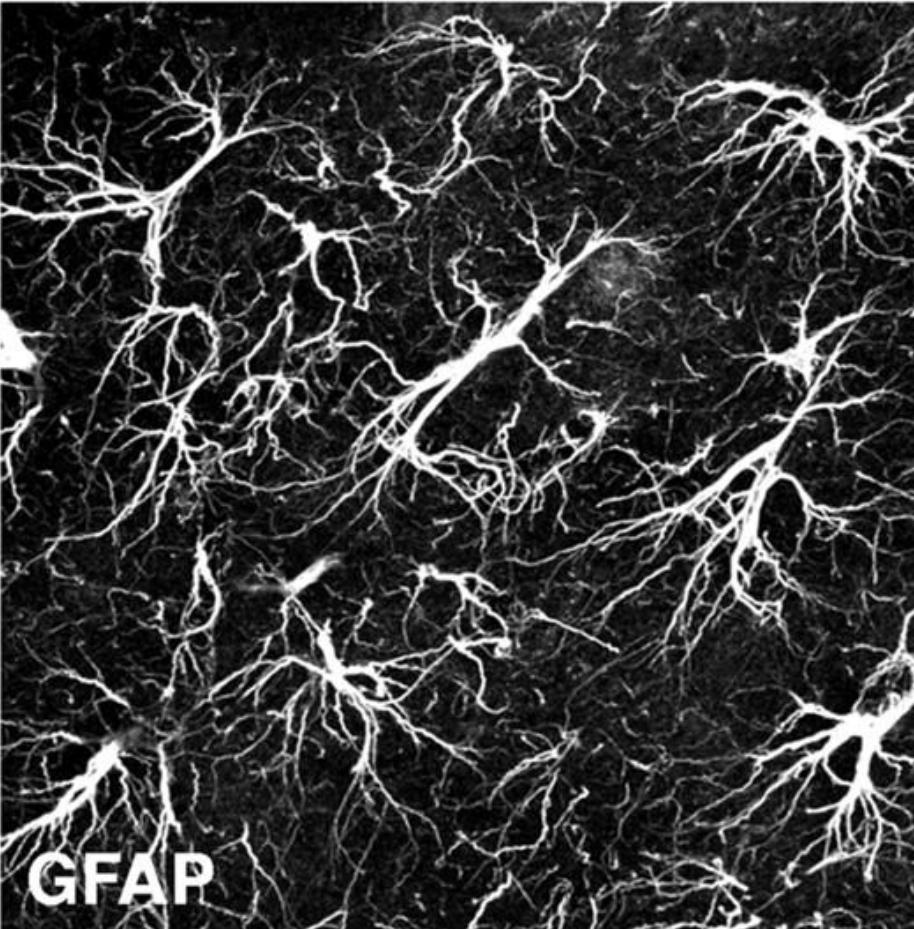


B

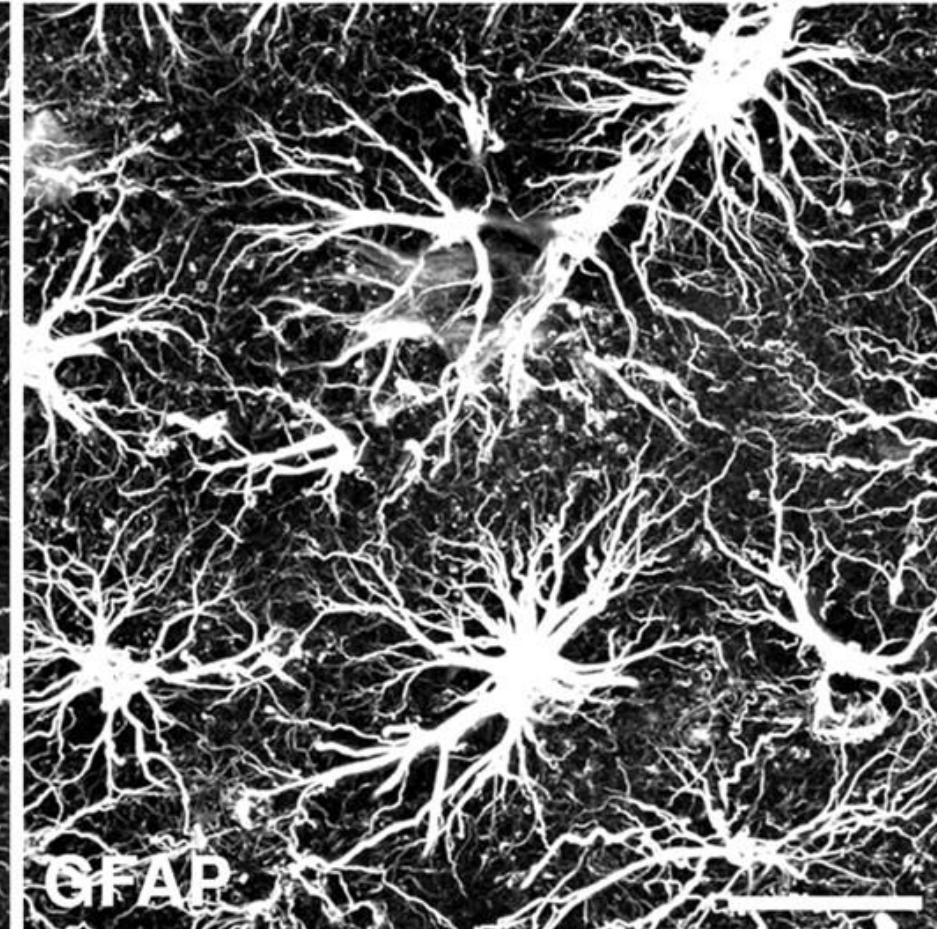


In Alzheimer's disease, astrocytes undergo morphological and functional changes

Nonreactive astrocytes



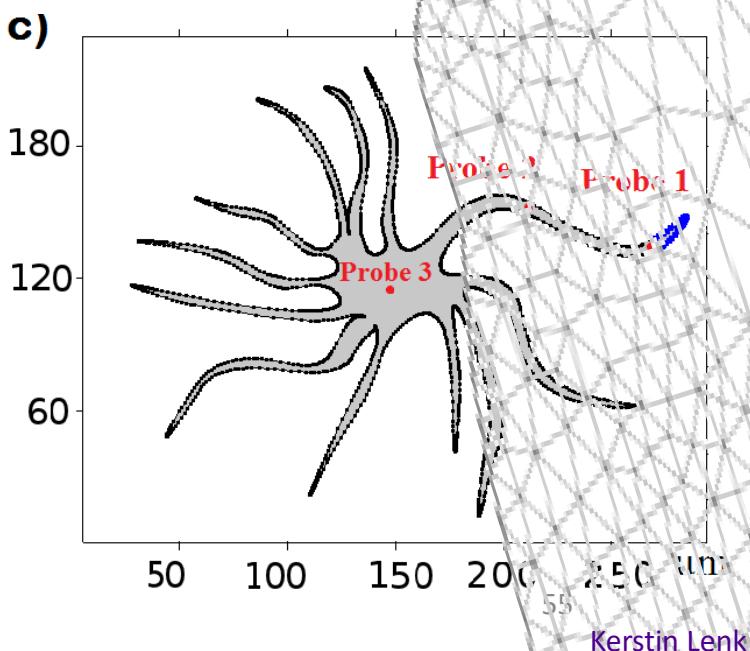
Reactive astrocytes



Model implementation as 2D FEM

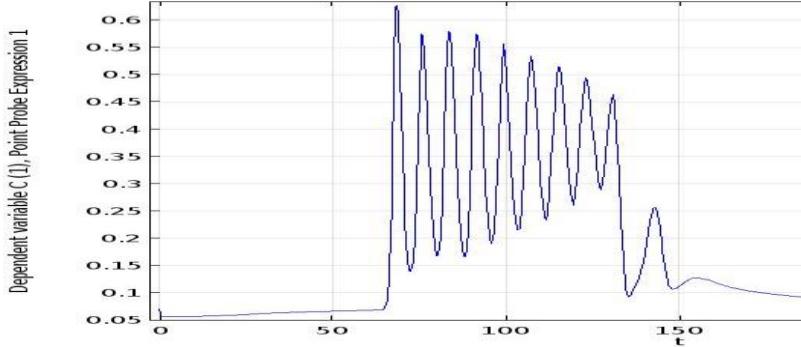
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- Model Based on G-ChI model of De Pitta et al., 2009
- Implementation into COMSOL Multiphysics
- Addition: Diffusion of the IP_3 and calcium in cell
- Boundary condition: input of glutamate e.g. from synapses

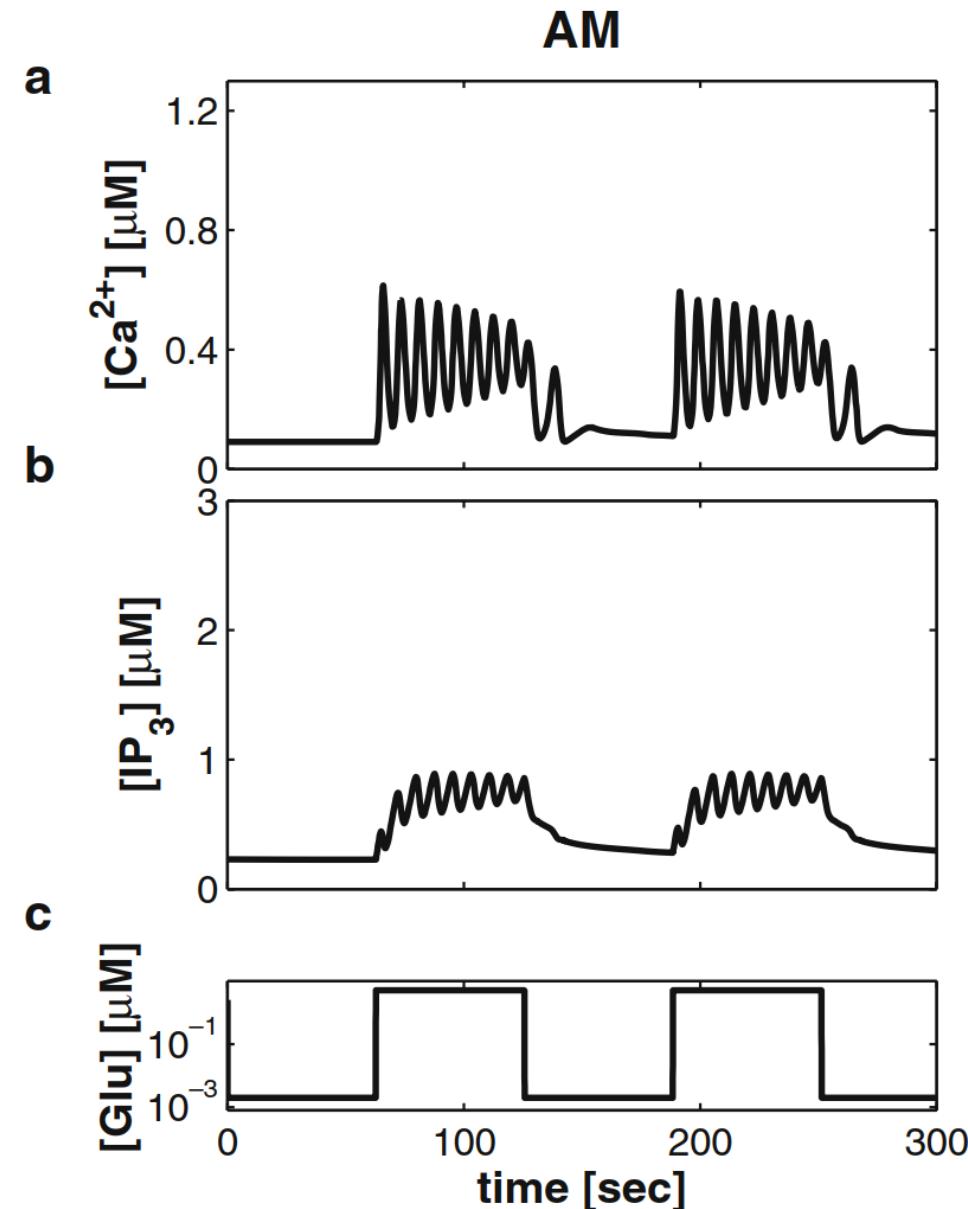


Replication of De Pitta – FEM simulation without spatial dimensions ("0D")

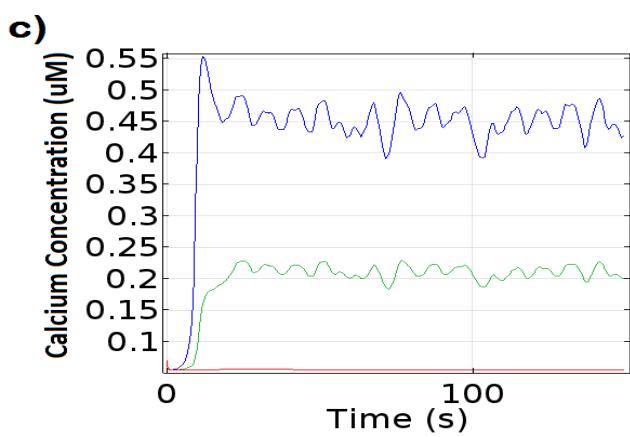
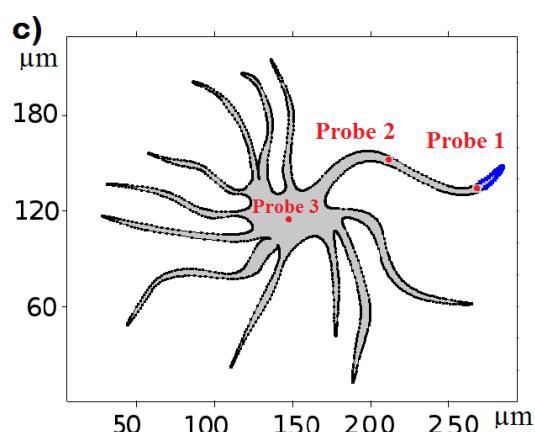
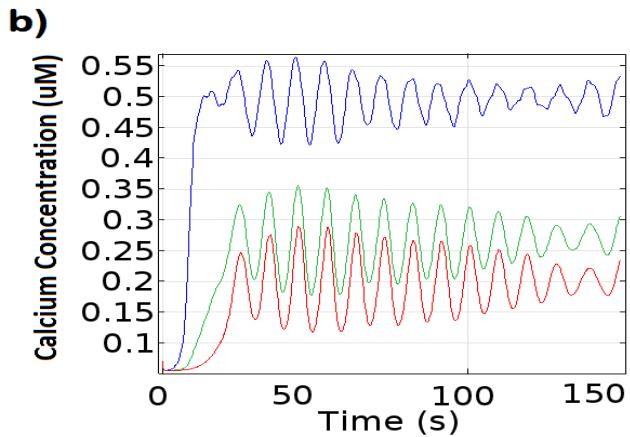
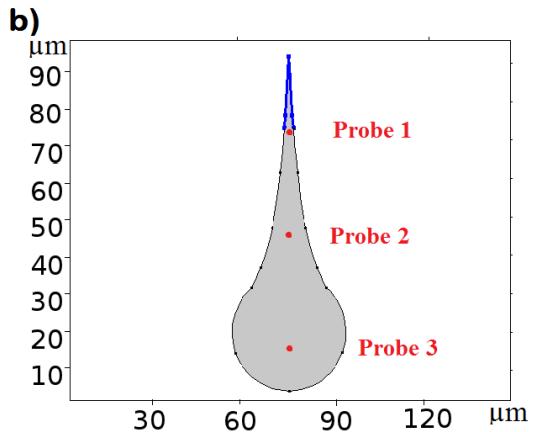
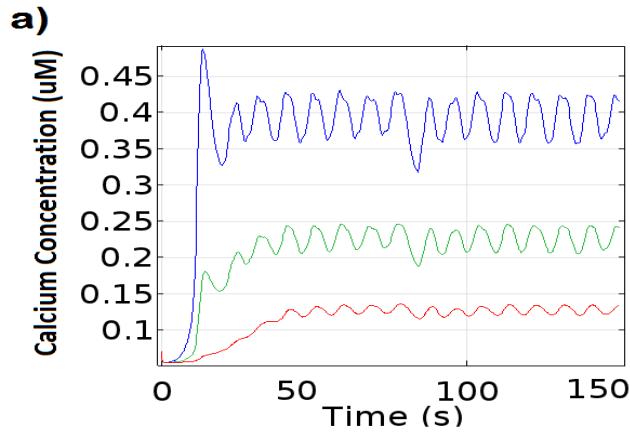
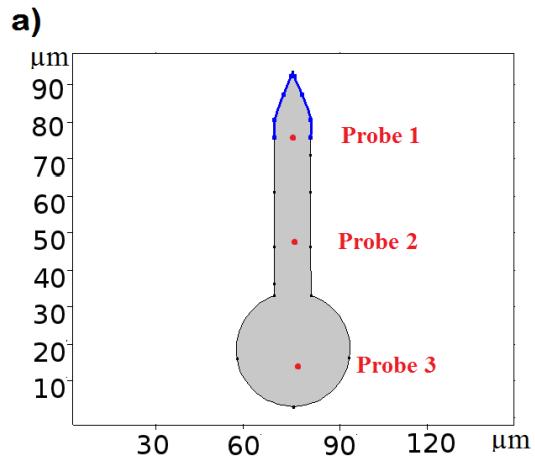
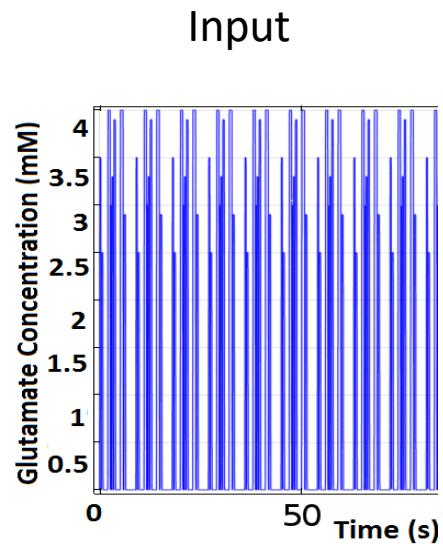
Resulting
Calcium in
astrocyte



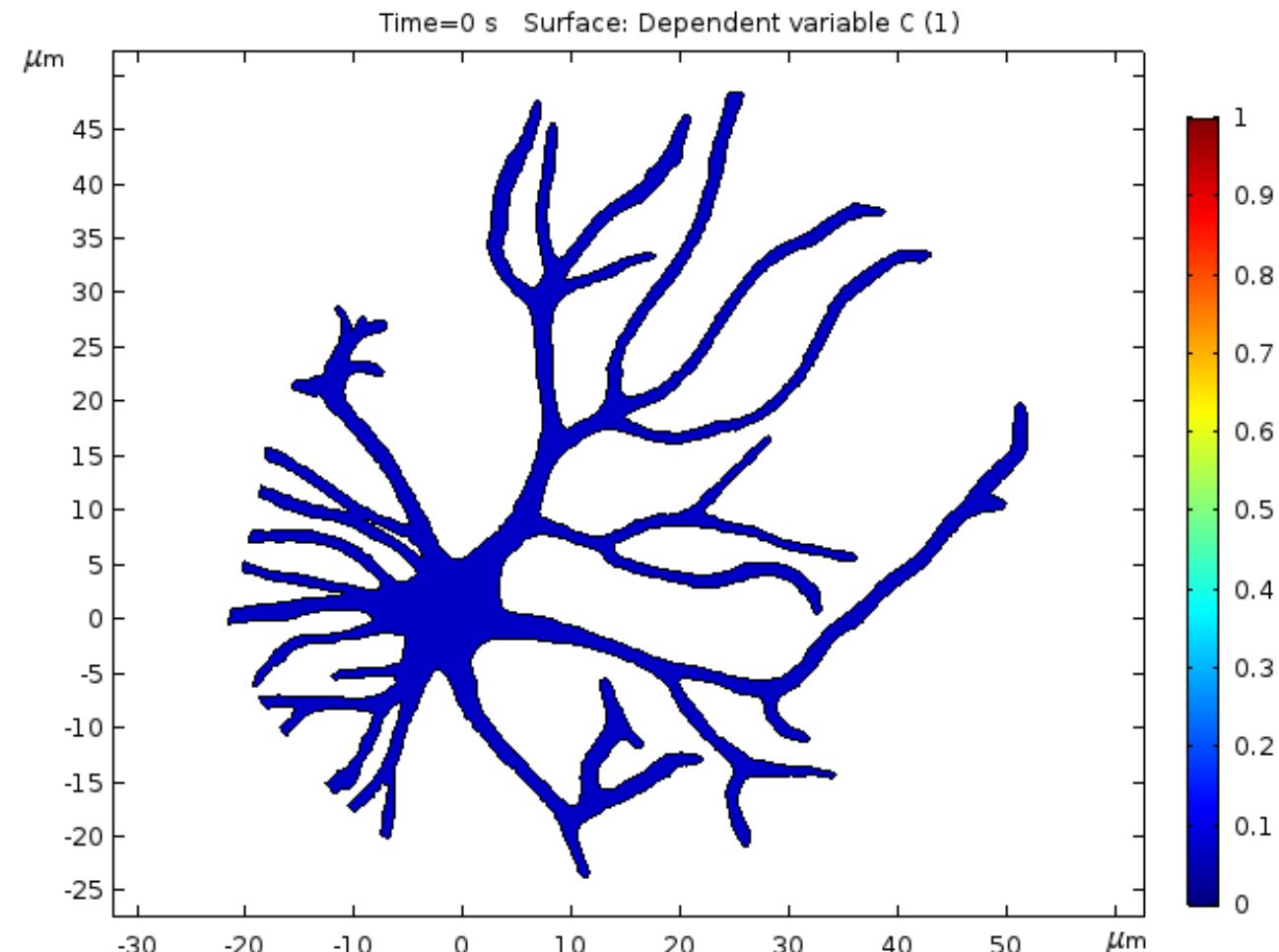
Glutamate
stimulus



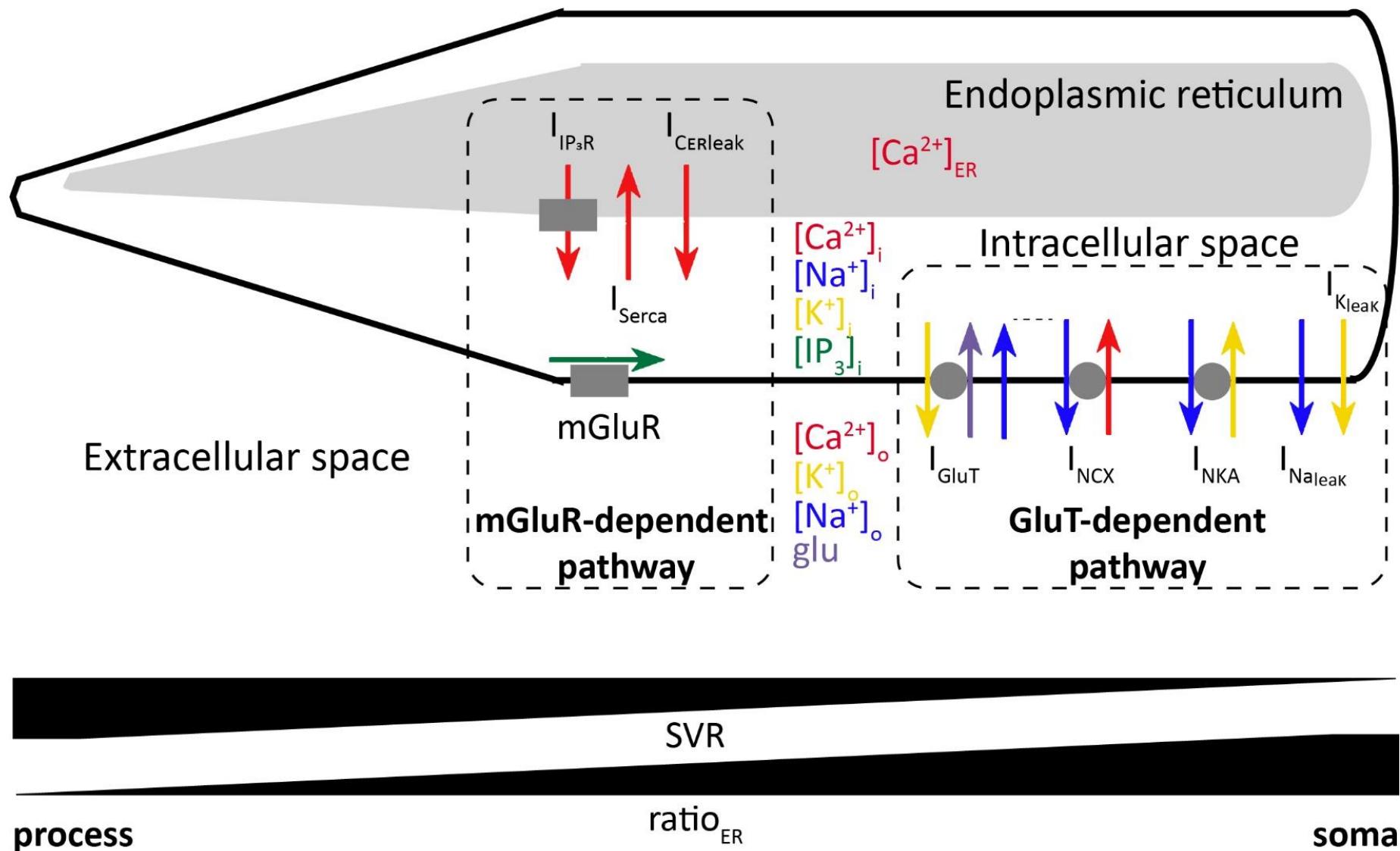
Different geometries



Astrocyte calcium after "synaptic" local release of glutamate



Implementation of glutamate pathways and ER distribution



Governing equation

$$\frac{d[Ca^{2+}]_i}{dt} = \frac{A}{F \cdot Vol} \cdot I_{NCX} + \frac{A \cdot \sqrt{ratio_{ER}}}{F \cdot Vol} \cdot (I_{IP_3R} - I_{SERCA} + I_{CERleak})$$

I_{NCX} = Na^{+}/Ca^{2+} exchanger

I_{IP_3R} = Ca^{2+} current through the IP3 receptor channel

I_{SERCA} = SERCA pump

$I_{CERleak}$ = Ca^{2+} leak from the ER

A = area of the outer cell membrane

F = Faraday constant

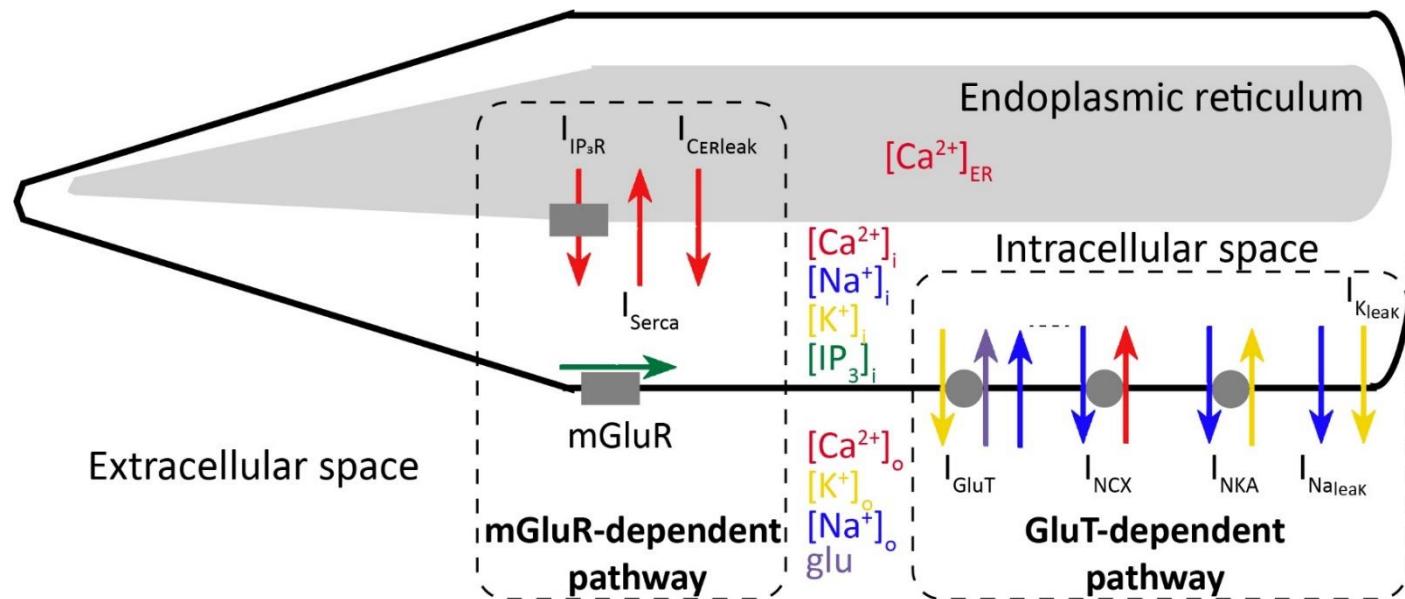
Vol = volume of the intracellular space

$A \cdot \sqrt{ratio_{ER}}$ = area of the internal Ca^{2+} store

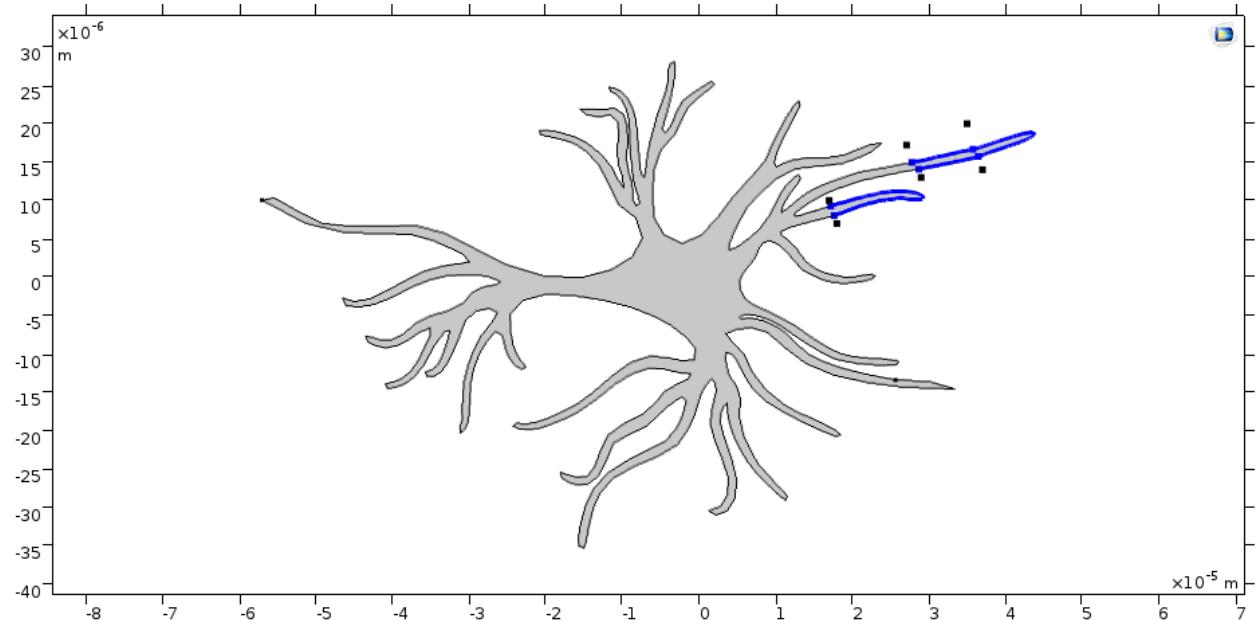
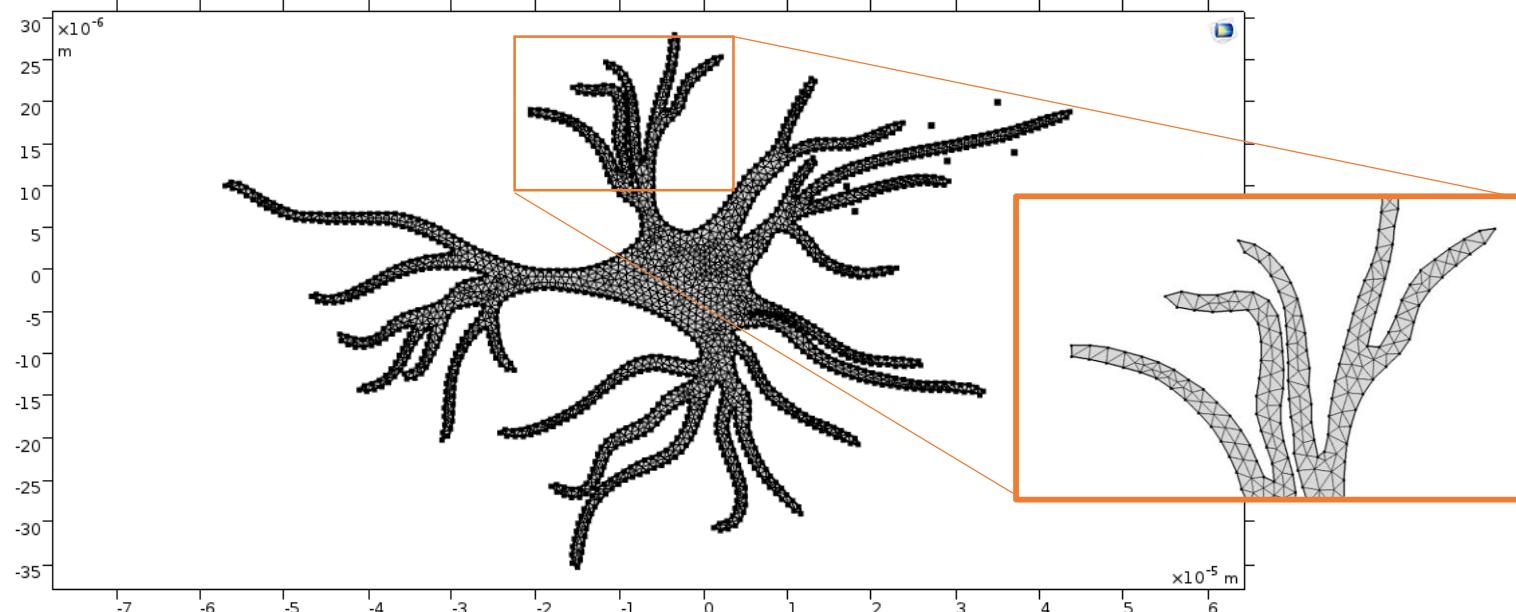
RESEARCH ARTICLE

Spatial separation of two different pathways accounting for the generation of calcium signals in astrocytes

Franziska Oschmann^{1,2✉}, Konstantin Mergenthaler¹, Evelyn Jungnickel¹, Klaus Obermayer^{1,2✉}



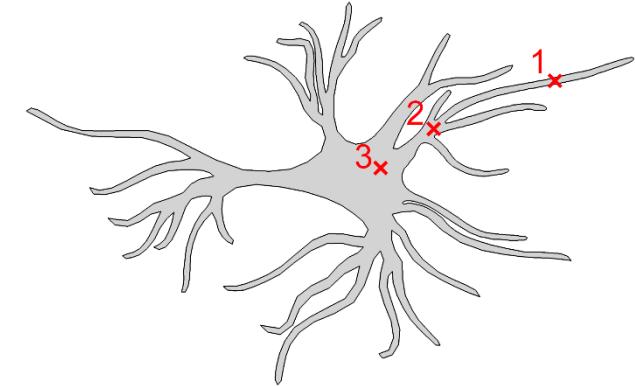
Constant glutamate stimulus at process(es)



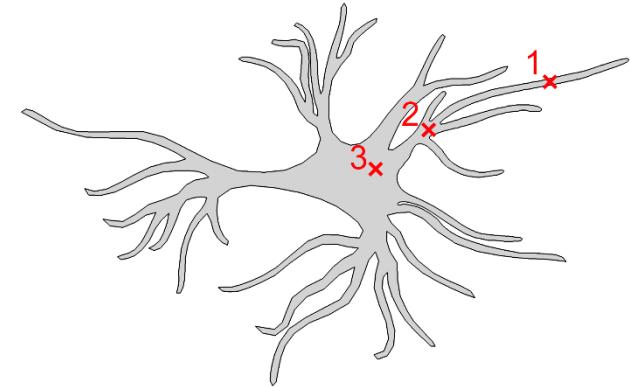
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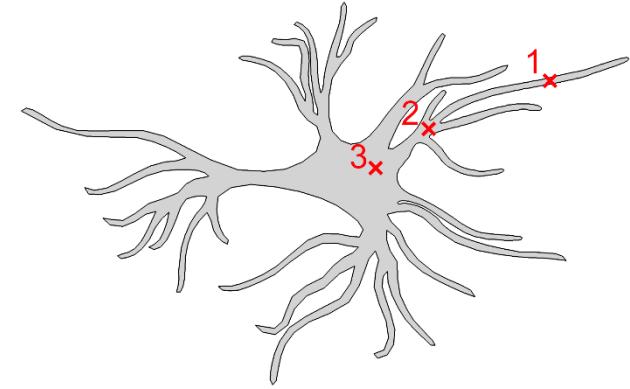
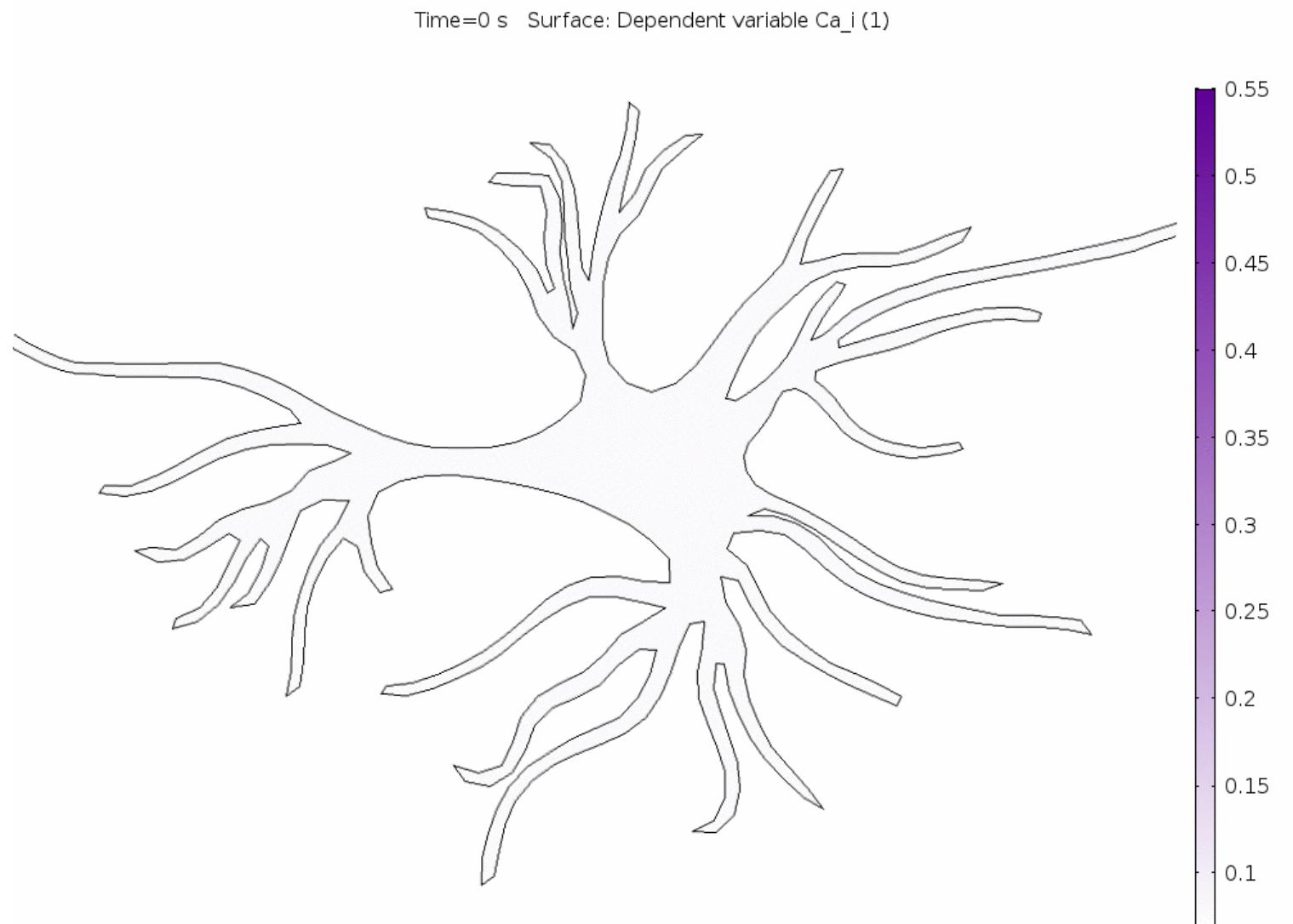
One stimulation site



Three stimulation sites



Three stimulation sites



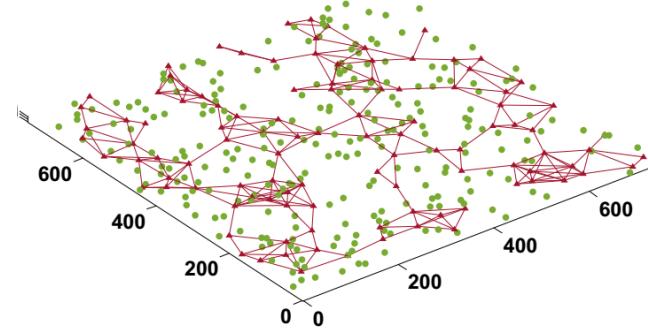
Work together with Aapo Tervonen

Kerstin Lenk

Conclusions

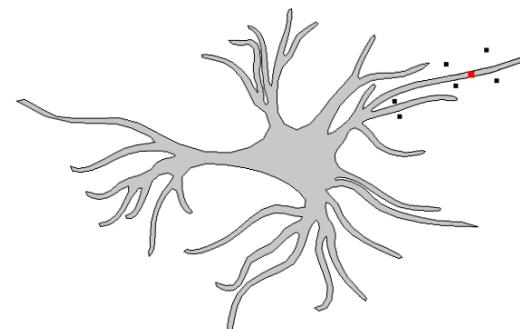
(1) INEXA model:

- One of the first neuron-astrocyte network models where one astrocyte is connected to several hundreds of excitatory synapses
- Astrocyte control over neurons can have profound effects to network behavior → astrocytes prolong the burst duration of neurons, while restricting hyperactivity
- The model is only using part of the pathways astrocytes are known to have

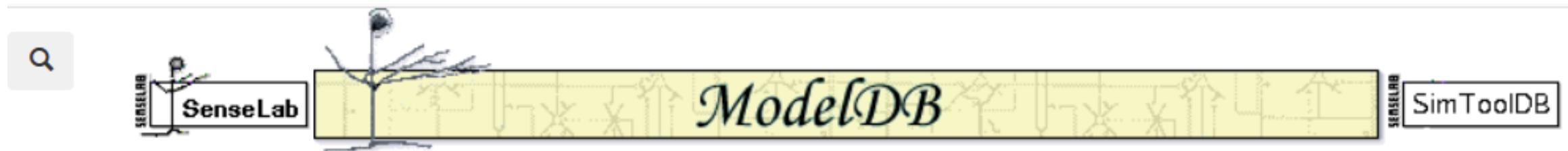


(2) Single cell astrocyte model:

- Calcium spread based on number of input sides
- Next steps: different morphologies, gap junction coupling with adjacent astrocyte, 2D vs 3D



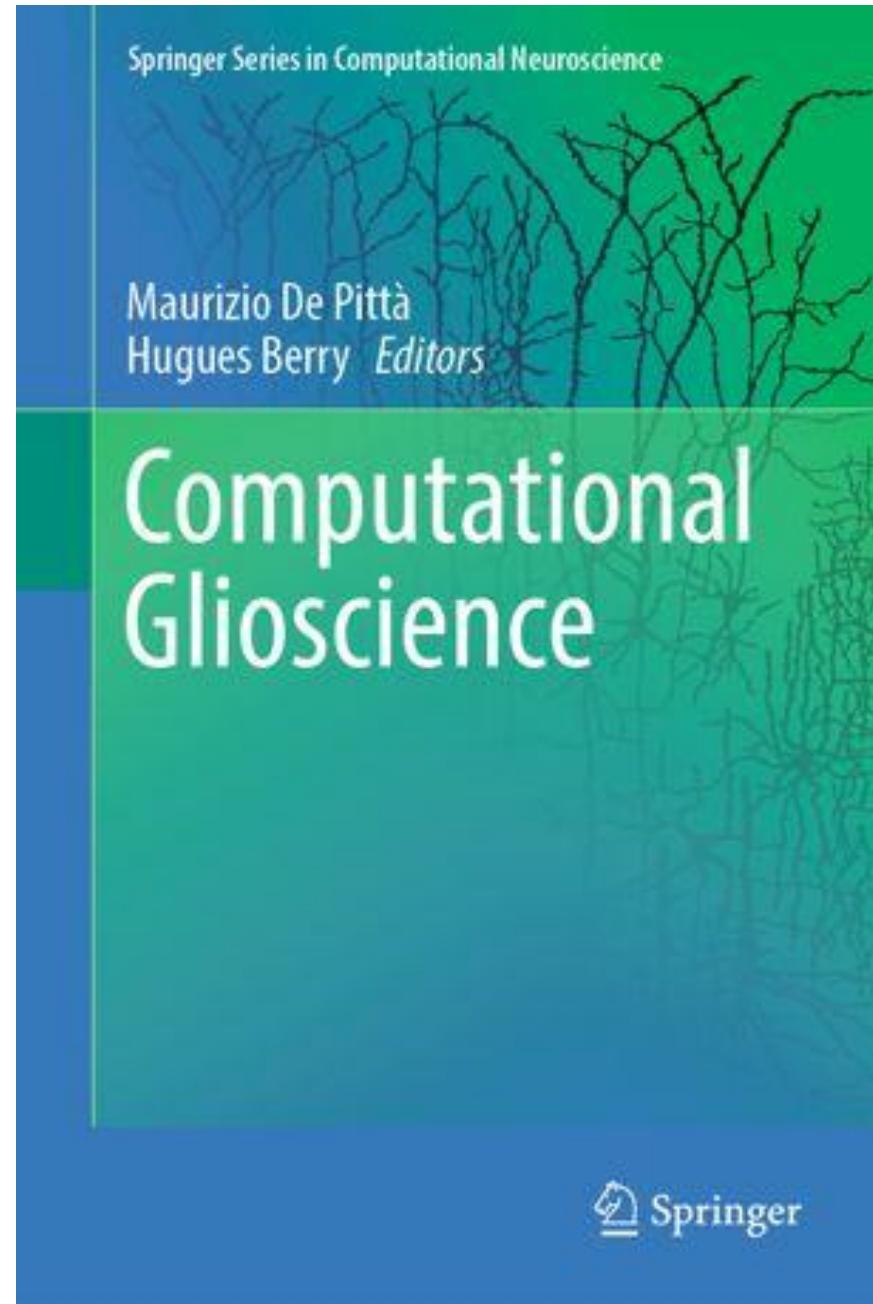
ModelDB - <https://senselab.med.yale.edu/modeldb/>



[Submit Model](#)

ModelDB provides an accessible location for storing and efficiently retrieving computational neuroscience models. ModelDB is tightly coupled with [NeuronDB](#). Models can be coded in any language for any environment. Model code can be viewed before downloading and browsers can be set to auto-launch the models. For further information, see [model sharing in general](#) and [ModelDB in particular](#).

Browse or search through over 1000 models using the navigation on the left bar or in the menu button on a mobile device. To search papers instead of models, go [here](#); this may be used to identify models whose paper cites or is cited by a given paper.



Main parts:

- Introduction
- Calcium Dynamics
- Tripartite Synapse and Regulation of Network Activity
- Homeostasis and Metabolic Coupling
- Computational Tools to Analyze and Model Astrocyte Experiments

Save the date:
Nordic Organ on Chip Workshop
"3rd" NOoC Workshop
22-23 August 2019
Tampere, Finland

Workshop is for PIs and researchers. During the meeting we will arrange two workshop sessions with oral presentations and a poster session/ hands-on training. On Thursday evening we are planning to have a get-together with outdoor activities and dinner.

For more information, contact
mari.pekkanen-mattila@tuni.fi



49th Computing in
Cardiology CinC2022
September 2022
Tampere, Finland

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Katja Nieweg, Philipps-University Marburg, Germany

AND YOU!

